

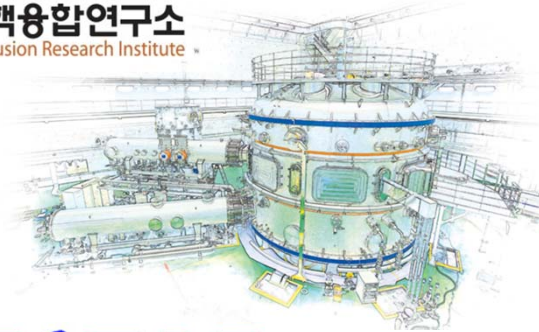
# Rotating MHD Analysis for Disruption Event Characterization and Forecasting

J.D. Riquezes<sup>1</sup>, S.A. Sabbagh<sup>1</sup>, J.W. Berkery<sup>1</sup>, Y.S. Park<sup>1</sup>, J.H.  
Ahn<sup>1</sup>, Y. Jiang<sup>1</sup>, R.E. Bell<sup>2</sup>, E. Fredrickson<sup>2</sup>, L.A. Morton<sup>3</sup>

<sup>1</sup>Department of Applied Physics, Columbia University, New York, NY

<sup>2</sup>Princeton Plasma Physics Laboratory, Princeton, NJ

<sup>3</sup>Oak Ridge Associated Universities, Oak Ridge, TN



**6<sup>th</sup> Annual TSDW**

**July 16-18, 2018**

**PPPL**



COLUMBIA UNIVERSITY  
IN THE CITY OF NEW YORK



Supported by US DOE Contracts DE-SC0016614, DE-SC0018623, and DE-FG02-99ER54524



# Automated identification of rotating MHD modes can be a practical tool for disruption forecast efforts

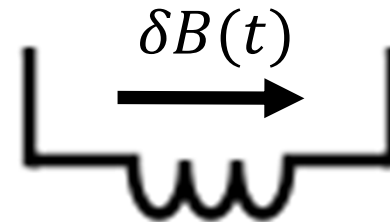
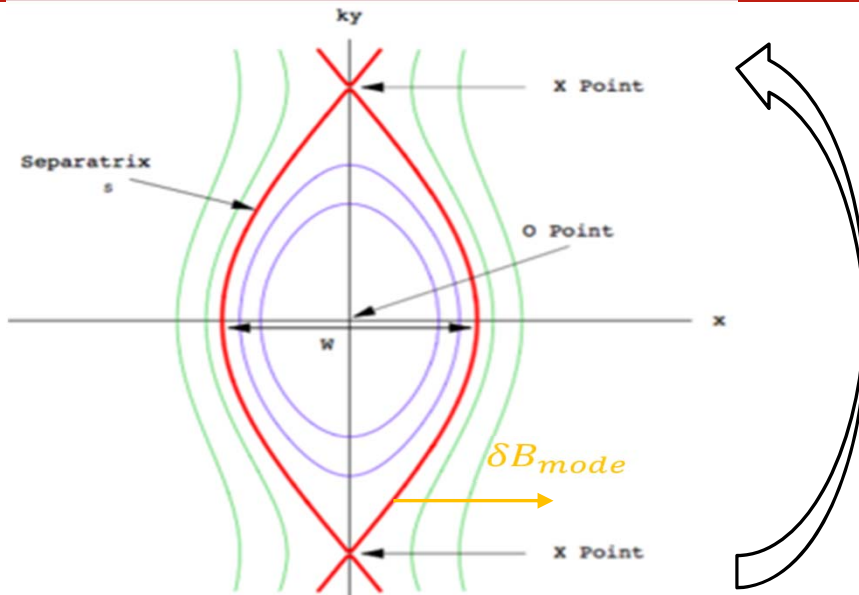
## □ Motivation:

- Validate the automated identification of rotating MHD instabilities in a tokamak plasma
- Develop a disruption warning level based on rotating MHD activity

