

Spatial Transport of Runaway Electrons in Axisymmetric Tokamak Plasmas

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Motivation: Spatial Evolution of Runaway Electrons

- The spatial profile of runaway electrons plays an important role in the evolution of a disruption:
 - Can shape the q-profile and thus influence MHD stability
 - Sets the inductance of the plasma → affects current decay rate
- Present reduced models of the evolution of a runaway electron population assume electrons to be tightly localized to magnetic flux surfaces [[Smith et al. 2006](#), [Konovalov et al. 2014](#), [Martin-Solis et al. 2017](#)]:
 - Spatial transport neglected or treated in an ad-hoc manner
 - In the presence of a 3D magnetic field transport is known to strongly impact the lifetime (energy) of a runaway electron population [[Papp et al. 2011](#)]
- This work seeks to identify under what circumstances non-negligible levels of runaway transport is present in the presence of good magnetic flux surfaces

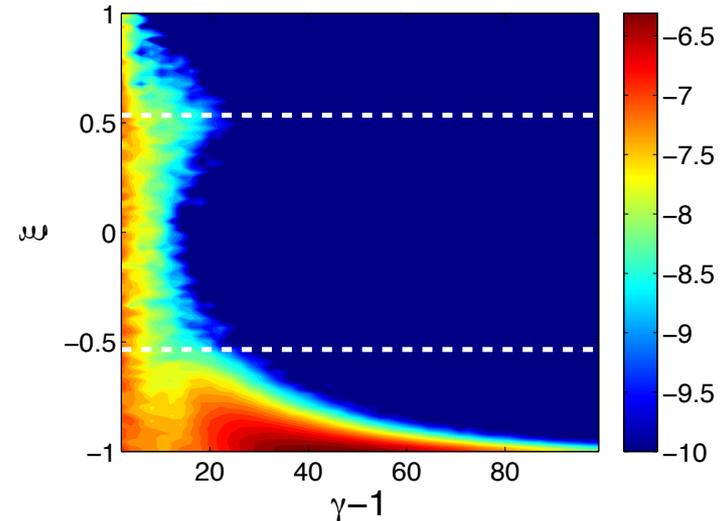
Outline

- Impact of Toroidicity on avalanche growth rate/threshold
- Spatial transport of runaway electrons in an axisymmetric plasma
 - Drastic enhancement in the presence of partially ionized impurities
 - Ware pinch \leftrightarrow inward collapse of runaway electron population
- Implications for phase space distribution of runaway electrons
 - Runaway spatial eigenmode

Description of Runaway Electrons

- Runaway electrons described by drift kinetic equation
- Allows 5D phase space to be evolved
 - Incorporates toroidal effects
 - Spatial transport
- Small-angle collisions treated by Monte Carlo collision operator [Boozer 1981]
 - Partial screening included [Hesslow et al. 2017]
- Synchrotron radiation damping incorporated
- Large-angle collisions (avalanche) described by Möller source
- Flux-surface averaged inductive electric field evolved via:
$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}, \quad \nabla \times \mathbf{B} = \mu_0 \mathbf{j}, \quad E_{\parallel} = \eta (j_p - j_{RA})$$
- Constant loop voltage ($V_{loop} = 2\pi R E_{\varphi} = \text{const}$) assumed in this work

McDevitt et al. 2018



Avalanche Growth Rate in a Tokamak

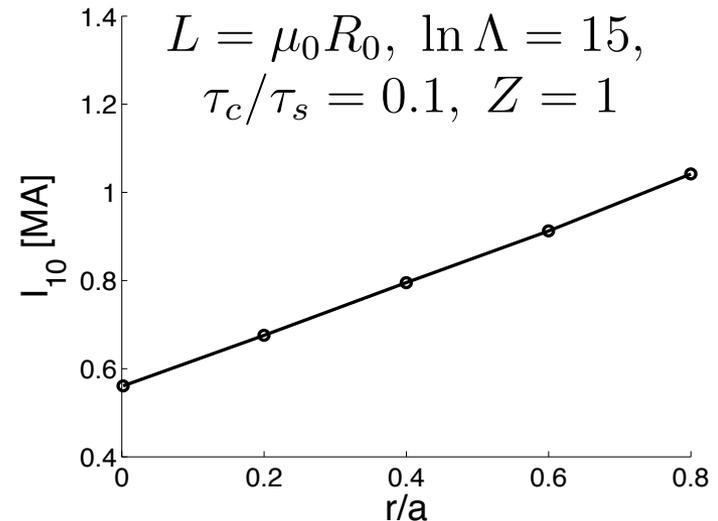
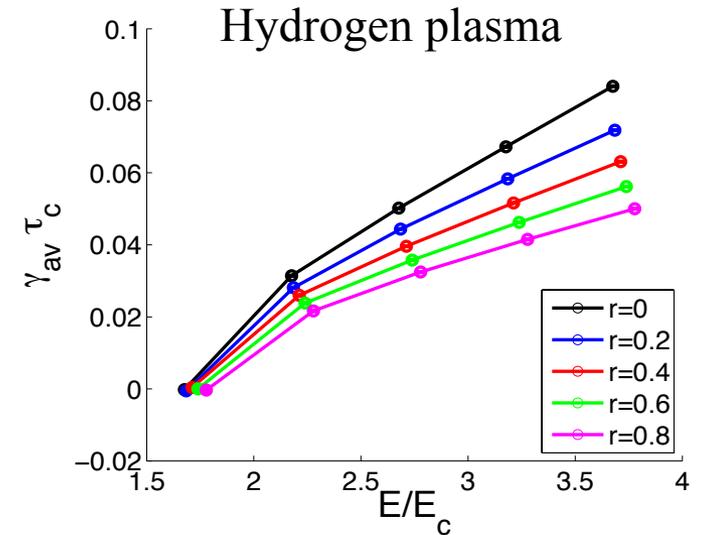
- Avalanche mechanism sensitive to toroidal geometry [Rosenbluth 1997, Chiu et al. 1998, Eriksson et al. 2003, Nilsson et al. 2015,...]
 - Secondary electrons often born in trapped region \Leftrightarrow cannot be directly accelerated
- Also useful to consider the number of exponentiations possible for a given change of plasma current [Rosenbluth 1997, Boozer 2018].

