
Generation of runaway electrons during the thermal quench

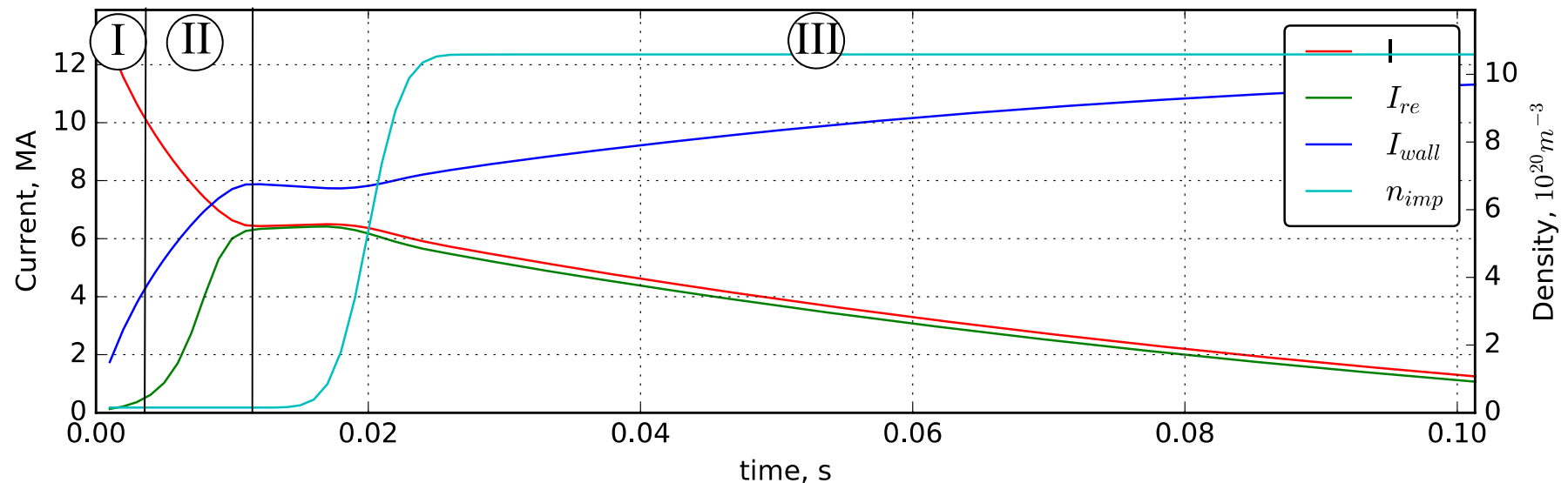
Pavel Aleynikov

Max-Planck-Institut für Plasmaphysik, Greifswald, Germany
and

Boris Breizman

Institute for Fusion Studies, UT Austin, USA

Sequence of “regimes” and models



① Dreicer mechanism [Gurevich 1960; Connor and Hastie 1975]

[Ismailov, Aleynikov, Konovalov, “Dreicer mechanism of runaway electron generation in presence of high-Z impurities”, EPS 2016]

Hot-tail mechanism [Chiu 1998; Helander 2004; Smith 2008]

A revised version of the “hot-tail” ideas brings interesting new results [this presentation]

②

③

Avalanche [Rosenbluth and Putvinski 1997]

“Near-threshold” regime [Aleynikov and Breizman PRL 2015]

The model

Consider, for example, the “killer-pellet” thermal quench (TQ)

1. Maxwellian pre-quench electrons (n_0, T_0) with Spitzer correction (j_0)
2. Pellet delivers cold ions and $n_{cold} > n_0$ after ionization
3. The timescales for collisions are:

$$\nu_{cold-cold} \gg \nu_{hot-cold} \gg \nu_{hot-hot}$$

Neglected

4. Kinetic equation for the hot electrons

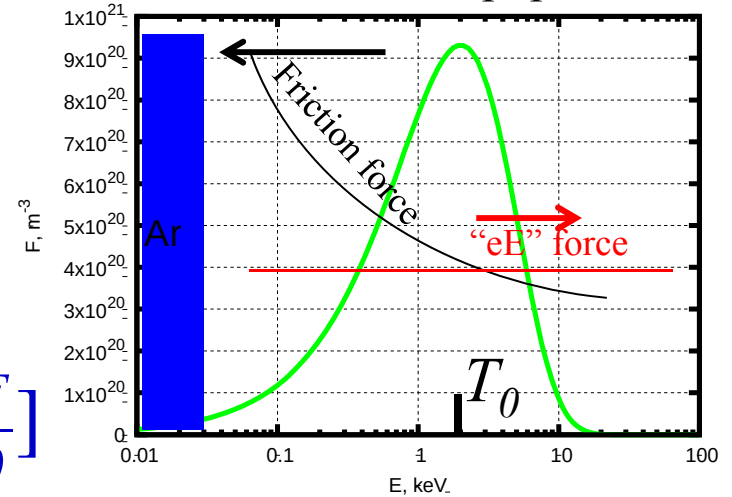
$$\begin{aligned} \frac{\partial F}{\partial t} + \frac{\partial}{\partial p} \left[E \cos \theta - 1 - \frac{1}{p^2} \right] F = \\ = \frac{1}{\sin \theta} \frac{\partial}{\partial \theta} \sin \theta \left[E \frac{\sin \theta}{p} F + \frac{(Z_{eff} + 1)}{2} \frac{\sqrt{p^2 + 1}}{p^3} \frac{\partial F}{\partial \theta} \right] \end{aligned}$$

1. The current density is constant during the TQ. The electric field evolves accordingly.

$$j_0 = \int e v_{\parallel} F(t, E) dp \sin(\theta) d\theta + \sigma_{cold} E(t)$$

1. σ_{cold} is determined by hot population energy release and line-radiation

Initial hot and cold populations



2D evolution of the hot electron distribution

Conservation of the total current prohibits slowing down of the **entire** hot population. The surviving hot electrons form a runaway beam.



