



Disruption Mitigation: 3D MHD Simulations and Plans for Experimental Validation

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Acknowledge conversations with: Carl Sovinec (UW), Scott Kruger (TechX), Val Izzo (UCSD), Paul Parks (GA), Eric Hollmann (UCSD), Karsten McCollam (UW), Nate Hicks (UAA), David Ennis (AU), David Rasmussen (ORNL), Larry Baylor (ORNL), Mark Lyttle (ORNL), Giovanni Cone (LANL).

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Abstract

Two disruption scenarios are modeled numerically by use of the CORSICA 2D equilibrium and NIMROD 3D MHD codes.

The work follows the simulations of Kruger for pressure-driven modes in DIII-D and Strauss for VDEs in ITER.

The aim is to provide starting points for simulation of tokamak disruption mitigation techniques currently in the CDR phase for ITER.

- *Pressure-driven instability growth rates previously observed in simulations of DIII-D are verified;*
- *Halo and Hiro currents produced during vertical displacements are observed in simulations with implementation of resistive walls for ITER*

We discuss plans to exercise new code capabilities and validation.

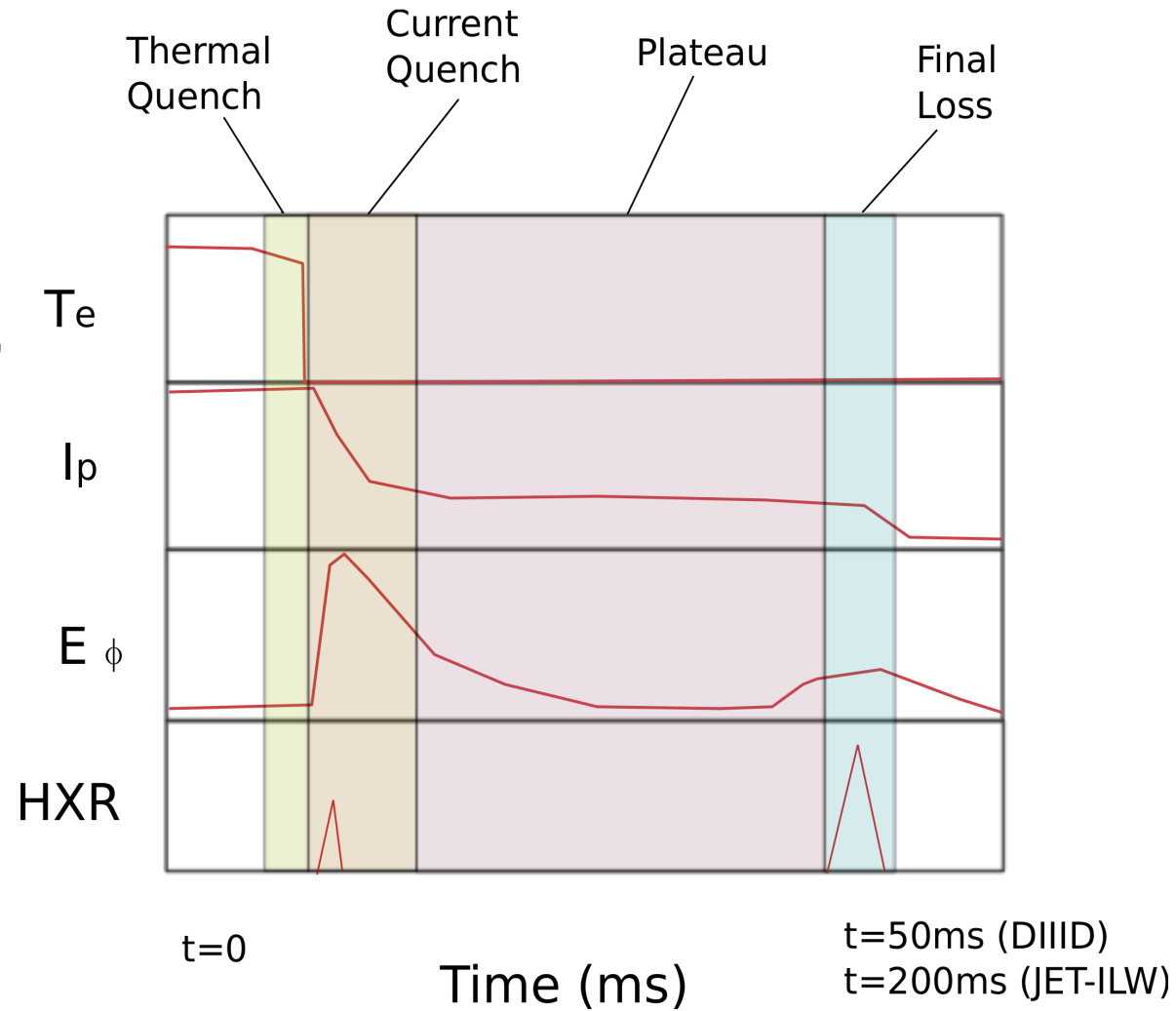
Disruptions in tokamaks

Large disruption taxonomy [1], with ~same anatomy (\rightarrow [2])

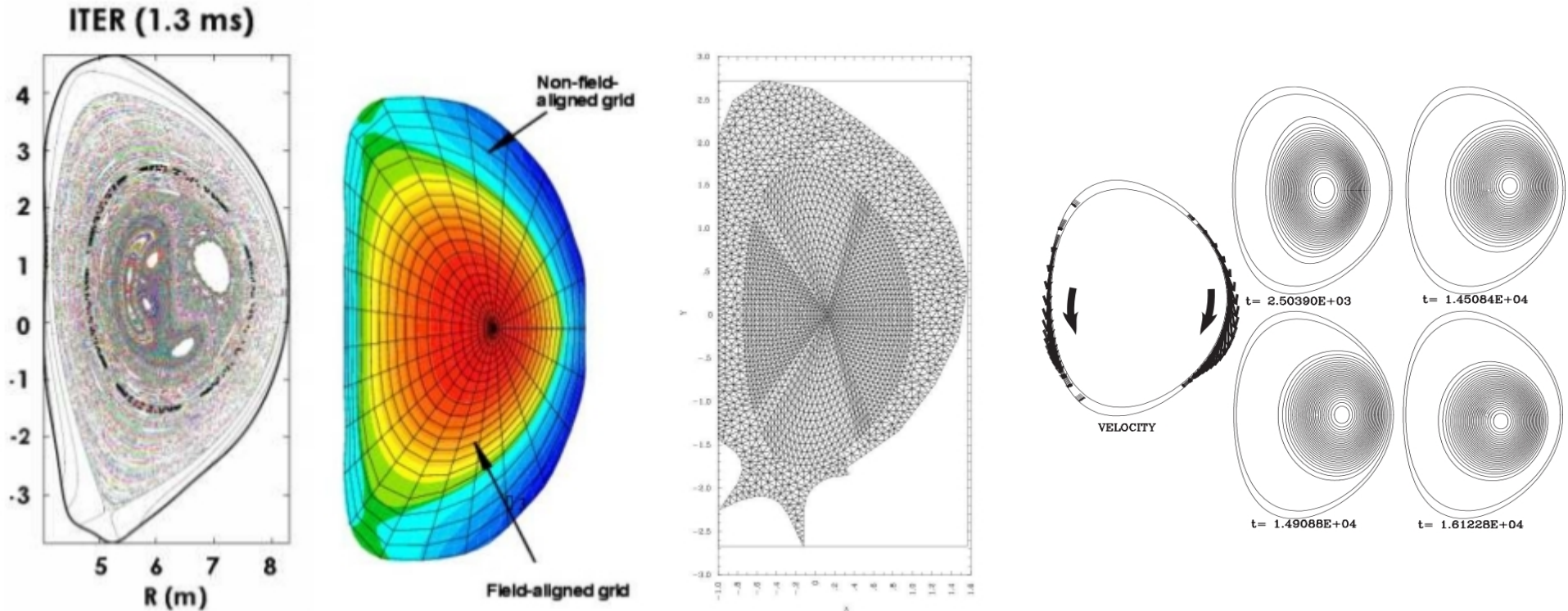
Current philosophy is to control the plasma to avoid disruptions, and mitigate if necessary.

Mitigation aims to: 1) limit impacts of CQ on in-vessel components; 2) suppress REs.

Main options right now: rapid massive pellet injection or rapid massive gas injection [3].



Prior disruption simulations



Izzo [4]

Kruger [5]

Strauss [6]

Aydemir [7]

Prior work focused on: REs, VDEs, halo / hiro current, and wall current.

We start with verification of Kruger [5] and Strauss [6], implementing NIMROD BCs like Aydemir [7].

Initial conditions

CORSICA [8] is a 1.5D plasma simulation code, coupling equilibrium, stability and transport: used for ITER, NSTX, DIII-D and other major fusion systems, which we operate under license to LLNL.

Light Tools

Ray-tracing in realistic geometries (obtained from CATIA engineering drawings) [10].

Engineering CAD

CATIA / STP compatible CAD.

3D MHD

The **NIMROD** code [9] solves non-linear initial value problems in 2 fluid MHD with the addition of the Hall term. Finite elements in the poloidal plane and Fourier series in the toroidal direction. Used extensively for tokamaks, including ITER, NSTX, DIII-D and for compact tori.

Stability

DCON is a code for determining the MHD stability of static axisymmetric toroidal plasma. It uses an algorithm, developed by Newcomb for cylindrical plasmas and generalized by Glasser to axisymmetric plasmas [11].