- Well above marginality:

$$\gamma_{av} \Delta t \approx \gamma_0 \frac{E}{E_c} \Delta t \sim -\frac{\gamma_0 \Delta t}{E_c} \frac{L}{2\pi R_0} \frac{\Delta I_p}{\Delta t} \sim \frac{\Delta I_p}{I_{exp}},$$

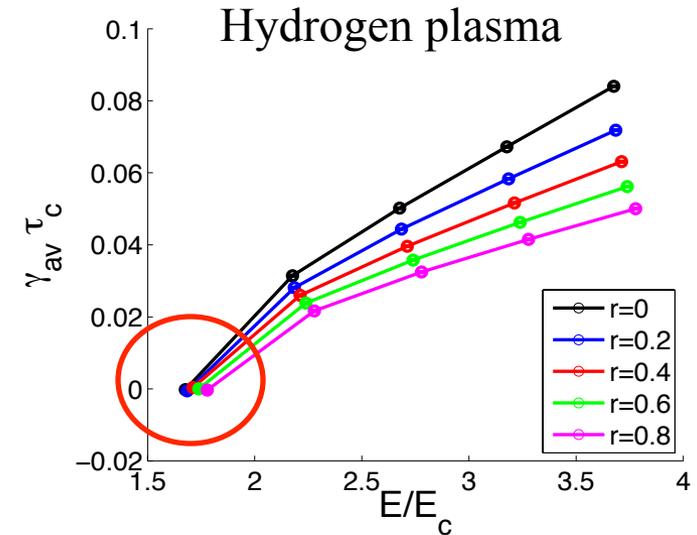
$$I_{exp} = \frac{2\pi R_0}{L} \frac{E_c}{\gamma_0}, \quad I_{10} = \ln 10 I_{exp}$$

- Number of potential exponentiations scales linearly with plasma radius
 - The spatial profile of runaway electrons strongly impacts the efficiency of conversion of thermal current via the avalanche mechanism