Hot electron survival in the limit of $\sigma_{\text{cold}}=0$

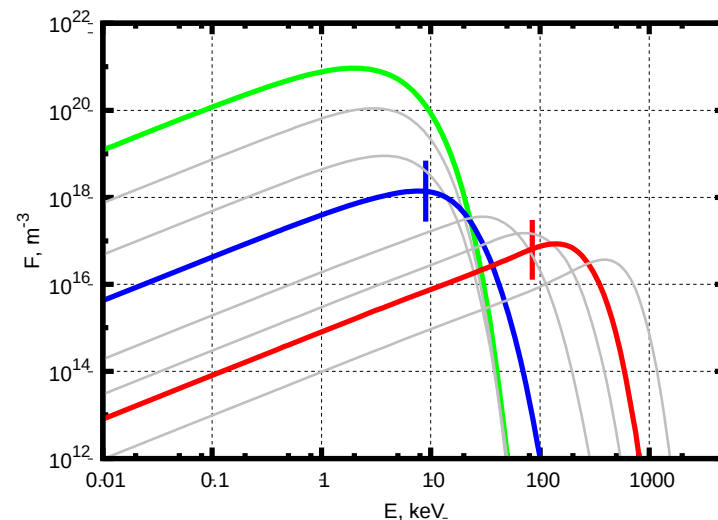
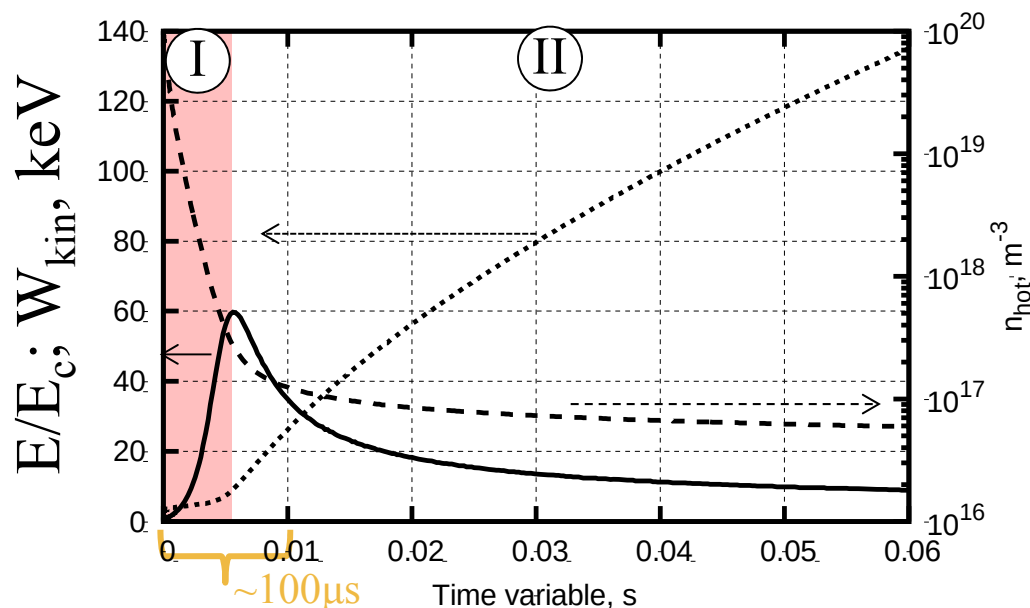
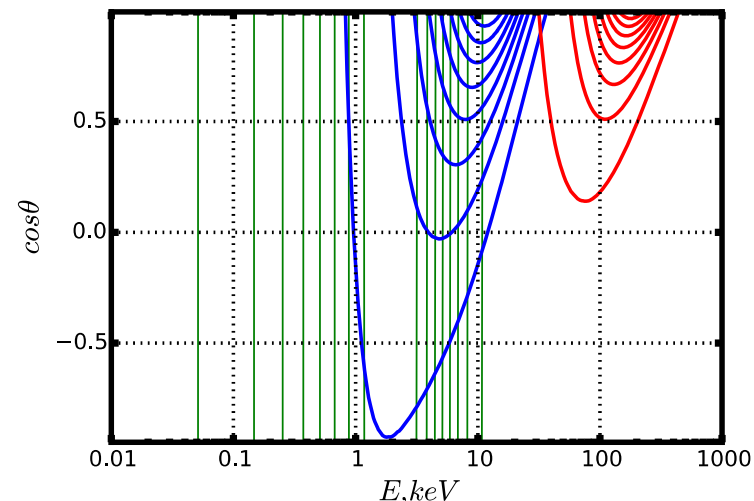
In the limit of $\sigma_{\text{cold}}=0$ (i.e. $T_{\text{cold}}=0$) the total current is carried by the hot population.

Phase I.

- Electric field rises in step with the loss of the hot population.
- The remaining hot electrons form a “beam” when

Phase II.