## □ Talk Outline

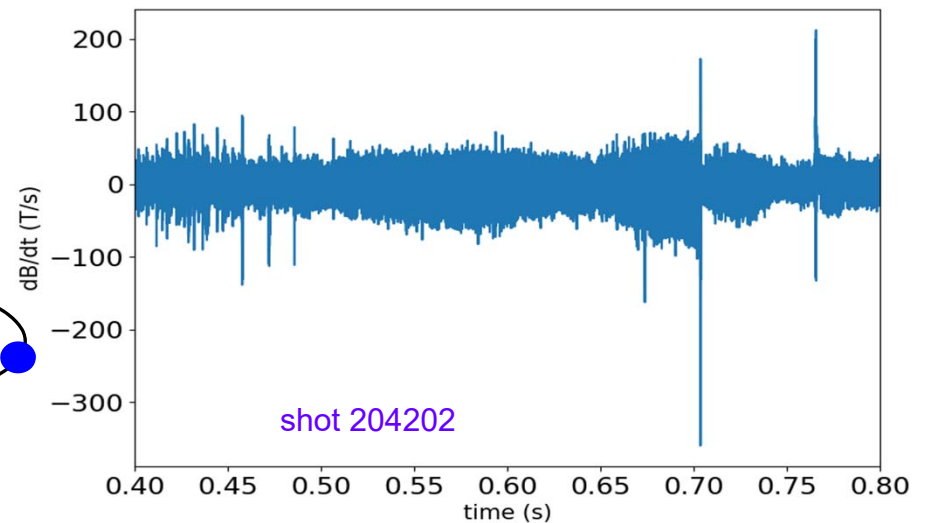
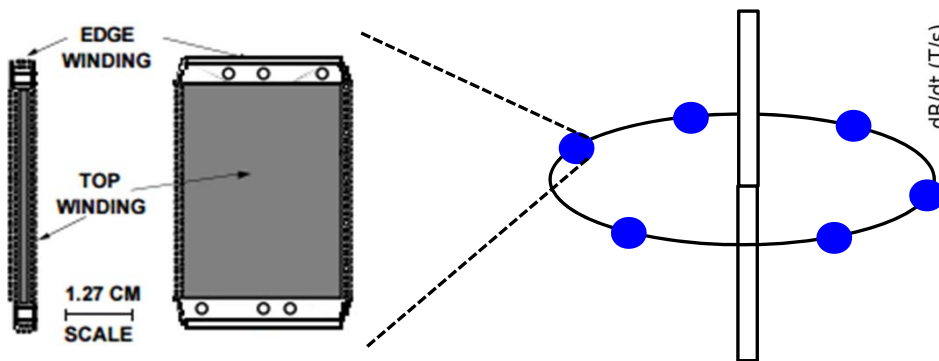
- Analysis and automated identification of rotating MHD
- Set of criteria used to determine a warning level for disruptions
- NSTX examples of varying plasma activity the code is tested on
- Summary & next steps

# Toroidal magnetic probes measure amplitude of magnetic field perturbations from modes



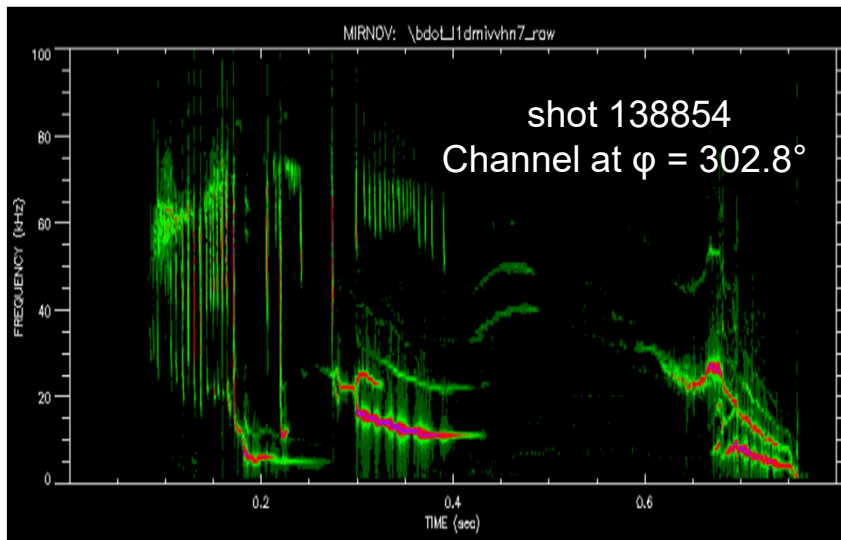
- Mode rotation can be detected by magnetic “pick up” coils placed toroidally around the tokamak