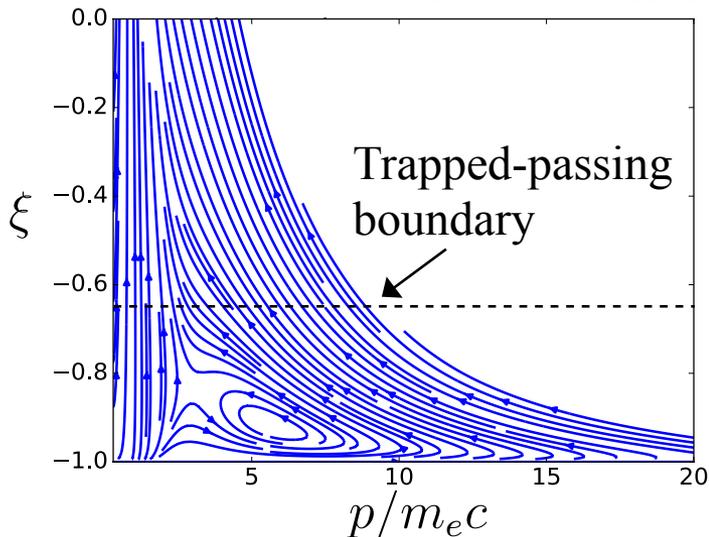


Impact of Toroidicity on Avalanche Threshold

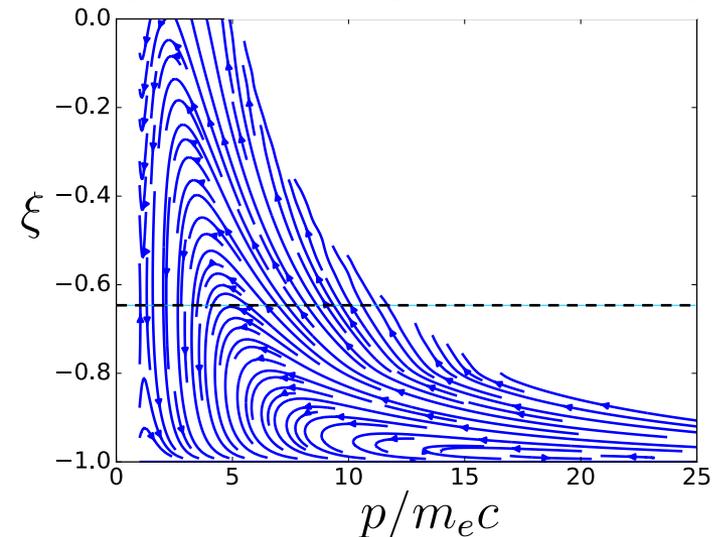
- Avalanche threshold only weakly impacted by toroidicity
- Well above threshold, runaway vortex strongly affected by trapped-passing boundary
 - Near threshold O and X points far from the trapped-passing boundary \Leftrightarrow toroidicity only weakly affects avalanche threshold
 - Above threshold, runaway vortex occupies a larger region of phase space \Leftrightarrow avalanche growth rate strongly impacted