(2013 NERSC allocation: 200k hours)

DIII-D Shot #087009: initial condition

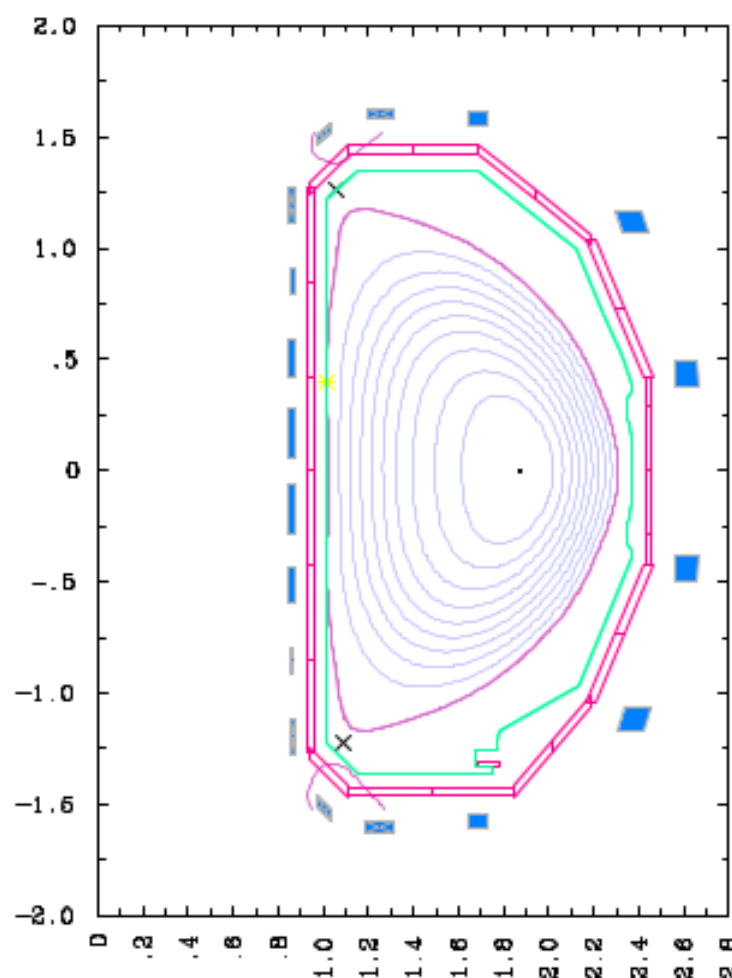
DIII-D shot #087009 @ 1.675 s
Constructed from g087009p2.01675

Kinetic EFIT at
 $t=1.675\text{ms}$.

Pressure increased to
marginal stability with
CORSICA/DCON.

Fixed-boundary:
 $S \sim 1e5 - 1e6$
 $n=0,1$

Free-boundary:
 $S \sim 1e5$
 $n=0,1$



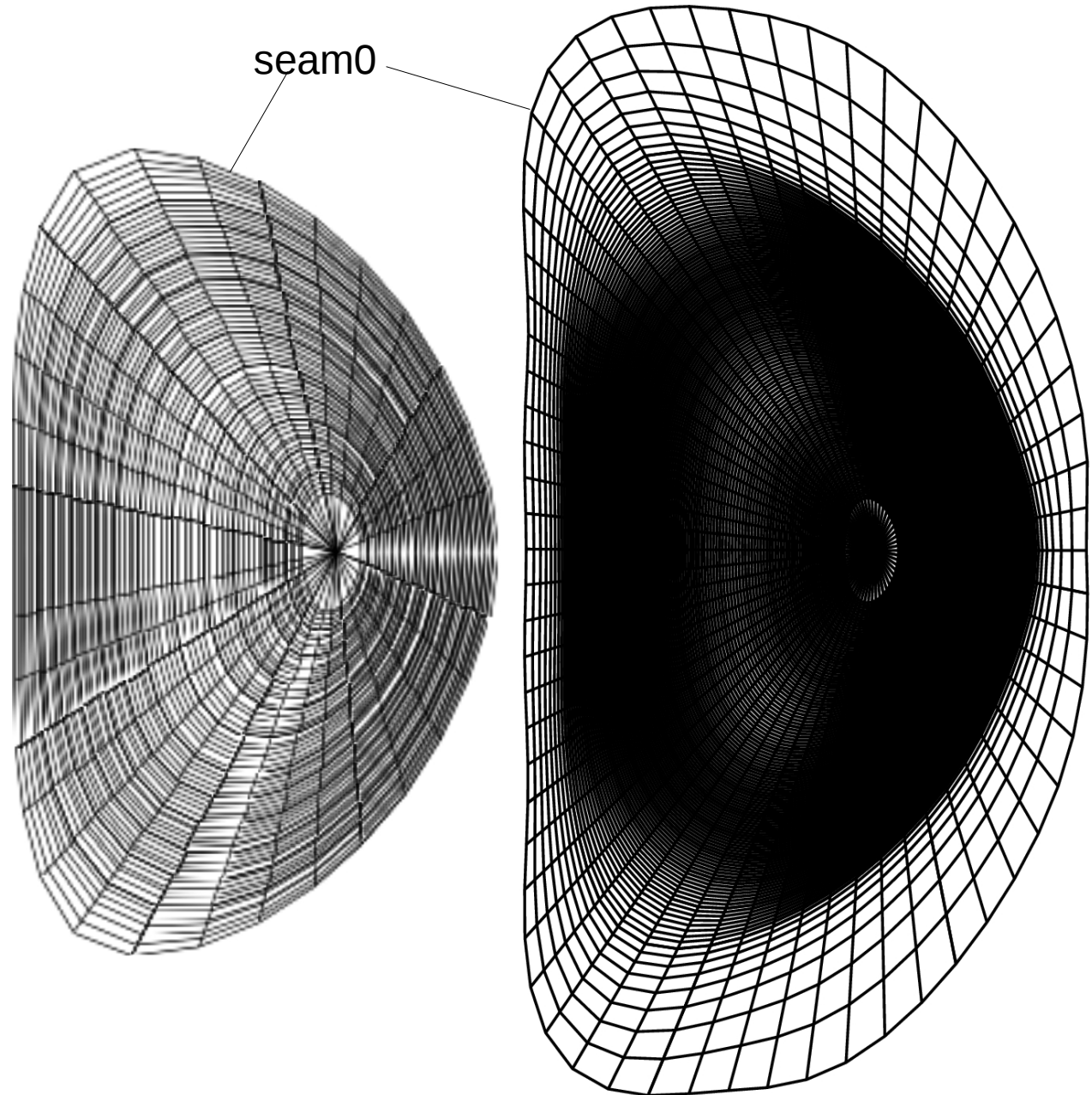
$I_p, B_0 @ R$	1.566	-2.078	1.695
R_0, α, A	1.663	0.647	2.571
$\beta_p, \beta_N, \beta^*$	2.420	2.105	4.428
$\beta_{p,ns}$	1.003	0.675	0.758
$l_{i,ns}$	1.002	0.673	0.756
$\varphi_0, \varphi_1^*, \varphi^*$	2.737	12.079	3.184
κ, δ	1.821	0.739	
$R, Z_{\text{center}}, \Delta R$	1.873	0.004	0.207
$R, Z, \psi_{\text{ext}} (U)$	1.060	1.262	-0.279
$R, Z, \psi_{\text{ext}} (L)$	1.087	-1.229	-0.275
$\Psi_{\text{ext},ns}$	-3.309	-3.797	-3.273
$L_{p,ns} [\mu\text{H}], h_i$	2.733	2.730	1.170
$\Psi_0, \Delta\Psi_p, \Phi$	1.650	-1.918	2.819
$W_{\text{tot},e} [\text{MJ}]$	3.127	4.953	2
alfa, betp(0)	1.509	0.894	999 0
alfa, betp(1)	2.675	1.000	999
betaj, β_{ext}	0.742	0.000	
R, Z_{centroid}	1.675	0.005	
Vol., Surf.	22.573	57.735	

DIII-D Shot #087009: meshes

Fixed and free
boundary
simulations run with
different meshes.

Conducting
boundary
conditions applied
to seam0.

Typically:
mx=128
my=64
nxbl=8, nybl=4
poly_degree=3
procs = 64 to 192



DIII-D Shot #087009 with fixed boundary

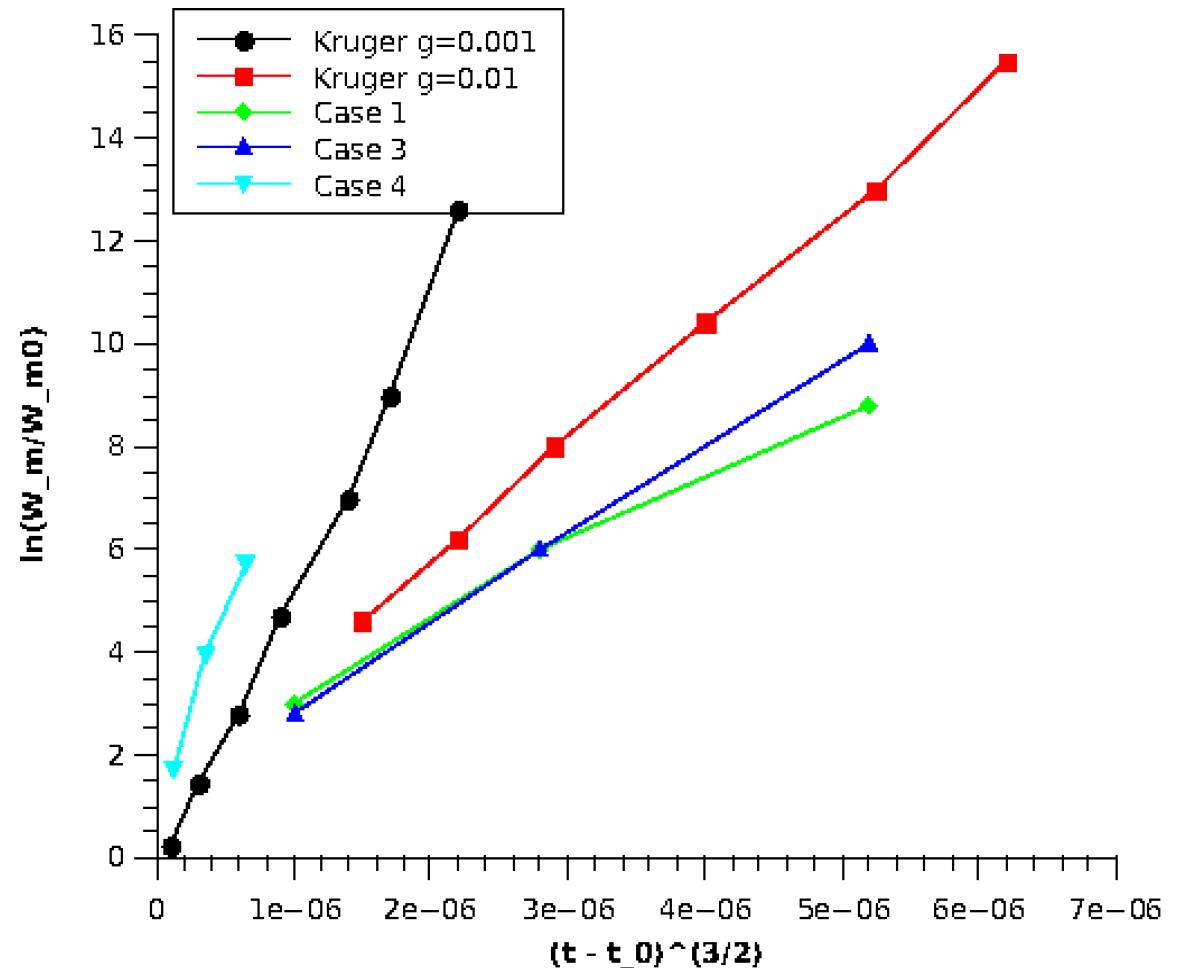
$$\frac{\partial P}{\partial t} = \dots + \gamma_H P_{eq}$$