Electric field decays slowly as the surviving electrons accelerate



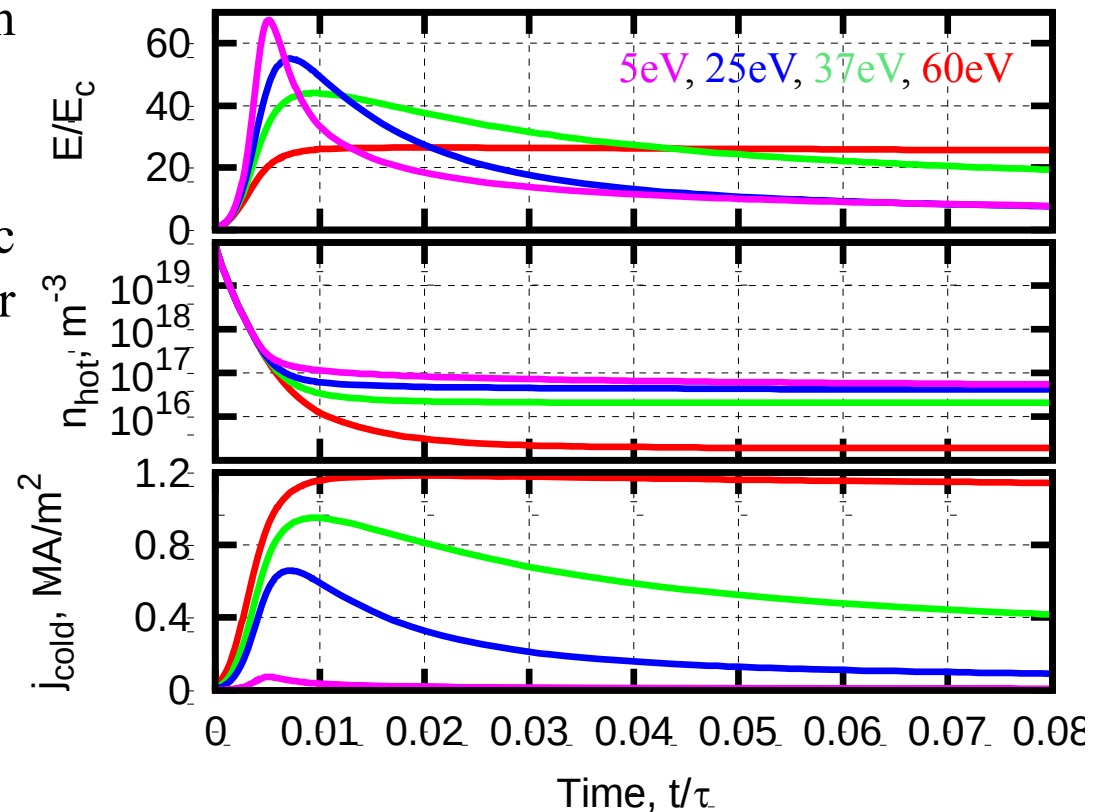
Seed reduction by the bulk conductivity

- If $\sigma_{\text{cold}}=0$, all the post-TQ current is carried by the hot electron beam (no need for the avalanche).
- Finite σ_{cold} reduces the electric field and makes it more difficult for the hot electrons to survive.

Lower temperature



More “surviving electrons”



Cooling down on impurities

- If instantaneous deposition of neutrals is assumed (valid for pellet injection)
- The ordering of collisions and ionization:
 - Initially, only hot electrons ionize impurity neutrals

$$\frac{dn_{cold}}{dt} = n_{hot} n_{imp} \langle v \sigma_i \rangle_{Maxwell}$$

- Thompson ionization cross-section

$$\sigma_i = \frac{\pi e^4}{(4\pi\epsilon_0)^2} \frac{1}{E} \left(\frac{1}{I} - \frac{1}{E} \right)$$

- **If n_{imp} is large** than ionization rate is faster than thermalisation of cold electrons with hot population (Spitzer slowing-down time).

- In particular, in few keV plasma, ionisation rate for first few Argon electrons

$$\frac{1}{n_{hot}} \frac{dn_{cold}}{dt} \approx n_{imp} 10^{-15} m^3 s^{-1}$$

- For $n_{Ar} > 10^{19} m^{-3}$ a separate “cold” Maxwellian population will be formed quicker than in a fraction of a millisecond

$$\nu_{cold-cold} \gg \nu_{hot-cold} \gg \nu_{hot-hot}$$

Self-consistent TQ

- Self-consistent temperature evolution:

$$\frac{\partial(W_{th} + W_{ionization})}{\partial t} = P_{stopping}(F) + \frac{j_{cold}^2}{\sigma_{cold}} - n_{imp} n_{cold} L(T)$$

- 1) Hot electrons heat the “cold” bulk via Coulomb collisions
- 2) The bulk overtakes a fraction of the current
- 3a) Bulk conductivity drops due to radiative losses
- 3b) The hot population decreases in the meantime

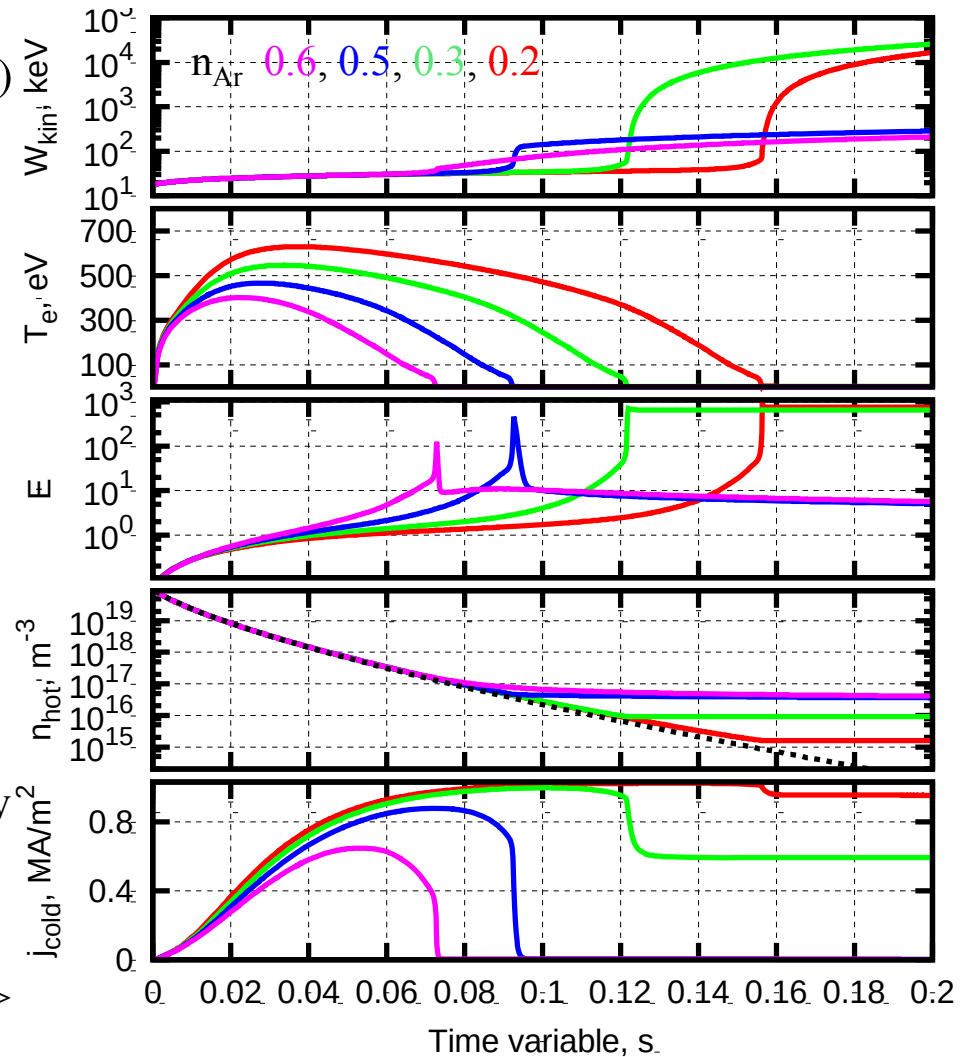
There are two possible outcomes:

1. Prompt conversion regime: purple & blue

Low energy REs carry the total current at low electric field.

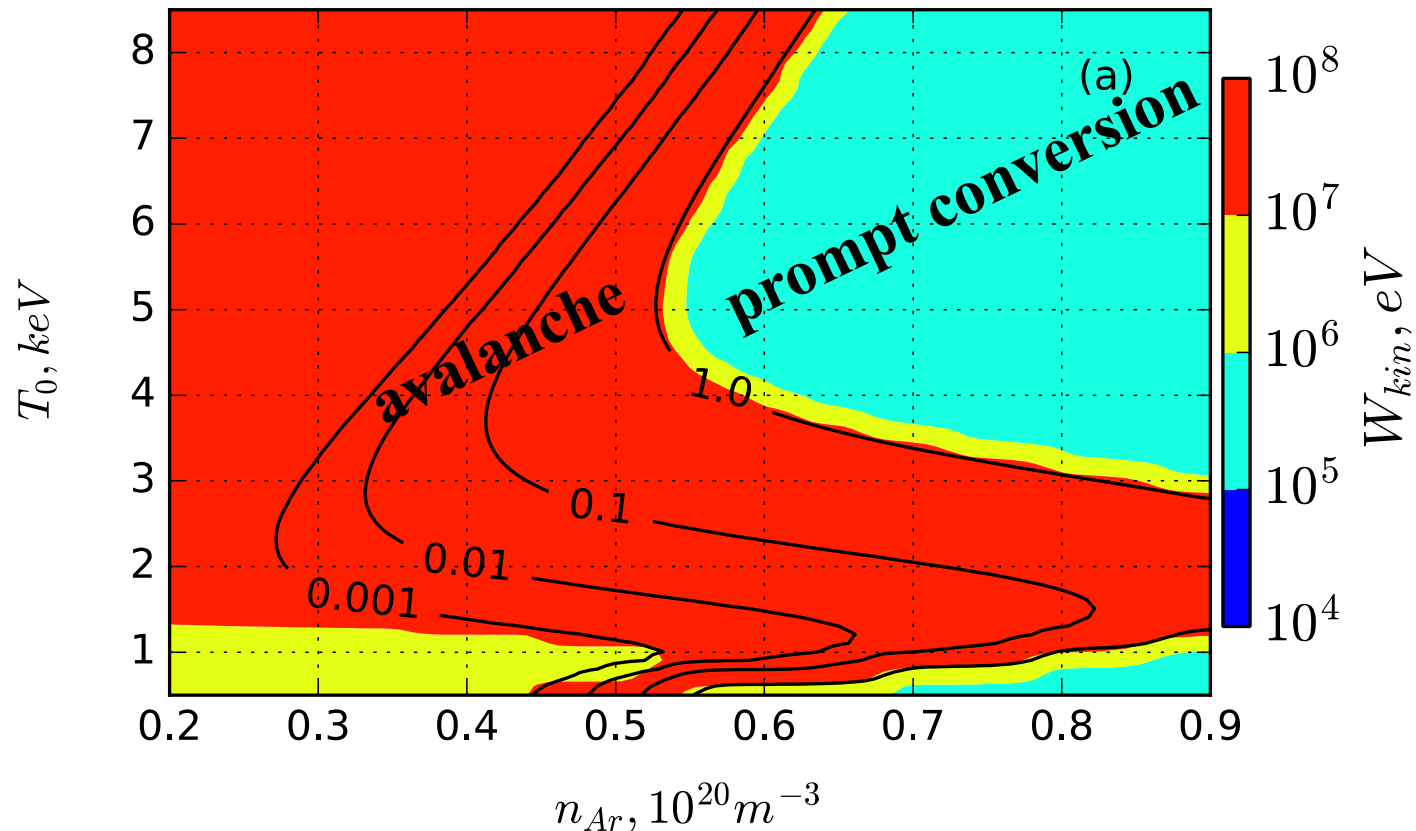
2. Seed for avalanche regime: green & red

Ohmic current requires high electric field -> high energy REs + avalanche.