Momentum Flux Slab: Near Threshold

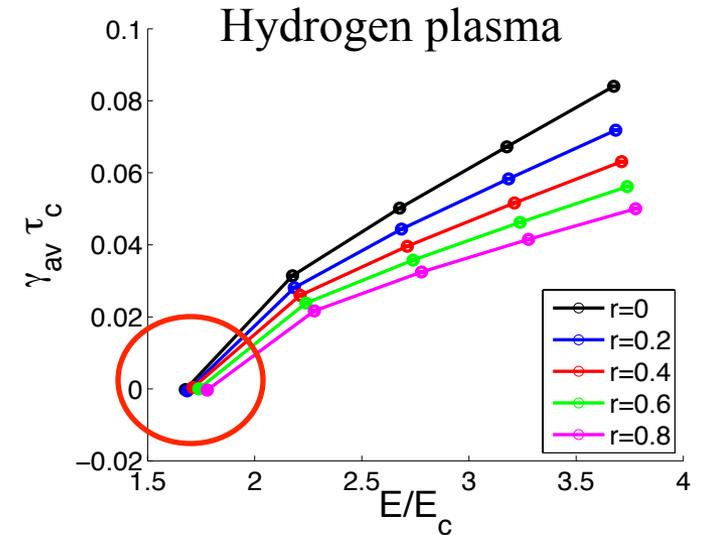


Momentum Flux Slab: Above Threshold

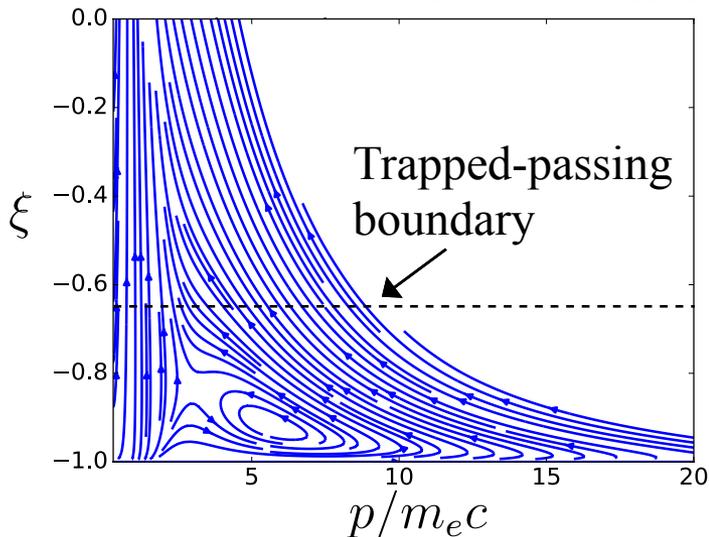


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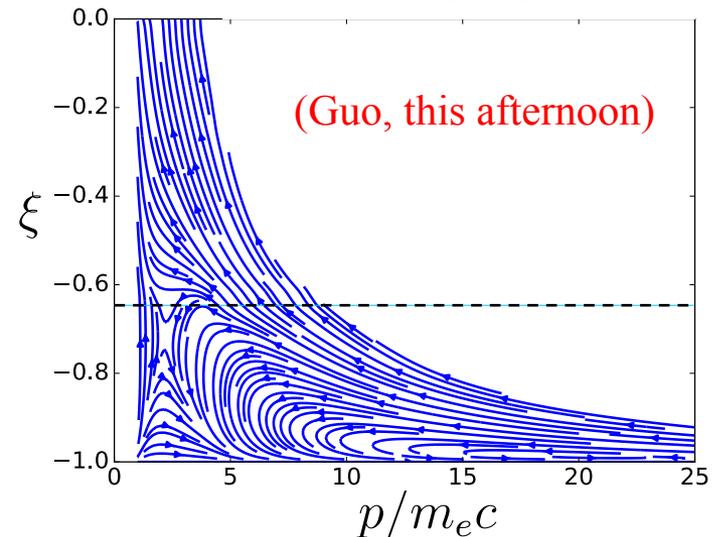
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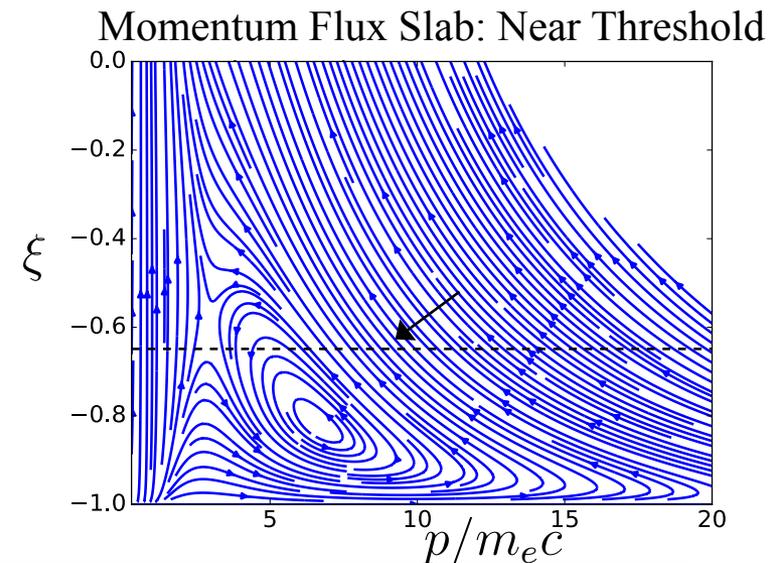
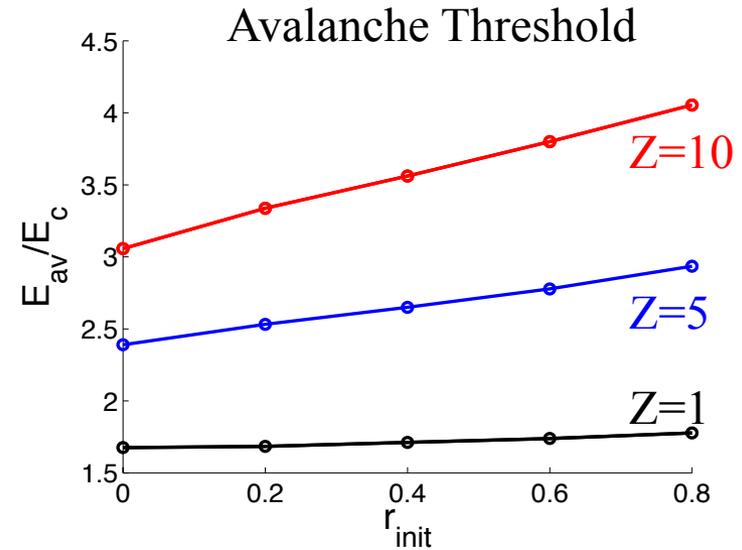


Momentum Flux Torus: Above Threshold



Impact of Toroidicity on Avalanche Threshold (cont'd)

- Threshold more strongly affected for high- Z_{eff} plasmas
- Presence of high- Z_{eff} ions enhances pitch-angle scattering
 - Broadens runaway distribution in pitch
 - Runaways more strongly affected by trapped passing boundary
- Trend not captured in early studies due to the neglect of synchrotron radiation



Collisional Transport of Runaway Electrons

- Collisional transport of runaway electrons is often assumed to be negligible
- The collisional transport of runaway electrons can be estimated as:

$$\frac{\tau_c D_{RA}}{a^2} \approx f_t^{RA} \frac{\Delta r^2}{2a^2} \tau_c \nu_D \approx \frac{f_t^{RA}}{2} \left(\frac{c}{a\omega_{c\theta}} \right)^2 (Z_{eff} + 1)$$

- where $\Delta r \sim c\gamma/\omega_{c\theta}$ (banana width of runaway), $\tau_c \nu_D \sim (Z_{eff} + 1)/p^2$, and f_t^{RA} is the fraction of trapped runaway electrons
- Comparing with thermal electrons yields (banana regime)

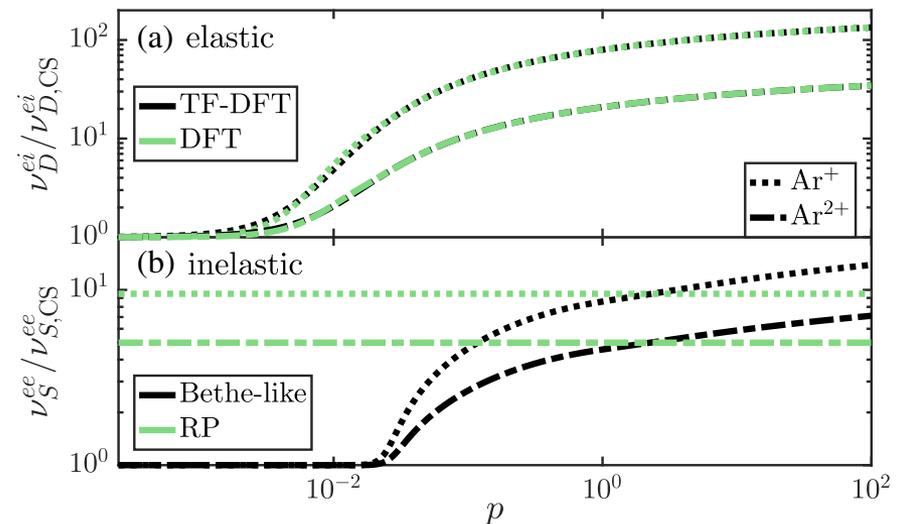
$$\frac{D_{RA}}{D_{Te}} \sim \frac{f_t^{RA}}{f_t} \frac{v_{Te}}{c} \ll 1$$