$$\beta_N = \beta_{NC}(1 + \gamma_H t)$$

Campaign:

- S=1e5, 1e6;
- gamma_heat= 0.1, 0.01, 0.001;
- bamp=1e-1, 1e-5, 1e-20
- l_phi=2 (n=0, 1 modes)
- Continuity and eta n=0
- Anisotropic thermal

Growth rate of n=1 mode measured and compared with scaling of $(t-t_0)^{(3/2)}$.



DIII-D results: Shot #087009 with free boundary

Campaign:

$S=1e5$;

$\gamma_{\text{heat}}= 0.1,$
 $0.01, 0.001$;

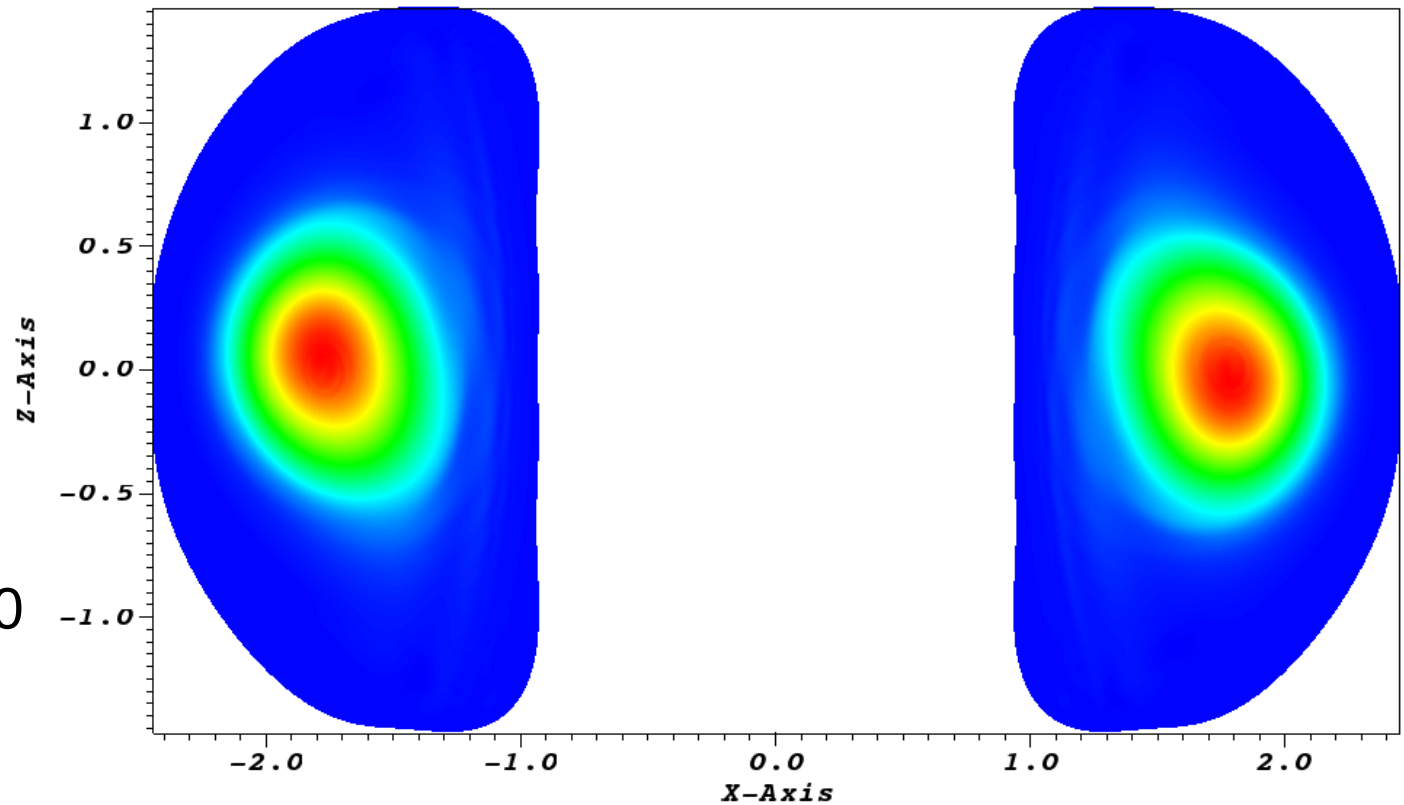
$b_{\text{amp}}=1e-1, 1e-5$

$l_{\text{phi}}=2$ ($n=0, 1$
modes)

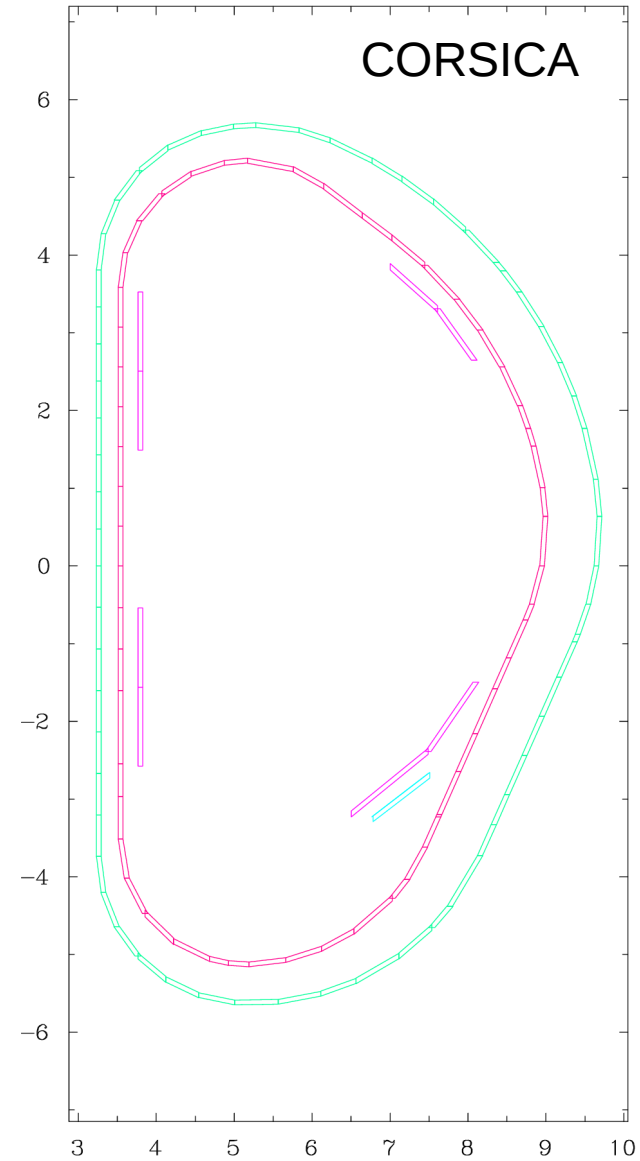
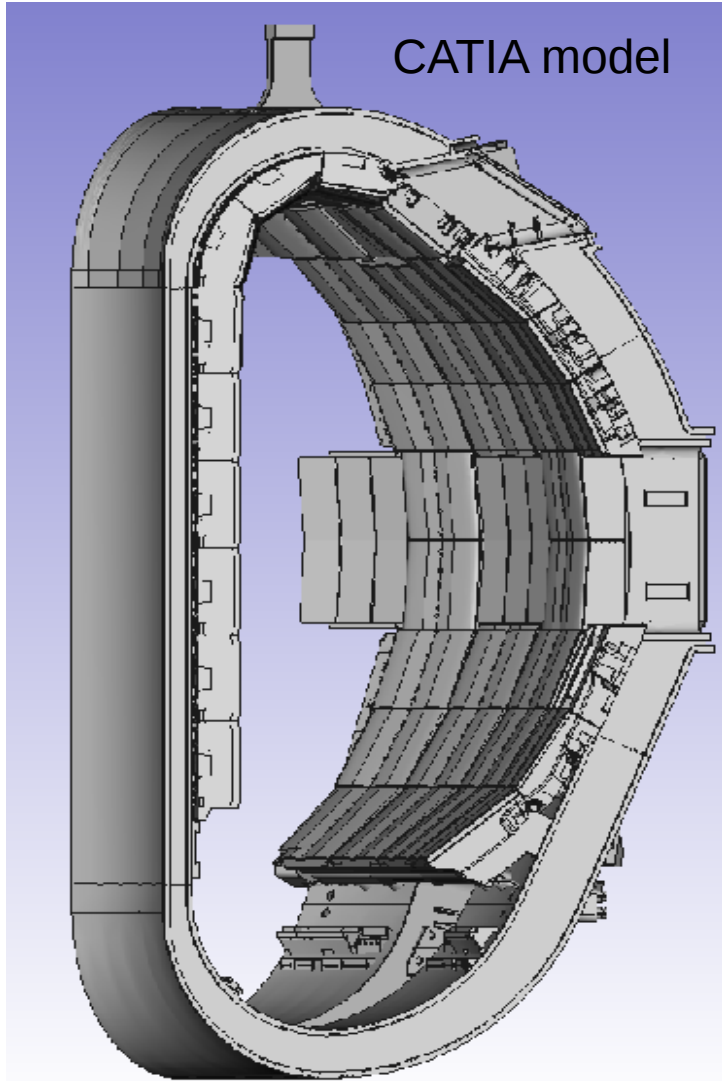
Continuity and eta $n=0$

Anisotropic thermal

Mode grows: $n=1$
distortion in all fields.