Scan over initial plasma parameters

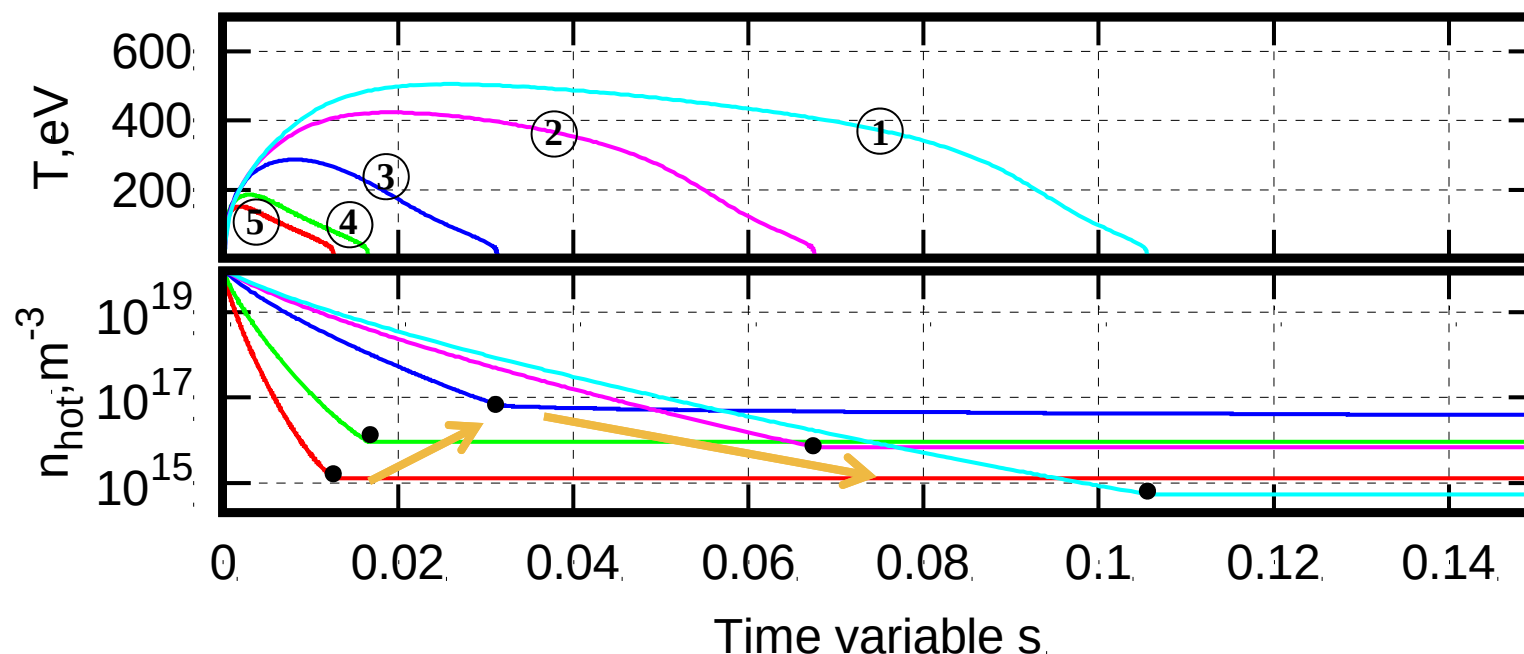
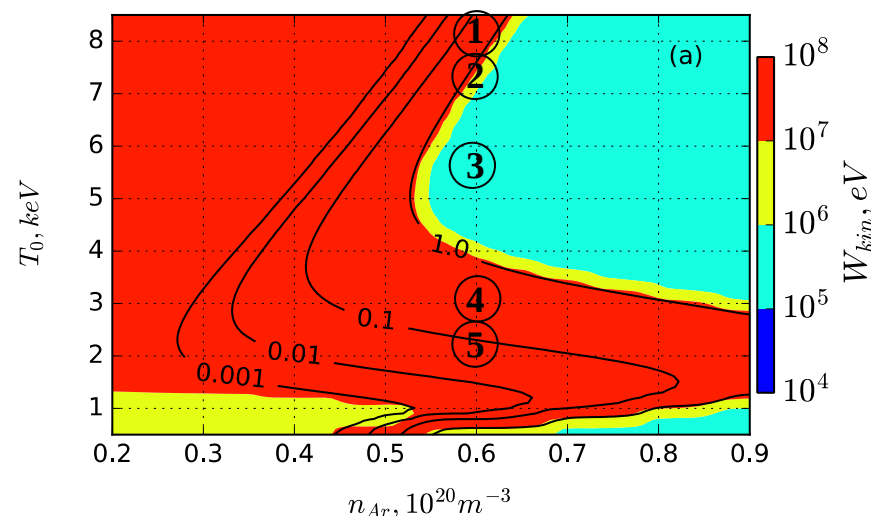
Contour plot of the survived hot electron population density (normalized to j_0/ec)
>1.0 is the **prompt conversion** regime (100% is sub-MeV RE current)



- The electric field is supercritical ($E/E_c \sim 4 \div 8$) in the prompt conversion regime (due to relatively slow transformation of the 100keV RE into 1MeV RE current)
- The seed density has a non-monotonic dependence on pre-quench temperature with a maximum at $T_0 \sim 4 \text{keV}$

Non monotonic behavior of $n_{re}(T_0)$

- Bulk cooling down time is a monotonic function of T_0
- Hot population decay rate is a monotonic function of T_0
- The resulting seed density is not monotonic, with a maximum at $T_0 \sim 4\text{keV}$