- Implies negligible transport of runaway electrons due to collisions

Impact of Plasma Impurities/Partial Screening

- Impurities often injected as a means of mitigating the heat load during the thermal quench
 - Radiate a significant fraction of thermal energy
- Resulting plasma composed of:
 - A low temperature bulk plasma containing weakly ionized impurities
 - Relativistic electrons

Hesslow et al. 2017



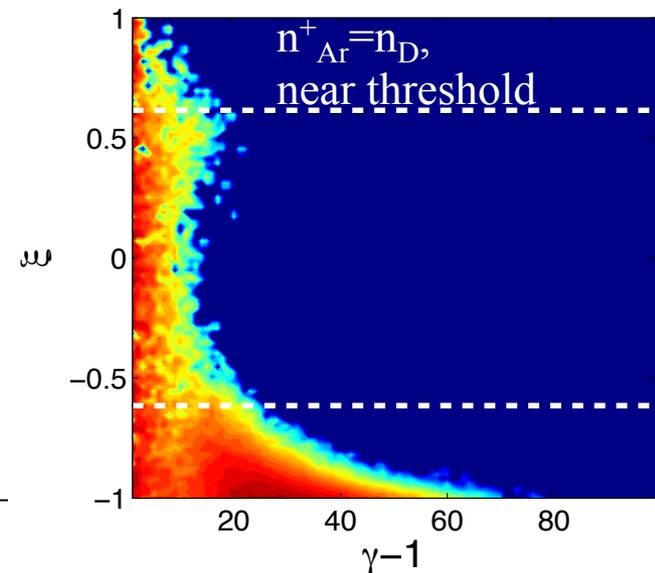
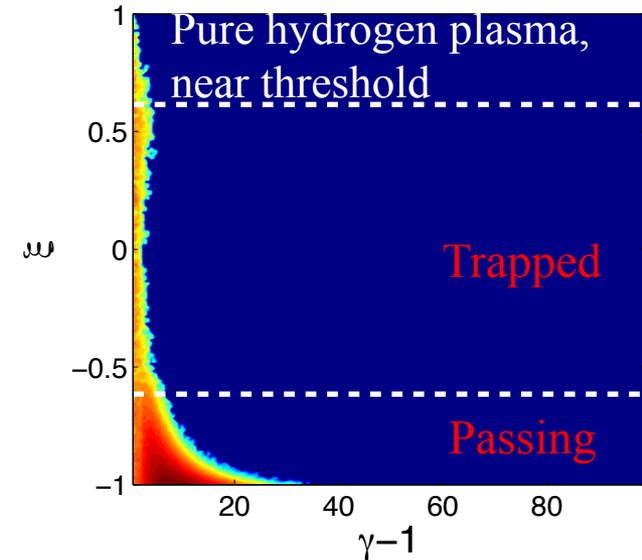
- Relativistic electrons able to probe internal structure of partially ionized impurity
 - Runaway electrons able to probe unshielded nuclei → enhanced pitch-angle scattering by a factor related to Z^2
 - Runaway electrons able to slow down against bound electrons → enhances drag by a factor of order Z

Consequences for Runaway Electron Distribution/Transport

- Enhanced collisional scattering due to partial screening leads to broader distribution in pitch of runaway electron distribution
- Collisional transport drastically enhanced:

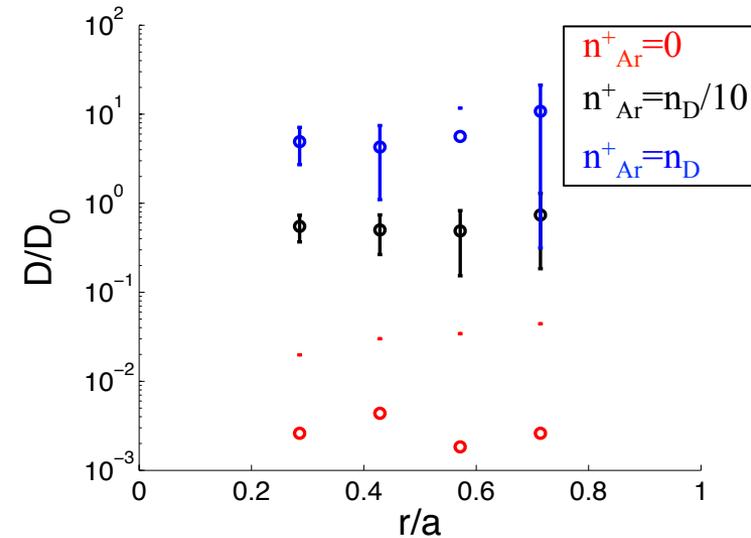
$$\frac{\tau_c D_{RA}}{a^2} \approx f_t^{RA} \frac{\Delta r^2}{2a^2} \tau_c \nu_D$$