ITER Passive Structure

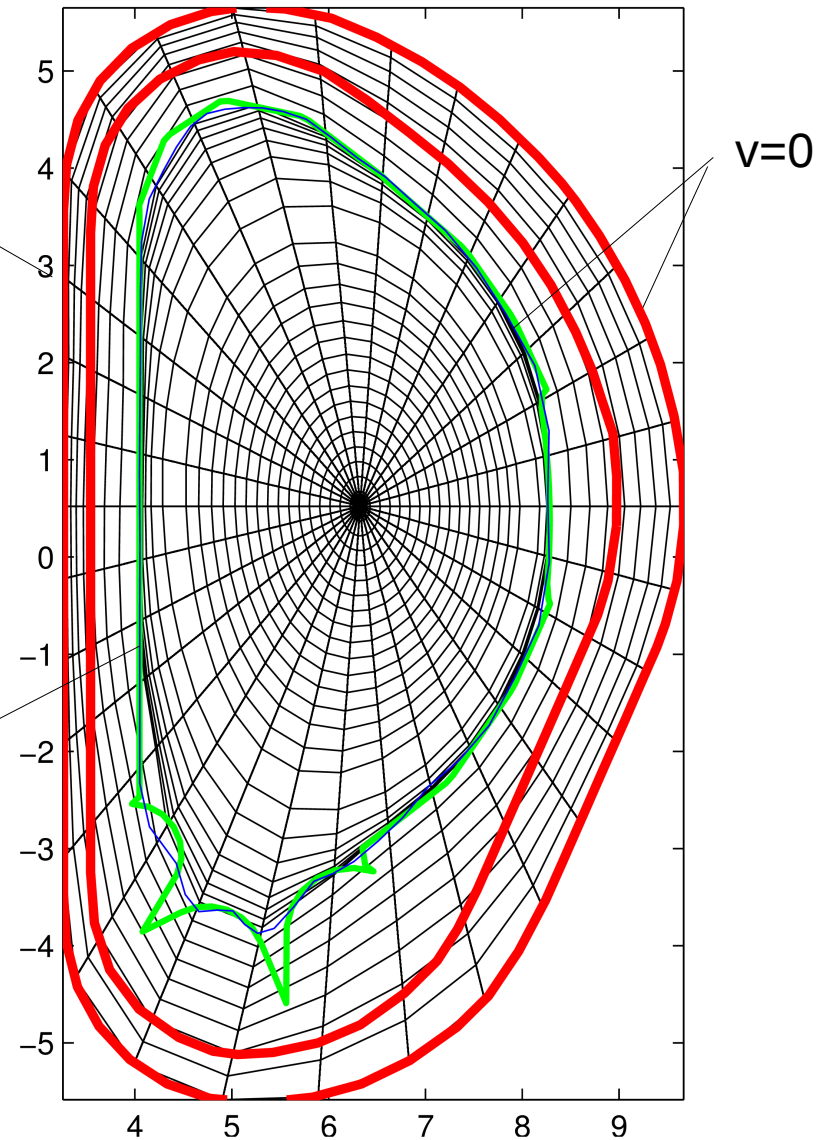
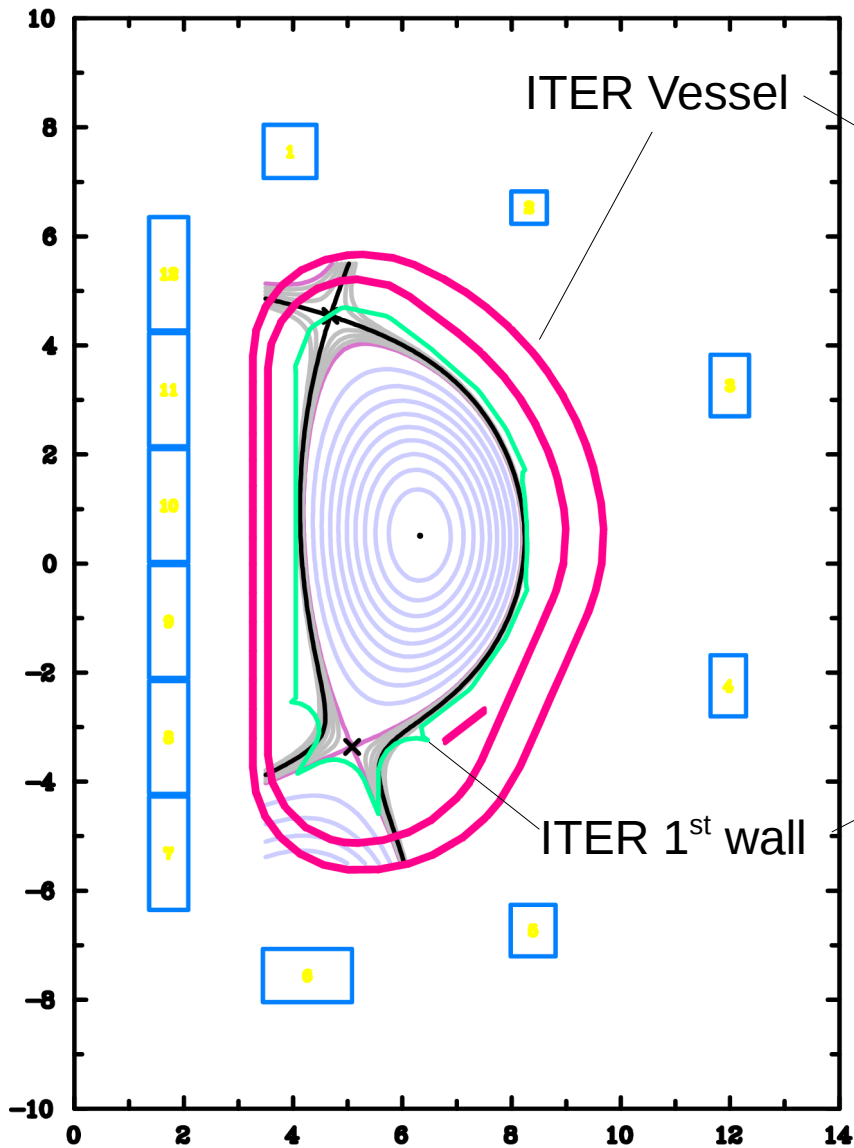


ITER wall meshed

ITER S2 • SOB, $t=150$ s

CORSICA

NIMROD

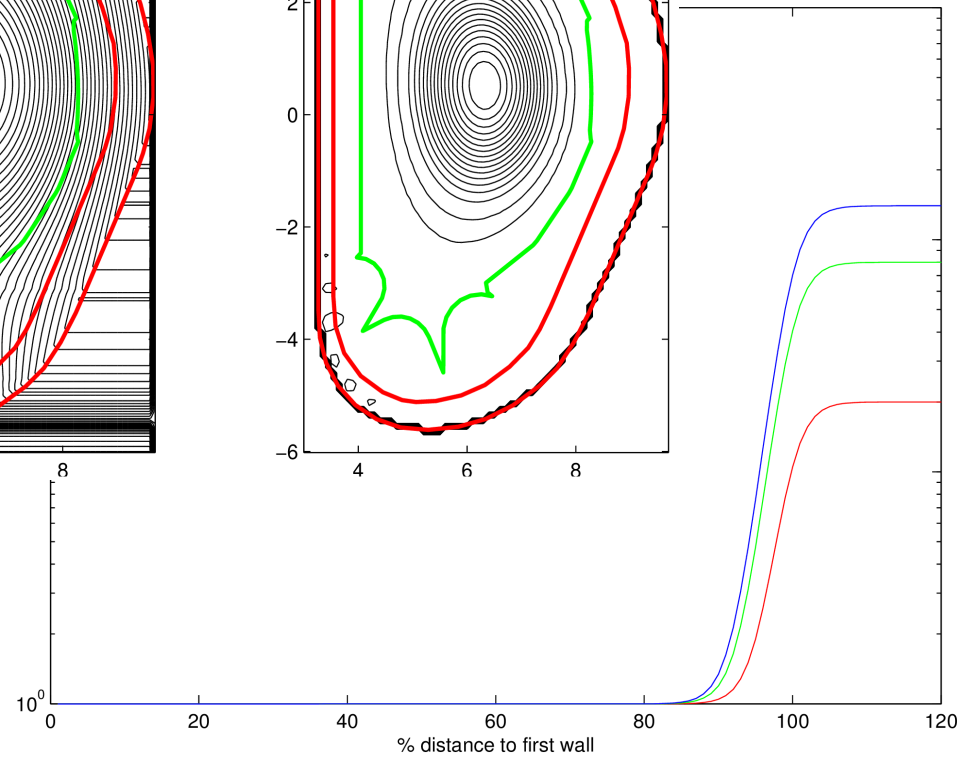
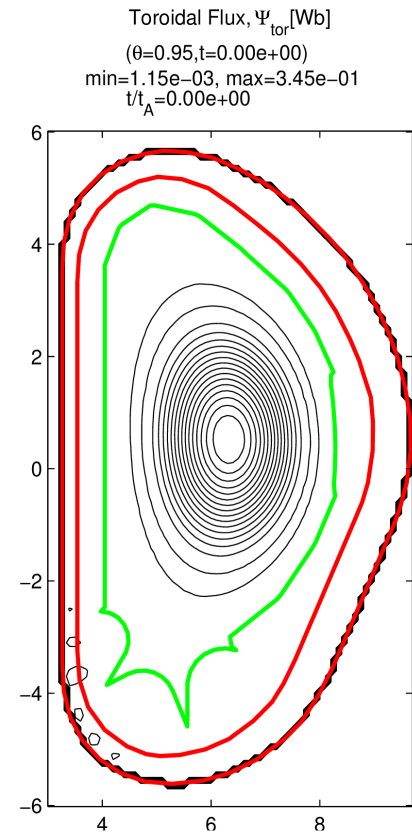
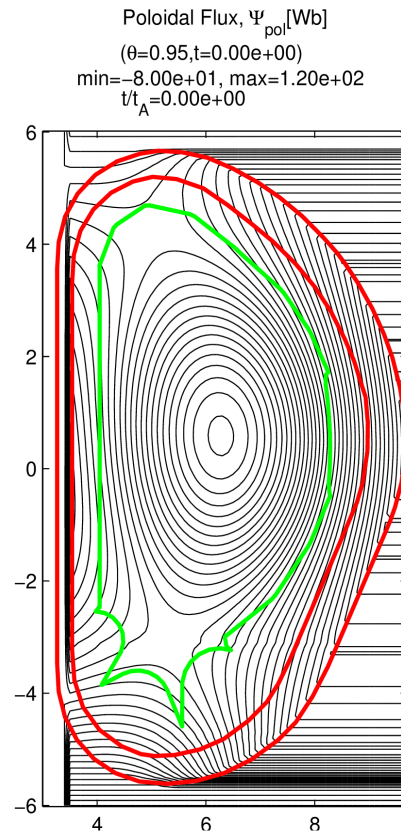