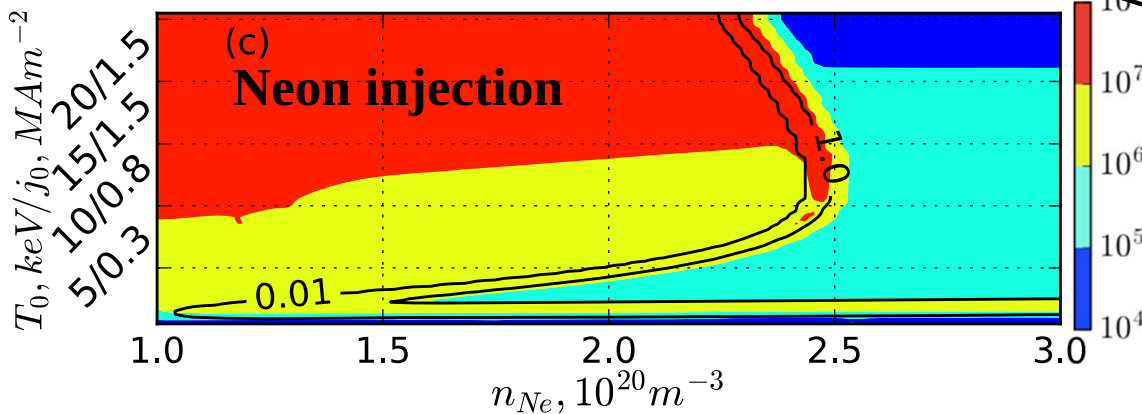
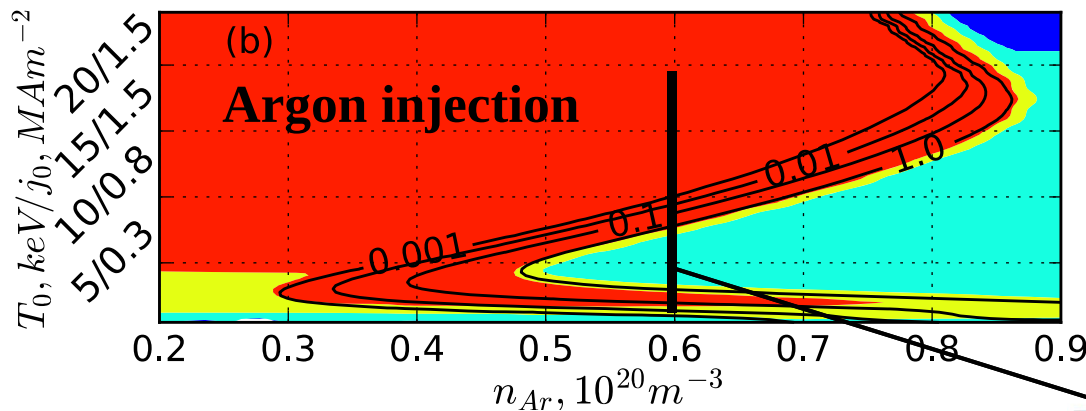


Argon and Neon in ITER

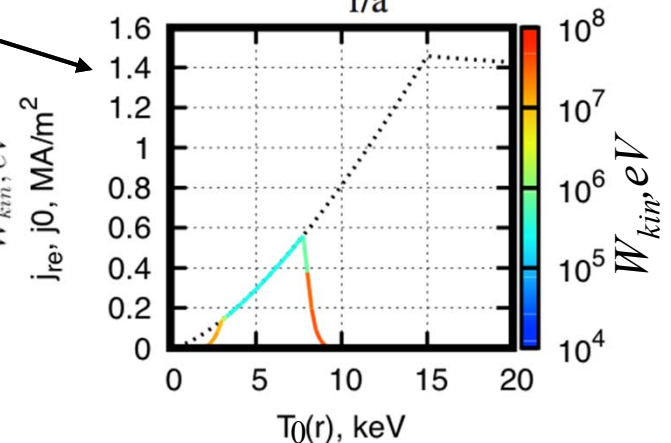
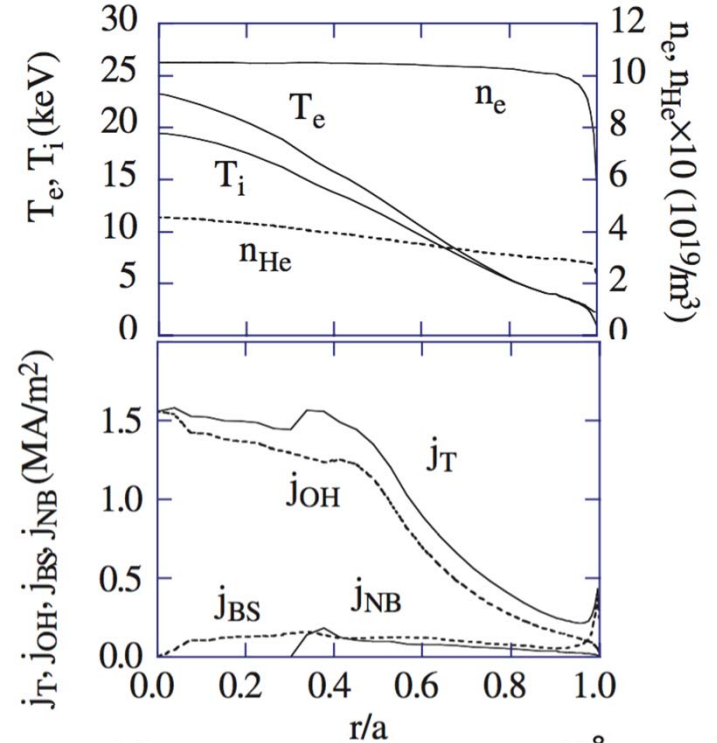
Both T_0 and j_0 determine n_{re} (with n_0 and n_{imp})

For ITER-relevant profiles (Ar injection):

1. Prompt conversion of full current for $n_{Ar} > 10^{20} m^{-3}$
2. RE-free disruption for $n_{Ar} < 3 \times 10^{19} m^{-3}$
3. Non-monotonic radial RE profile



[B.Green, PPCF **45** (2003) 687]