- Pitch-angle scattering enhanced by roughly two orders of magnitude
- Finite trapped particle fraction at high energies



Spatial Transport of Runaway Electrons: Diffusion

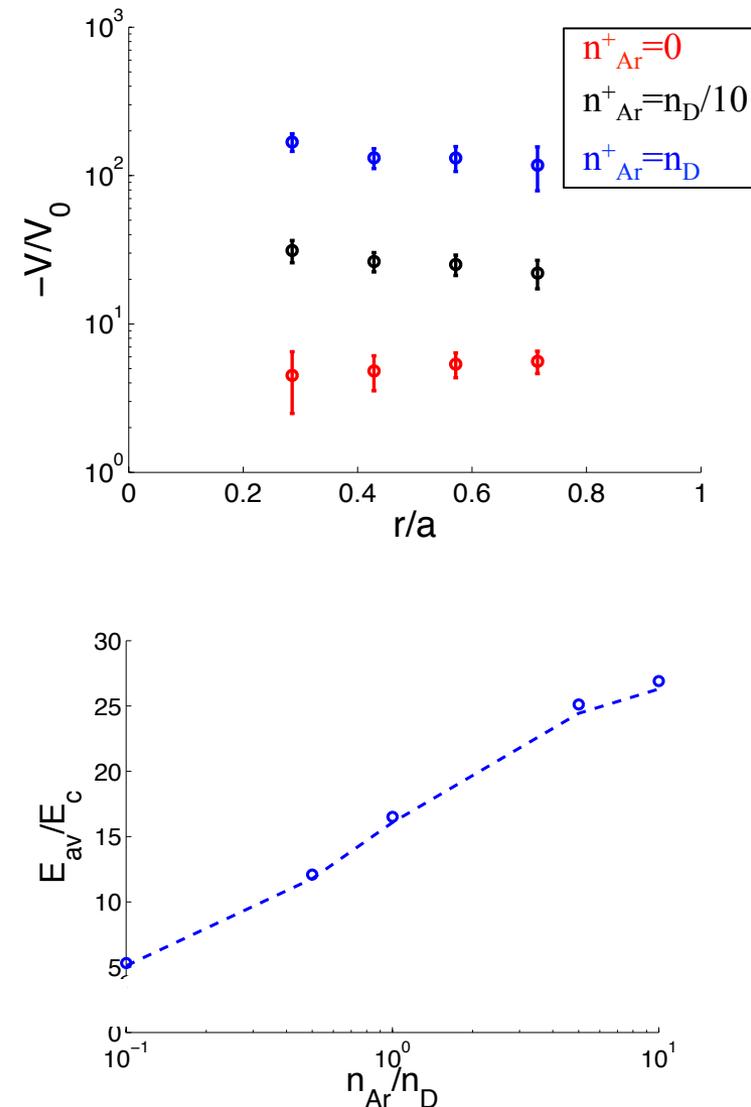
- Collisional diffusion of runaway electrons dramatically enhanced by partially ionized impurities
 - A small amount of argon impurities enhances transport by more than an order of magnitude
 - Collisional diffusivity increases with the amount of argon fraction