ITER Start of Burn reference case (15MA) (CORSICA: iter_sob.sav)

Campaign 1:
Wall with z_off.

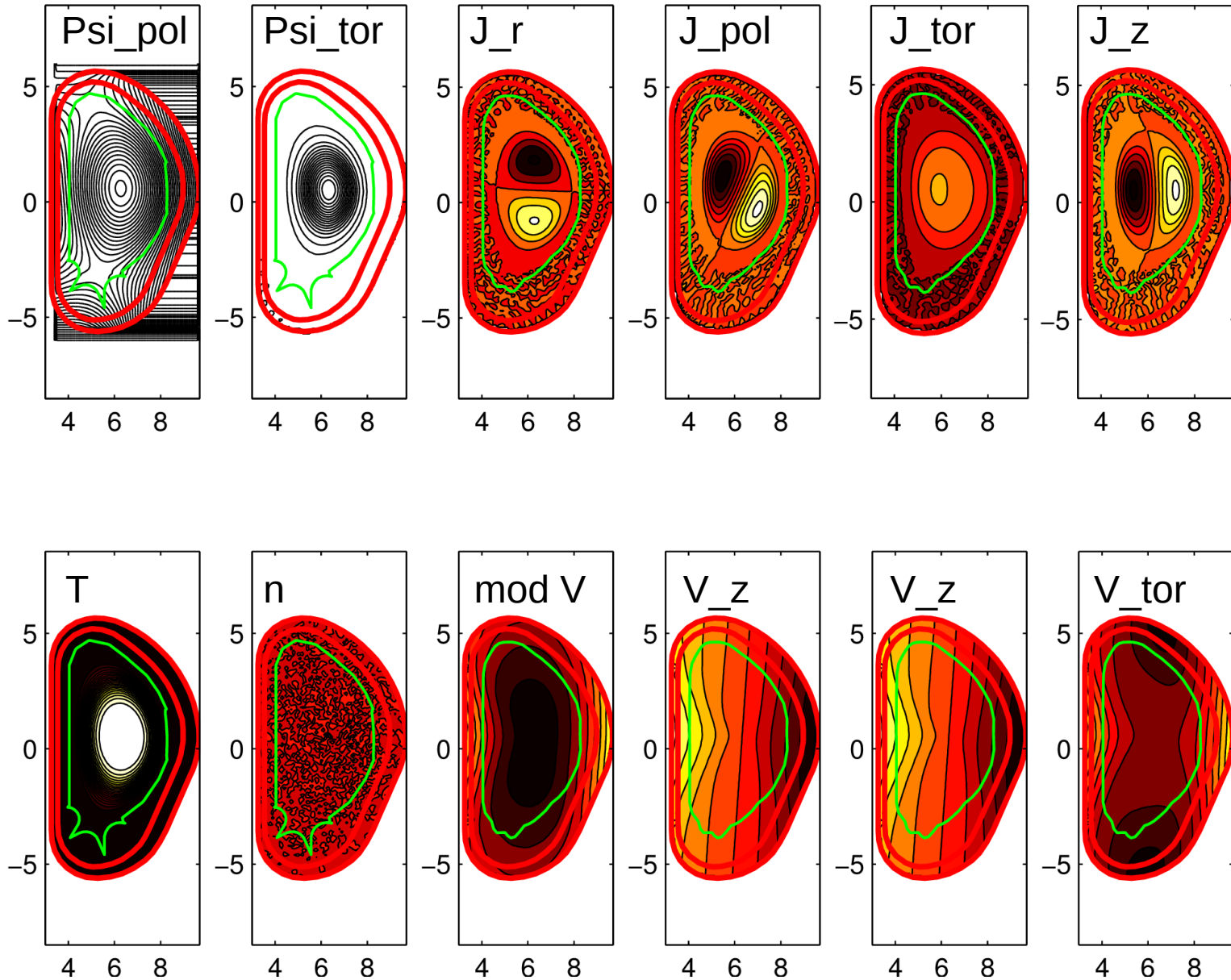
Campaign 2:
CORSICA VST marginally stable IC -> NIMROD heating.

Campaign 3:
dvac= 20, 80, 140;
·bamp=1, 0.2, 0.1;
·S~1e4;
T=5keV;
t/tau_A ~ 1e2
I_phi=2 (n=0, 1 modes)
Continuity n=0 and eta fixed
Anisotropic thermal