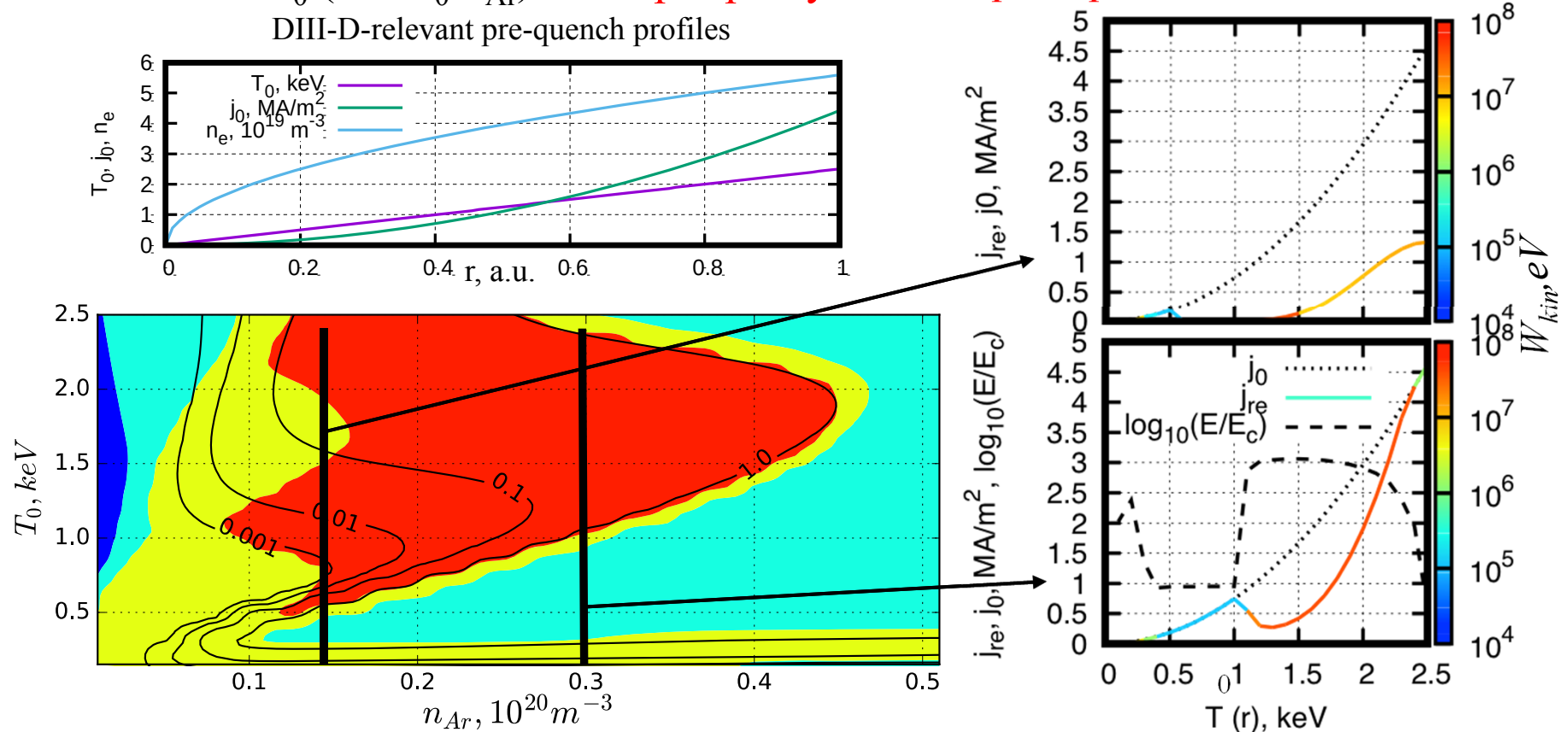


Argon injection in smaller machines

DIII-D is different from ITER:

1. $T_0 < 5$ keV exhibit **peaking** of the RE seed **toward the core**
2. High current density (~ 3 MA/m²) facilitates hot electron survival and favors the Dreicer generation
3. Decrease of n_0 (and n_0/n_{Ar}) at the **periphery** leads to **prompt conversion** in this area

DIII-D-relevant pre-quench profiles



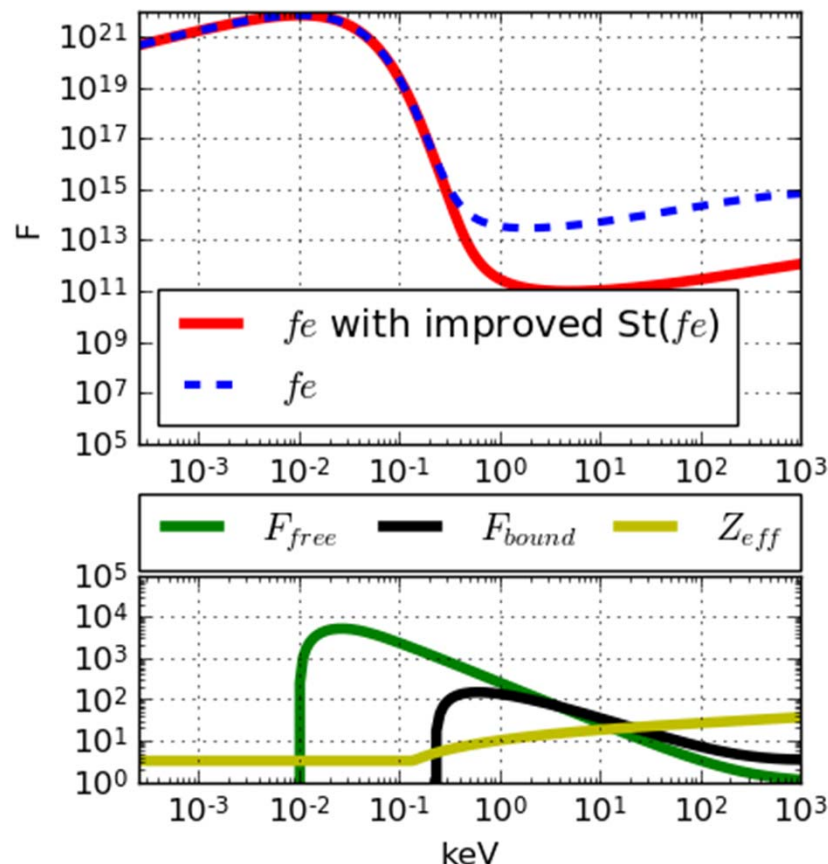
Summary of RE generation model

- **Prompt conversion** of the pre-quench current into the sub-MeV RE current is feasible for abundant impurity injection.
Note: **Prompt conversion** looks **tolerable** for the **plasma position control**. The subsequent slow decay of the RE current should follow the near-threshold regime governed by the impurity amount.
- **RE formation is less efficient at high pre-quench temperatures ($>4\text{keV}$)**, which should produce **significant radial variation** of the runaway seed (in contrast with the present-day $< 4\text{keV}$ experiments, where REs are peaked at the core).
- Non-uniformity of the plasma allows the post-quench current to be carried by **two distinct runaway populations** (a sub-MeV and an ultra-relativistic).
- [P.Aleynikov, B.N.Breizman, Generation of runaway electrons during the thermal quench in tokamaks, Manuscript submitted for publication]
- 1D seed + avalanche calculations are ongoing