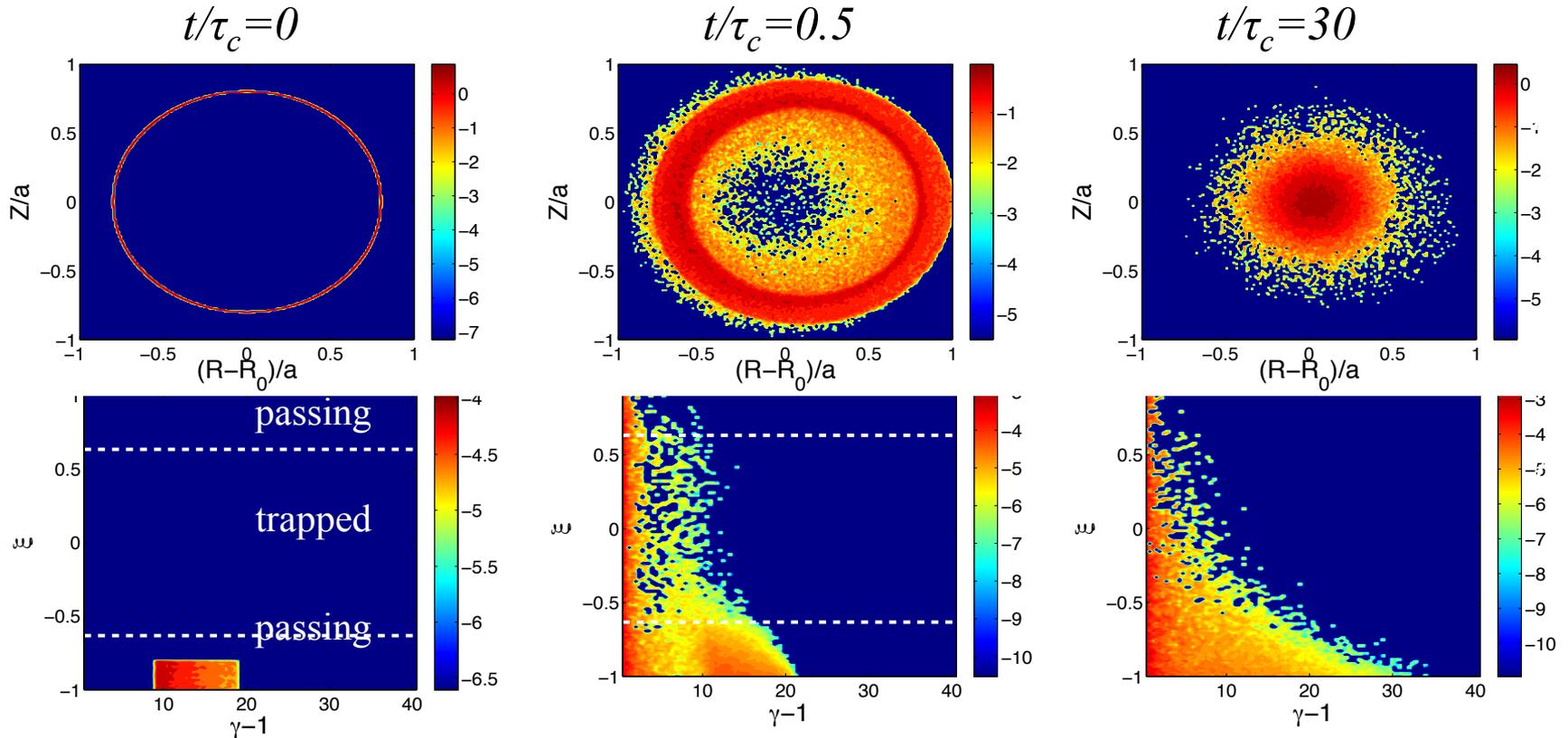
Spatial Transport of Runaway Electrons: Convection

- Convection velocity similarly enhanced
- Convective transport enhanced via two mechanisms:
 - The presence of a significant impurity population increases the magnitude of the inductive electric field necessary to sustain a runaway electron population
 - The increase of pitch-angle scattering results in a larger population of energetic trapped electrons \leftrightarrow allows significant contribution from the Ware pinch

$$\Gamma_r^{Ware} \sim -f_t^{RA} \frac{E_\varphi}{B_\theta}$$



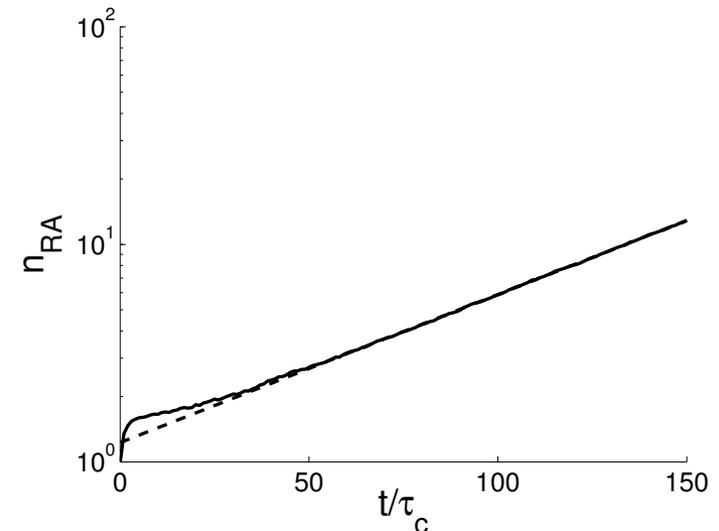
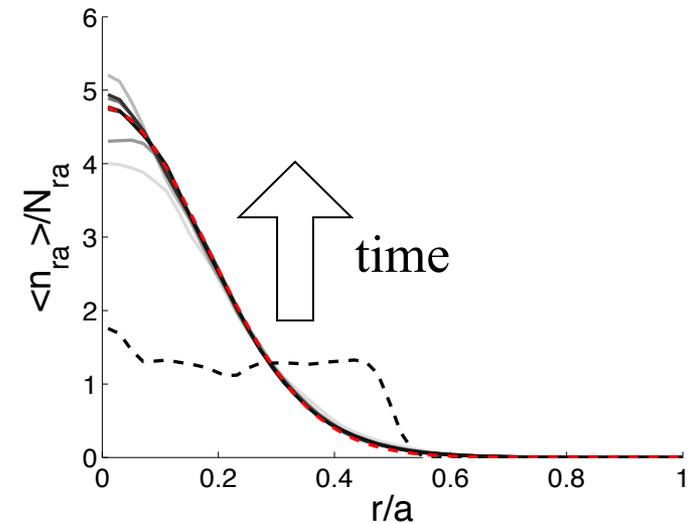
Spatial Transport: Role of Ware Pinch