ITER CQ following VDE

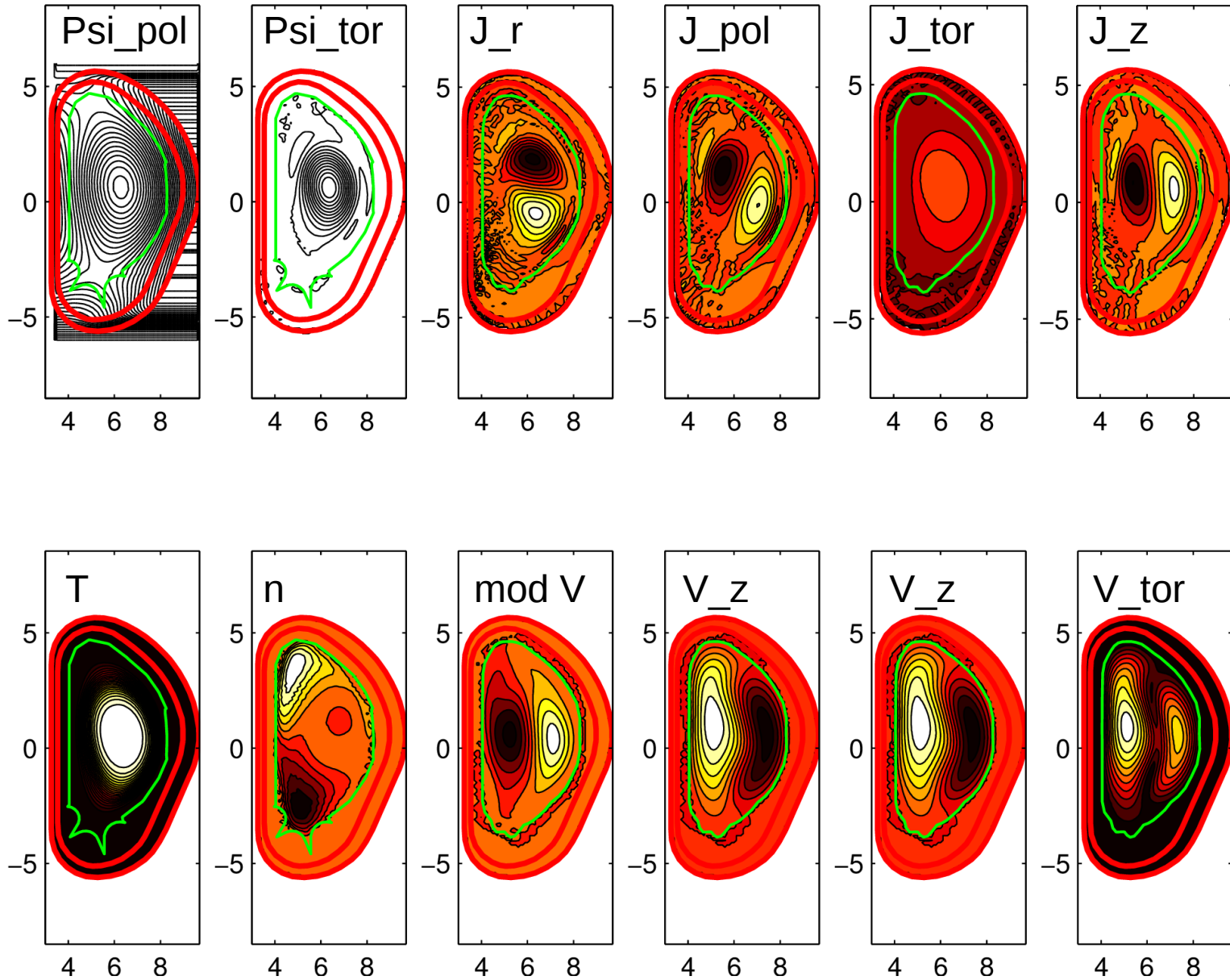
$t/t_A = 0$
 $dvac = 20$
 $bamp = 1$



ITER CQ following VDE

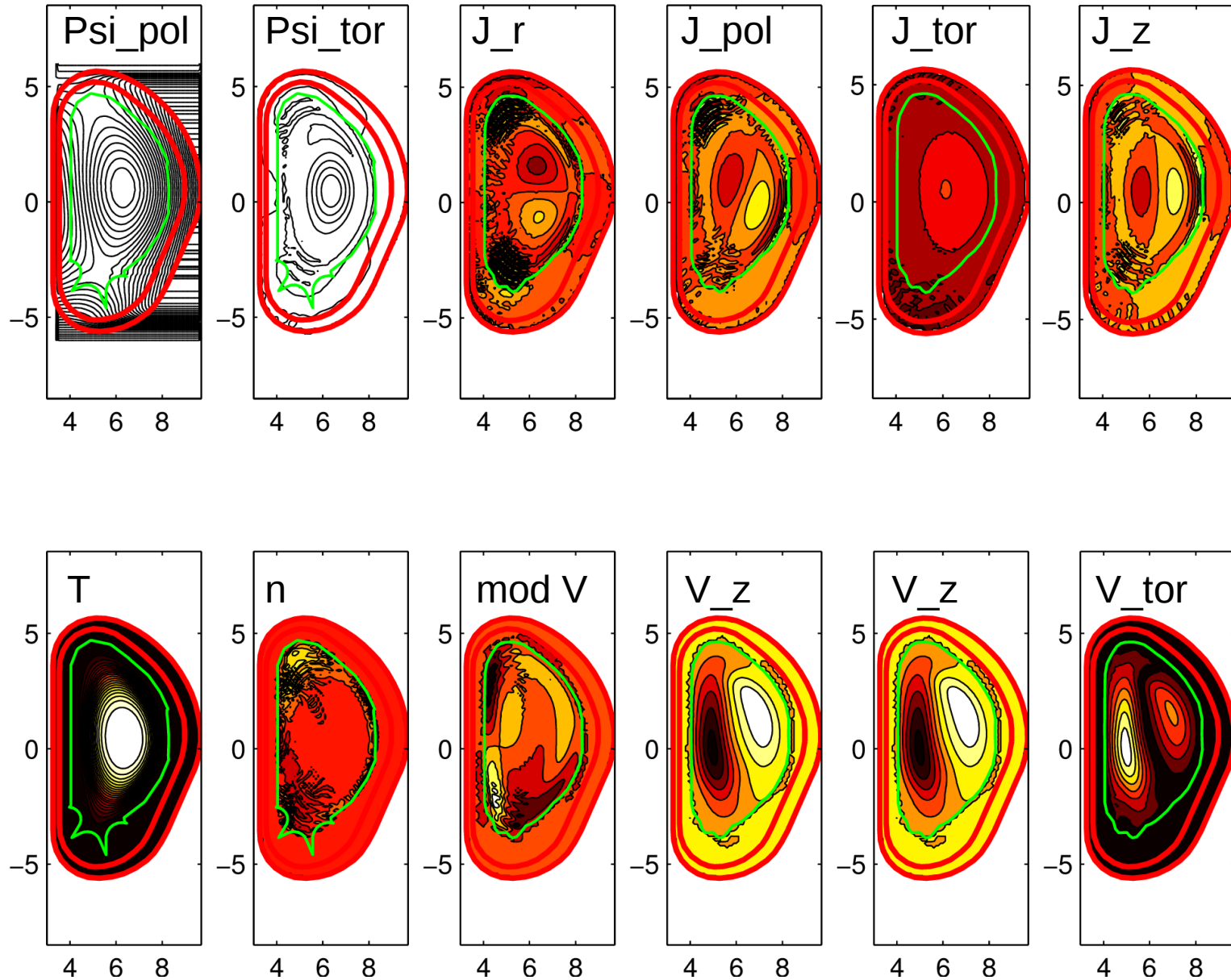
$t/t_A = 26$

dvac=20
bamp=1

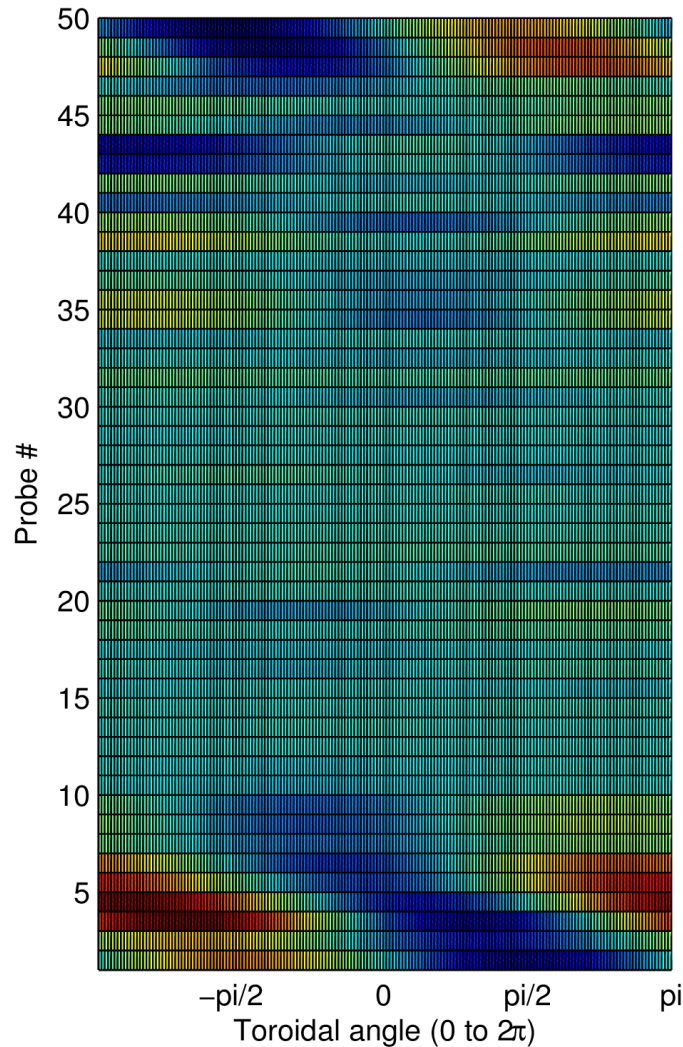


$t/t_A = 247$

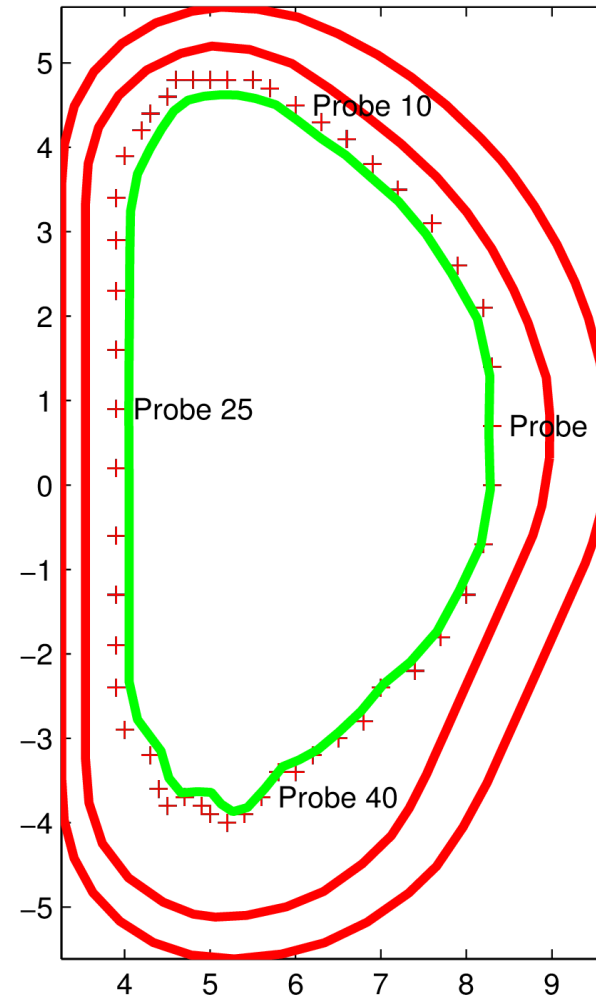
dvac=20
bamp=1

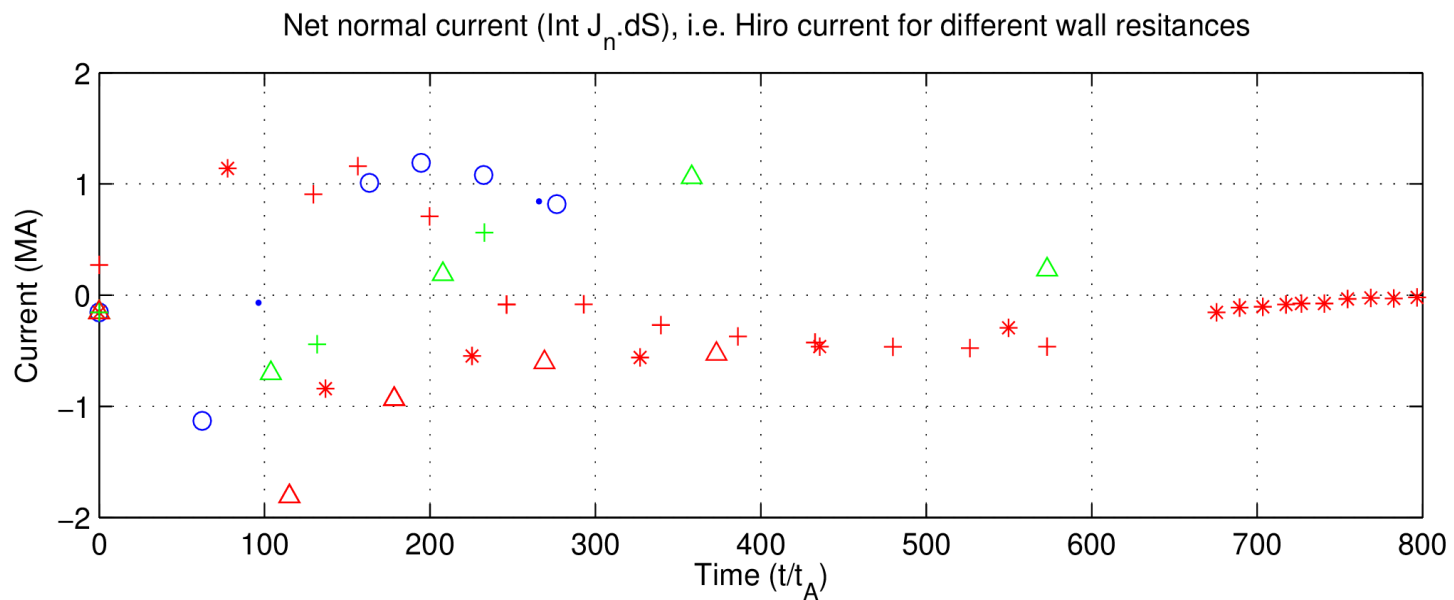
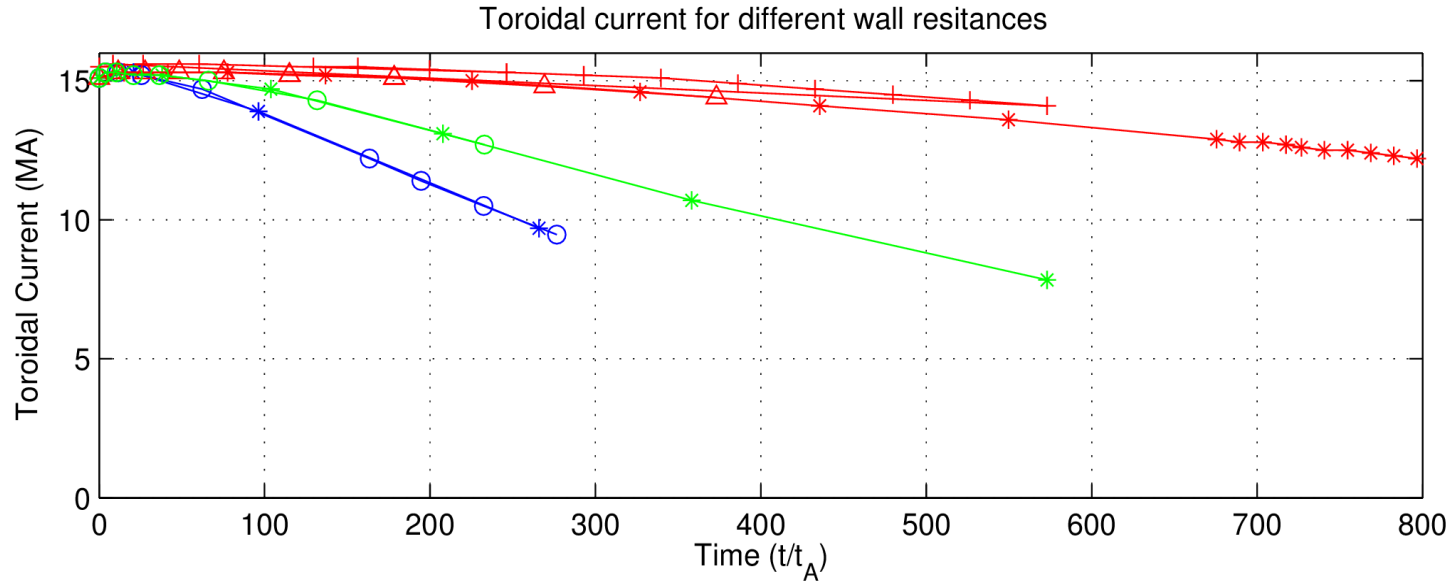


$I_{\text{halo}} = \int_S [J_n] \cdot dS$
 $(\theta=0.95, t=5.72e-06)$
 $\text{min}=-3.33e+04, \text{max}=5.42e+04$
 $t/t_A=2.66e+01$



Current probe positions