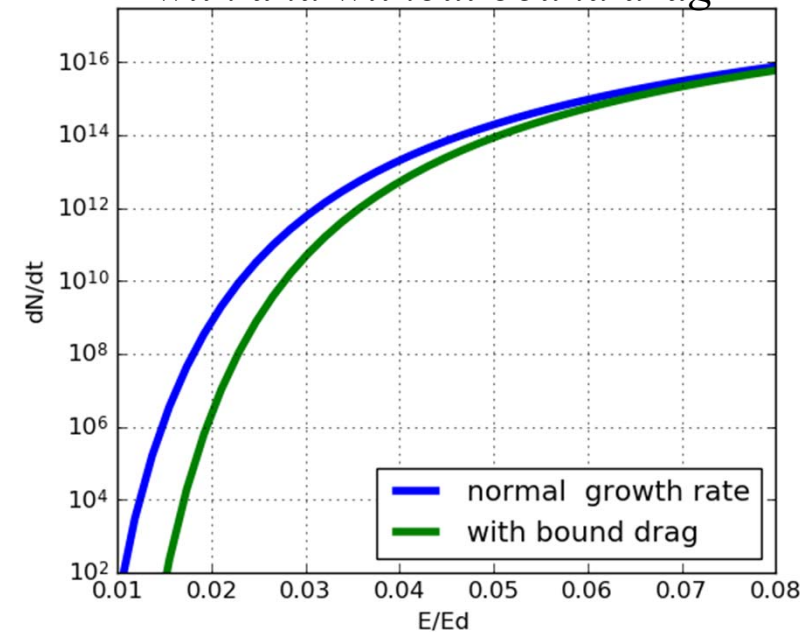
Extra

Dreicer mechanism in presence of high-Z impurities

- As electrons accelerate they start to interact with bound electrons and scatter on shielded high-Z impurities, unlike thermal electrons.
- “Extra” friction reduces the Dreicer flow**
- The effect is less pronounced at high electric field



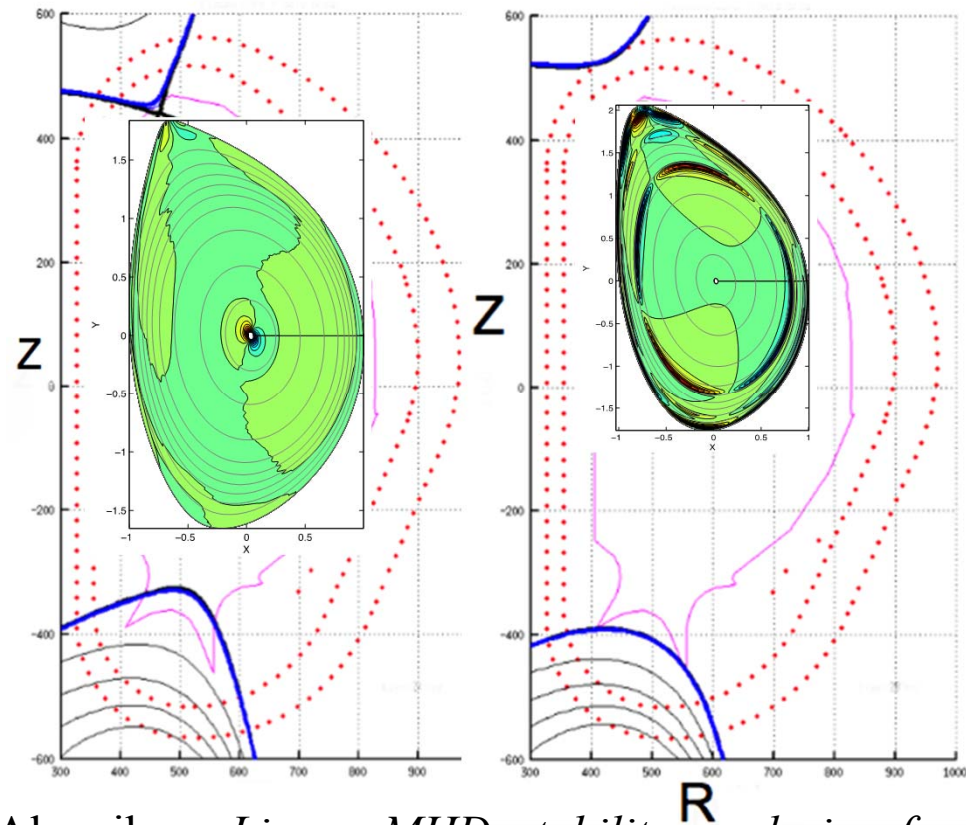
*Dreicer rate dependence on electric field
with and without bound drag*



[Ismailov, Aleynikov, Konovalov, “Dreicer mechanism of runaway electron generation in presence of high-Z impurities”, EPS 2016]

MHD stability of post-disruption plasmas in ITER

- 2D plasma evolution with DINA
- Linear MHD stability analysis of unperturbed equilibrium with CASTOR and MISHKA
- A variety of different modes can appear in post-disruption plasma with RE
- Results are sensitive to the RE seed profile



[K. Aleynikova, G.T.A. Huijsmans, P. Aleynikov, *Linear MHD stability analysis of post-disruption plasmas in ITER*, Plasma Physics Reports **42** (2016)]

DIII-D QRE modeling

- Experimental data is used to calculate the evolution of the distribution function
- The time-dependent kinetic equation is solved numerically

Without the avalanche a clear bump is formed around $p_{\max}$ after the puff



DIII-D QRE modeling

- Experimental data is used to calculate the evolution of the distribution function
- The time-dependent kinetic equation is solved numerically

With avalanche the bump almost disappears