- Considering a ring of electrons initialized at a large radius (DIII-D like case)
 - Strong pitch-angle scattering leads to the formation of energetic particle population
 - Ware pinch convects a small fraction of energetic electrons inward
 - Inwardly convected electrons are detrapped \rightarrow run away
 - Provide “seed” for avalanche instability near $r/a \approx 0$
- Resulting runaway population strongly peaked near tokamak origin
 - Final state largely independent of phase space distribution of “seed” electron population

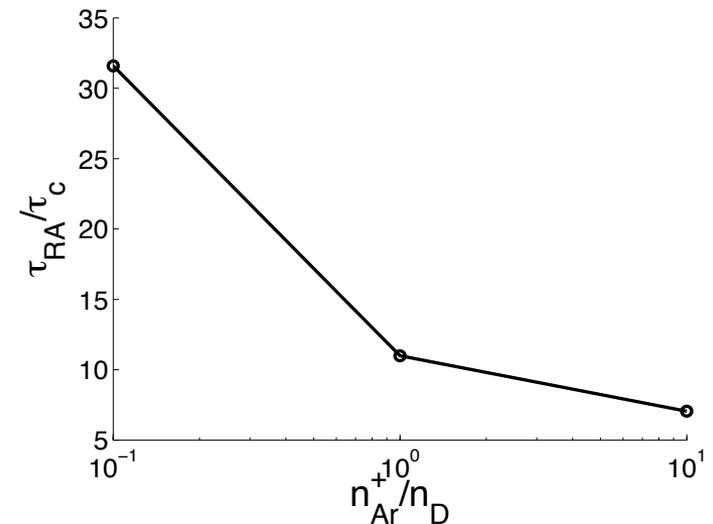
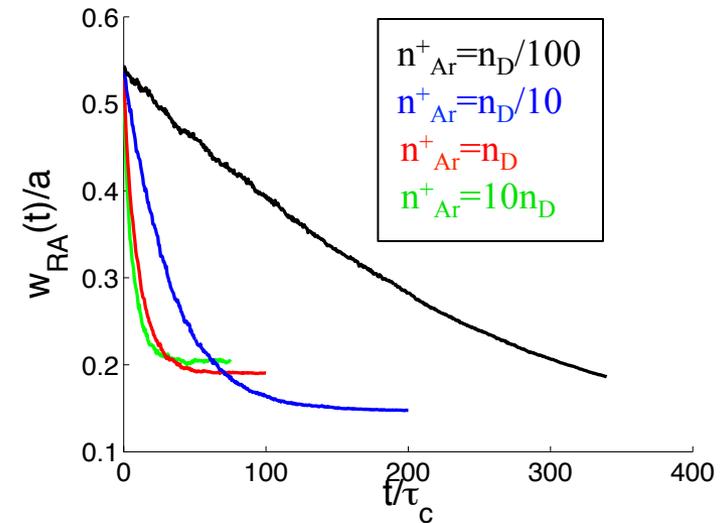
Formation of Runaway Spatial Eigenmode

- Runaway electrons tend toward a spatial eigenmode in long time limit
- Focusing of runaway electrons near origin is due to:
 - Inward convection, primarily due to the Ware pinch
 - Peaking of the avalanche growth rate near $r/a \approx 0$
- Finite spatial spread determined by:
 - Diffusion of runaway electrons
 - Finite orbit width



Eigenmode Width and Relaxation Time

- Width and relaxation time to a spatial eigenmode depends sensitively on the impurity fraction of the plasma
- Larger impurity fraction tends to increase the eigenmode width, reduce the timescale τ_{RA} for the relaxation to the eigenmode
- Pure hydrogen plasmas unlikely to collapse to runaway eigenmode on experimentally relevant time scales



Conclusions

- The transport of runaway electrons can be significant during conditions typical of actively mitigated disruption scenarios even when good flux surfaces are present
 - Requires extension of momentum space formulations to account for real space transport
- The presence of partially ionized impurities:
 - significantly enhances transport
 - aids in establishing centrally peaked runaway electron distribution
- In the long time limit, runaway electrons form a spatial eigenmode near the tokamak origin
 - Spatial eigenmode independent of runaway seed \Leftrightarrow enabled by spatial transport



Impact of Self-Consistent Evolution of Inductive Electric Field

- Axisymmetric electric field evolved by:

$$\nabla \times \mathbf{E} = -\frac{\partial \mathbf{B}}{\partial t}, \quad \nabla \times \mathbf{B} = \mu_0 \mathbf{j}$$

- where $E_{\parallel} = \eta (j_p - j_{RA})$
- Self-consistently computed inductive electric field has non-trivial structure
 - Conducting wall boundary condition forces inductive electric field to decay at larger radii
 - Rapid generation of runaways near $r/a \approx 0$ can result in a hollow profile
- Transient evolution of the runaway spatial profile strongly affected
 - Spatial mode width more weakly impacted