 $(\theta=0.95, t=5.72e-06)$
 $t/t_A=2.66e+01$





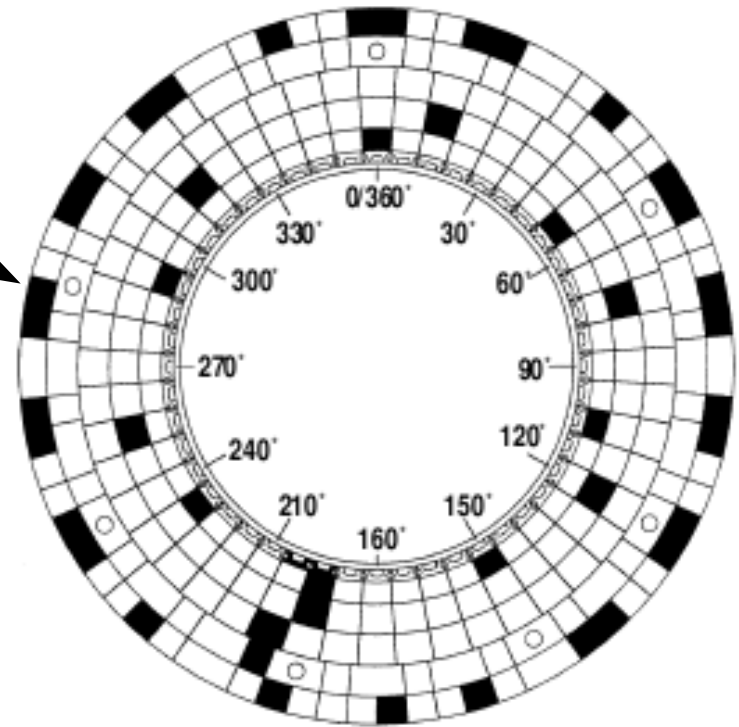
Further work: Validation

Halo current measurement has also been performed (and is ongoing) in many existing tokamak experiments.

Resistive shunts under tiles in **DIII-D** and ASDEX Upgrade, Rogowski coils in **JET**, and a combination of Rogowski and tile measurements in **NSTX**.

Whole problem validation (calibration or validation) would be a logical next step for DIII-D, NSTX or JET.

Unit problem validation also of interest (perhaps for an EPR expt.)