- Error fields and current gradients drive formation of magnetic islands

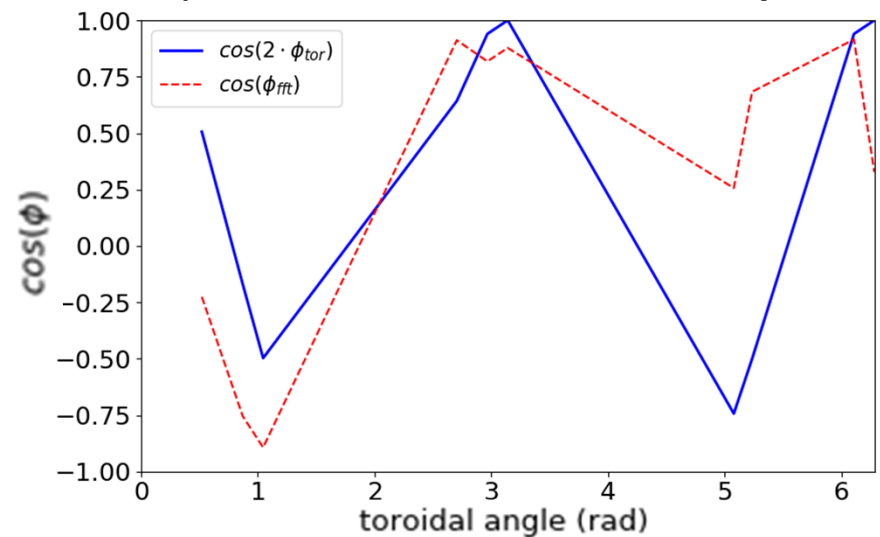
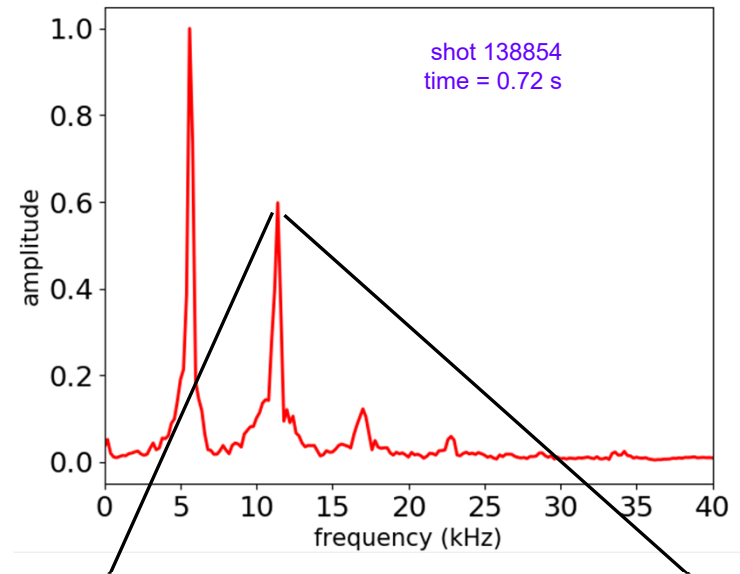


# Spectral decomposition of probe signals used to identify the mode number and rotation frequency

- Consecutive short time FFTs give the phase and amplitude of a signal in frequency and time



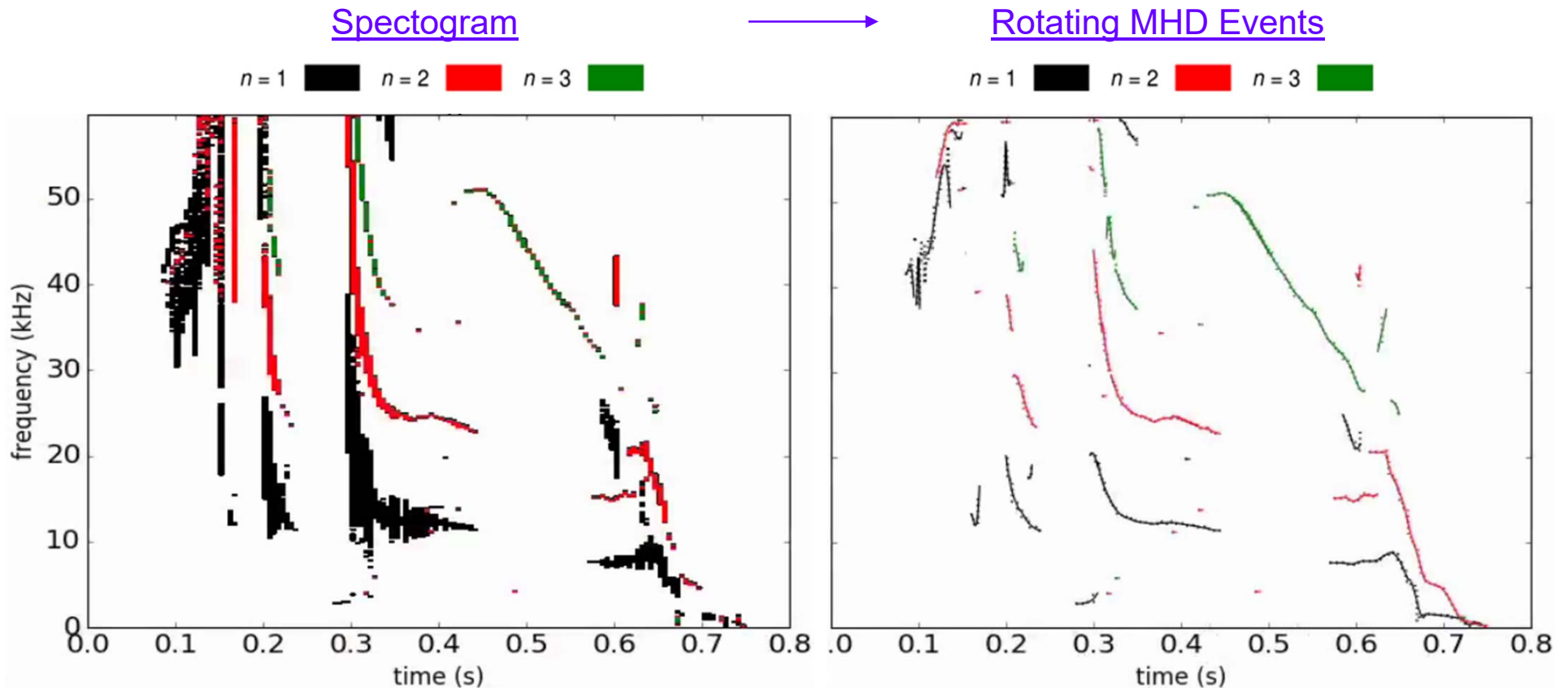
- The phase shifts at every frequency and time point for the channel array should match with the expected toroidal angle dependence of the predominant n mode.





# Simplified generated spectrogram for further analysis of rotating MHD modes

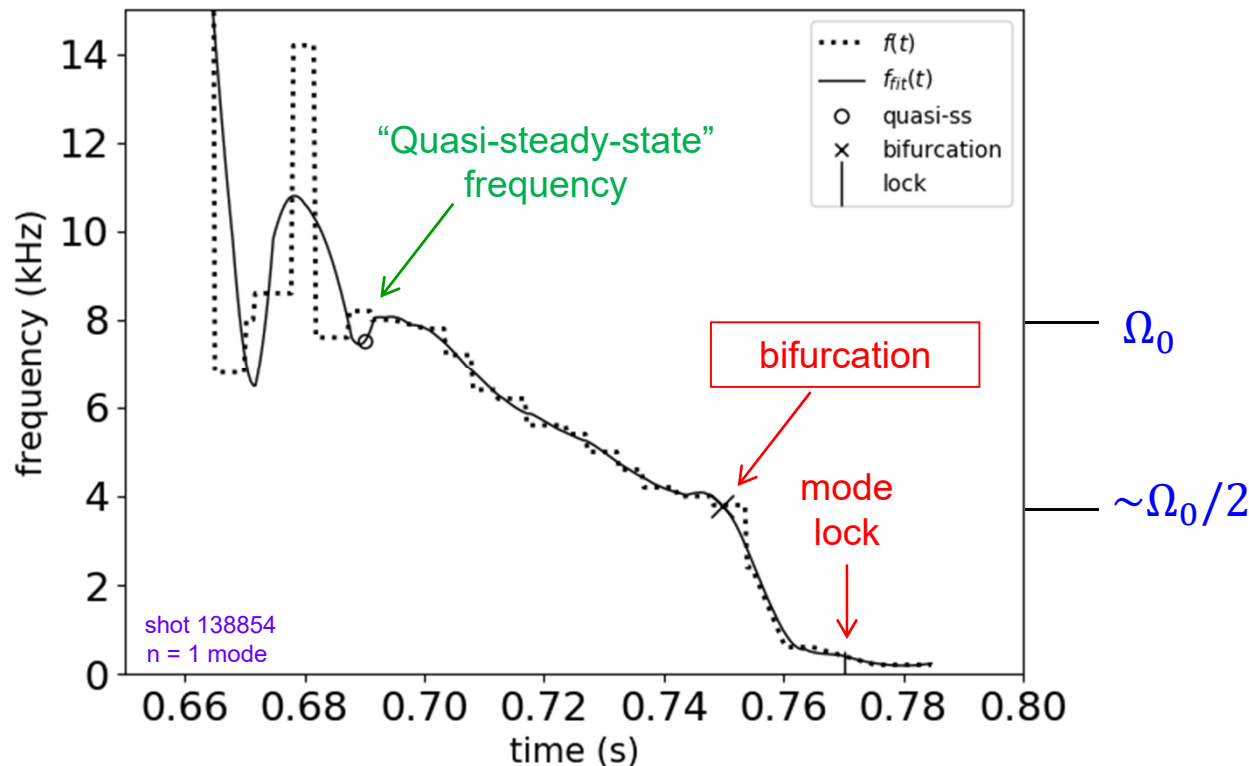
- Selected peak amplitude frequency from bandwidth
- Performed smoothing fit on frequency curves