DIIID shunt locations, permission Hollmann

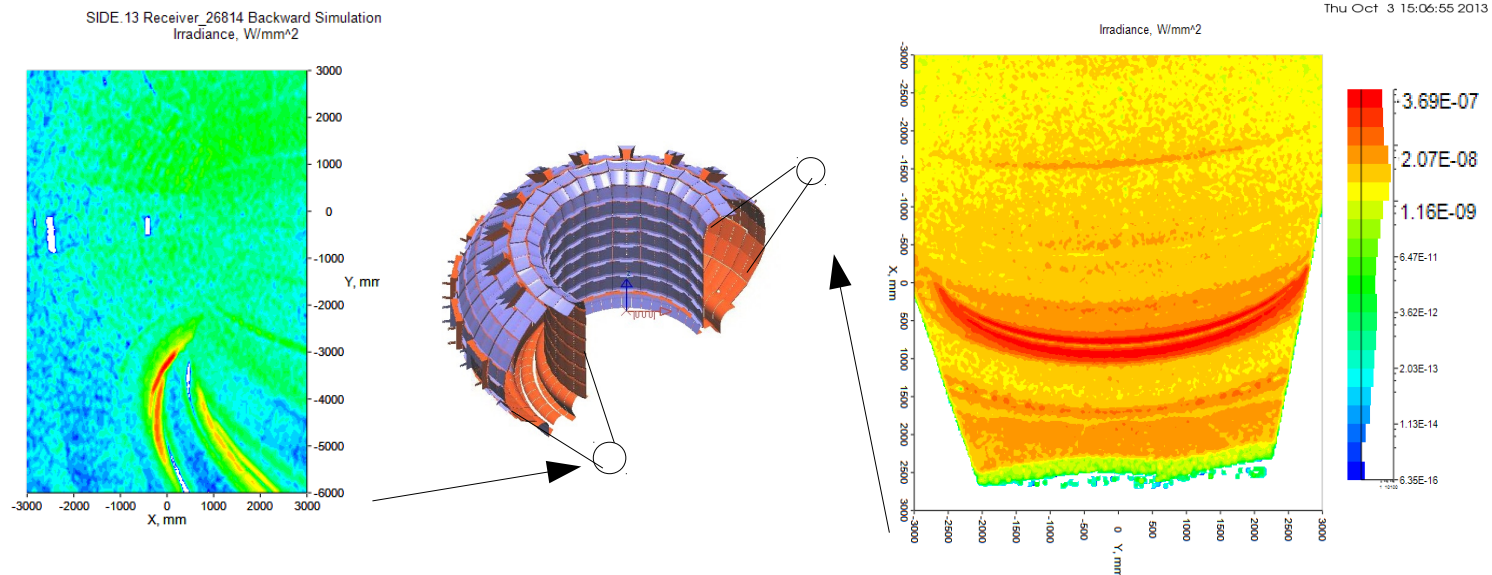
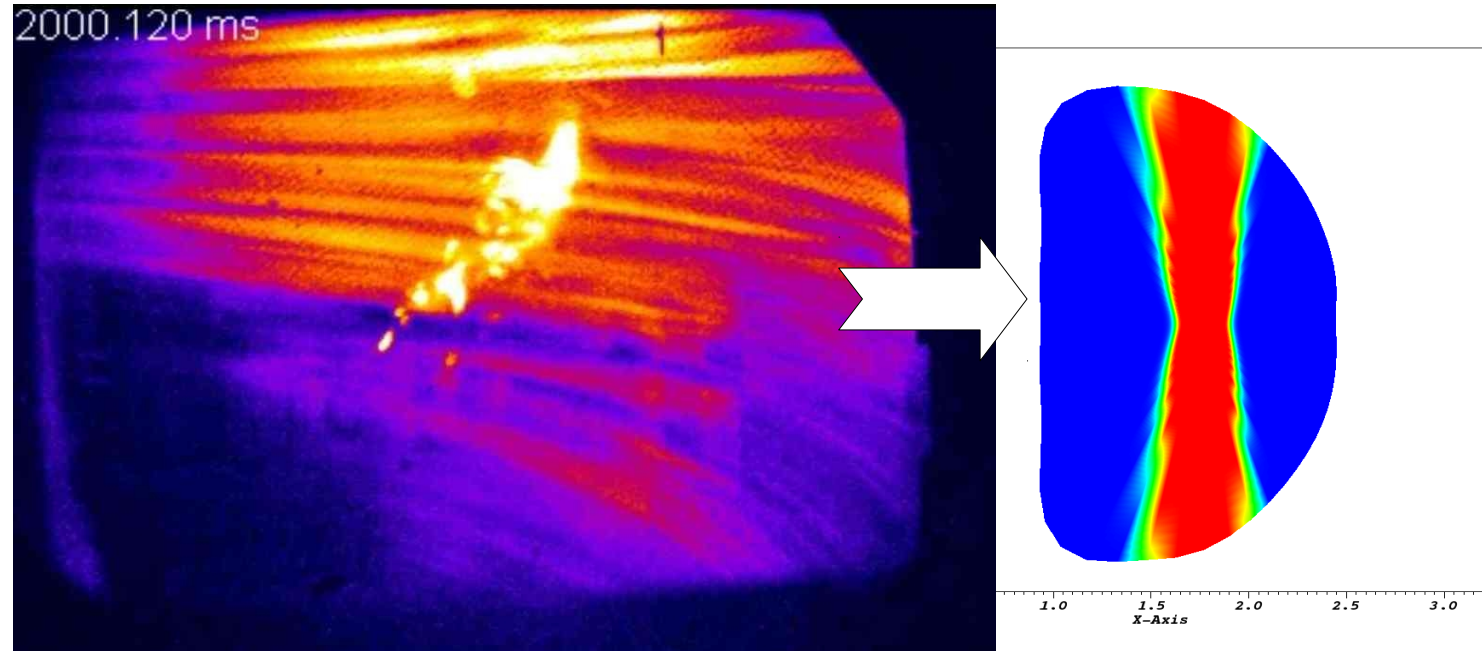
Further work: Shattered pellet simulations

1. *plasma* density azimuthally localized (per Strauss);

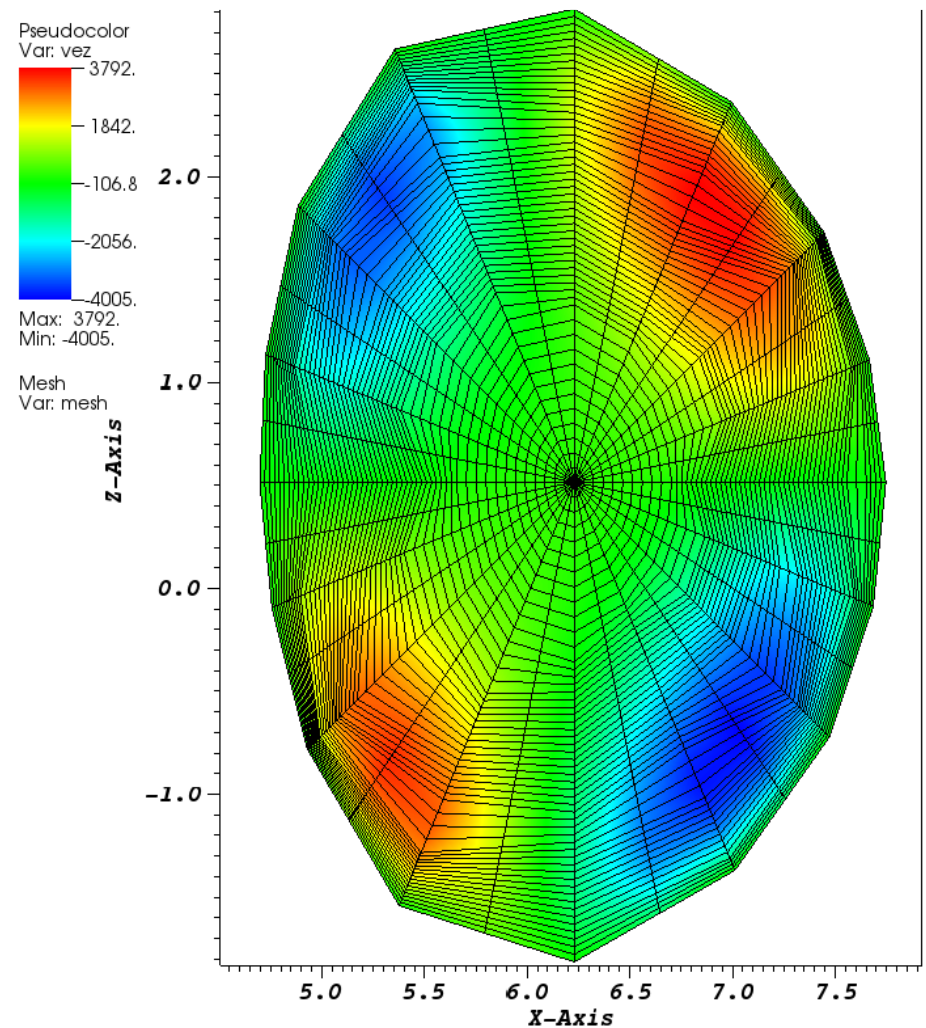
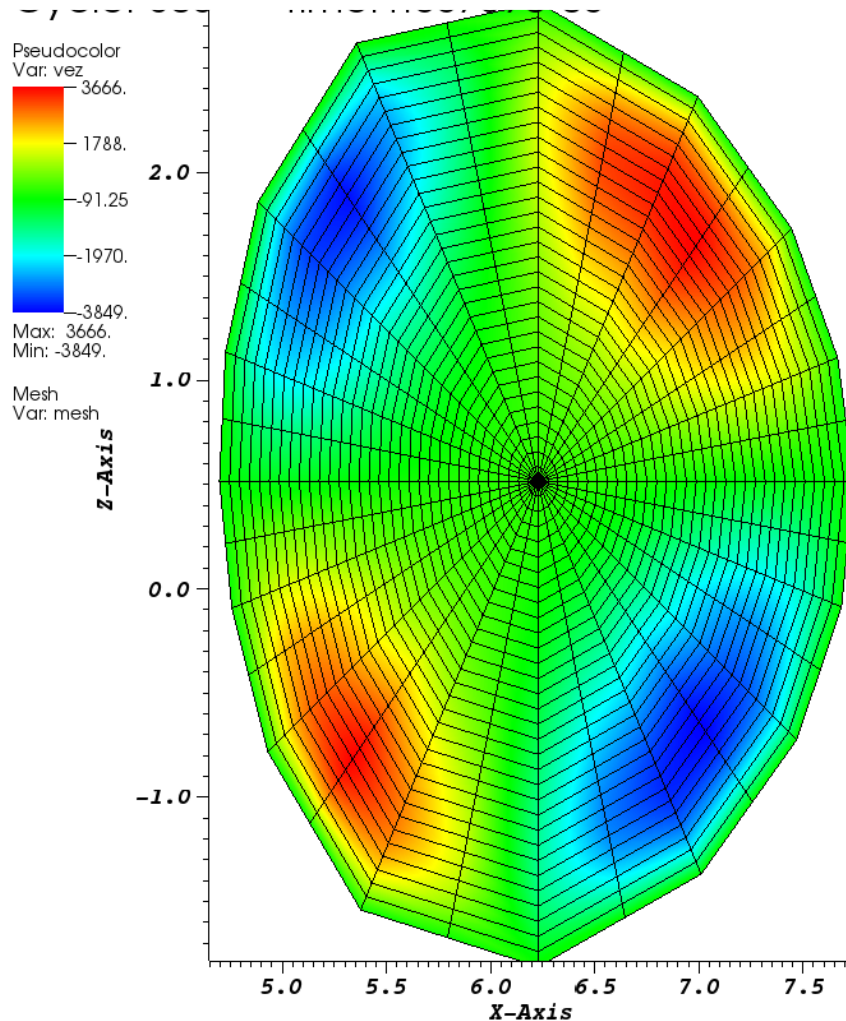
2. consider neutral / radiation model (per Izzo / Shumlak)

Synthetic diagnostics could include LightTools, IR, vis, h-alpha already modeled for ITER.

11/14/13



New mesh adaptation for NIMROD: user-defined parameters (here: gradients in the solution) [12] - [16].



Summary

Two prior simulations of disruptions have been investigated with the CORSICA and NIMROD codes.

We find that the primary results of prior studies are verified:

- pressure-driven mode in DIII-D is reproduced with most recent version of NIMROD (nimdevel)

- vertical displacements and subsequent current quench (and disruptions) are reproduced for ITER using NIMROD with a resistive wall.

Next steps are:

- VALIDATE code capabilities with experiment (DIII-D, NSTX, EPRs);

- SIMULATE the effects of shattered pellets on disruptions;

- continue DEVELOPMENT of new code capabilities (inc. adaptation).

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