shot 130198

# Rotating MHD modes create a friction in the plasma that leads to slowing of the modes and potential locking

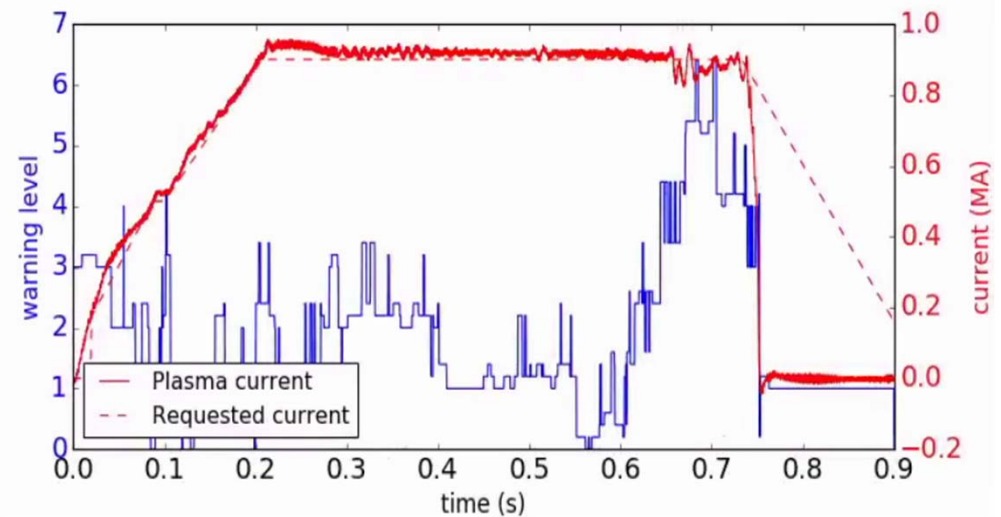
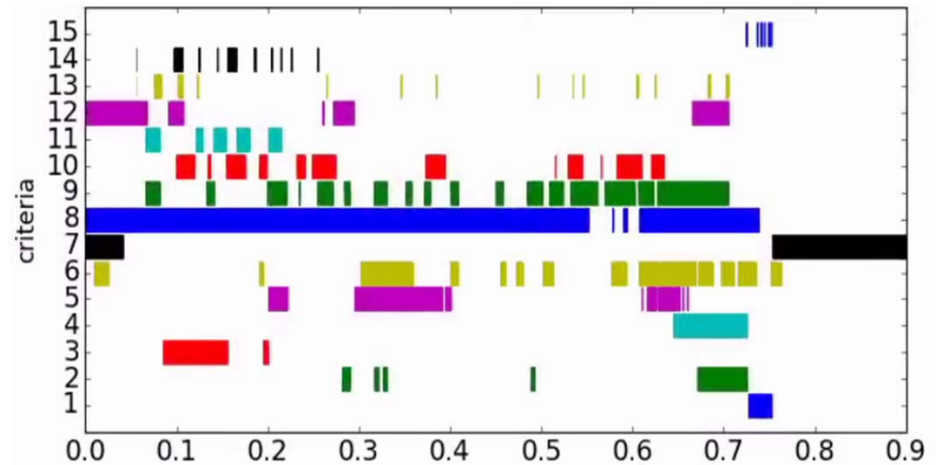
- ❑ Natural frequency of mode rotation is reached due to a force balance of drag and driving auxiliary heating
- ❑ In the process of slowing down the mode can lose force balance leading to a frequency bifurcation



# Severity of mode determined from criteria based on rotating MHD analysis and relevant plasma signals

- ❑ Low frequency magnetic probes
- ❑ Rotation Profiles
- ❑  $\beta_N$  and internal inductance
- ❑ Mode amplitude
- ❑ Past bifurcation
- ❑ Magnitude of frequency
  
- ❑ Criteria cover magnetic and kinetic properties of the plasma relevant to rotating MHD mode evolution
  
- ❑ Summed criteria with the appropriate weights to generate disruption warning level

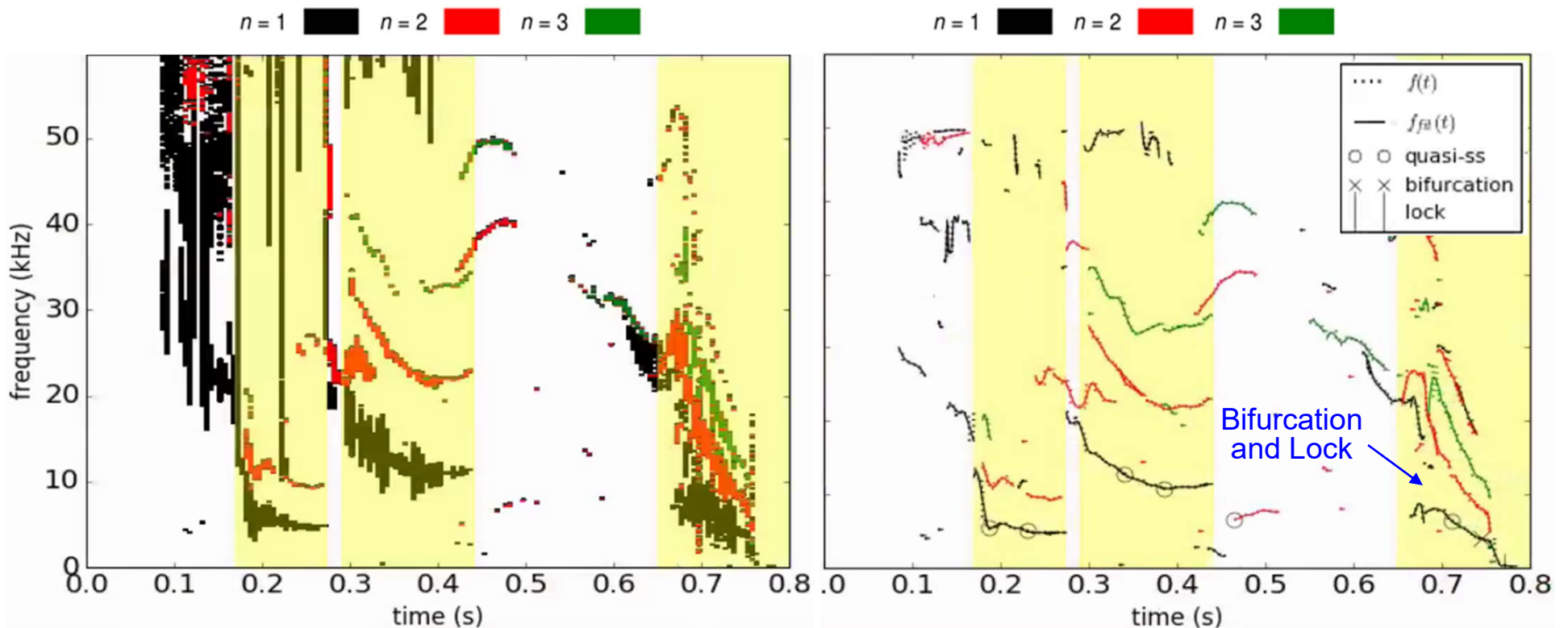
Criteria	Description
15	Locked n=1 strong
14	Outer core rotation
13	Mid core rotation
12	Low core rotation
11	Dec. outer rotation
10	Dec. mid rotation
9	Dec. core rotation
8	Low li
7	$\beta_N$ /li range
6	Decreasing $\beta_N$
5	Strong mode
4	Bifurcation
3	High-freq
2	Low-freq
1	Lock freq



shot 130198

# Example 1: Archetypal mode bifurcation and locking

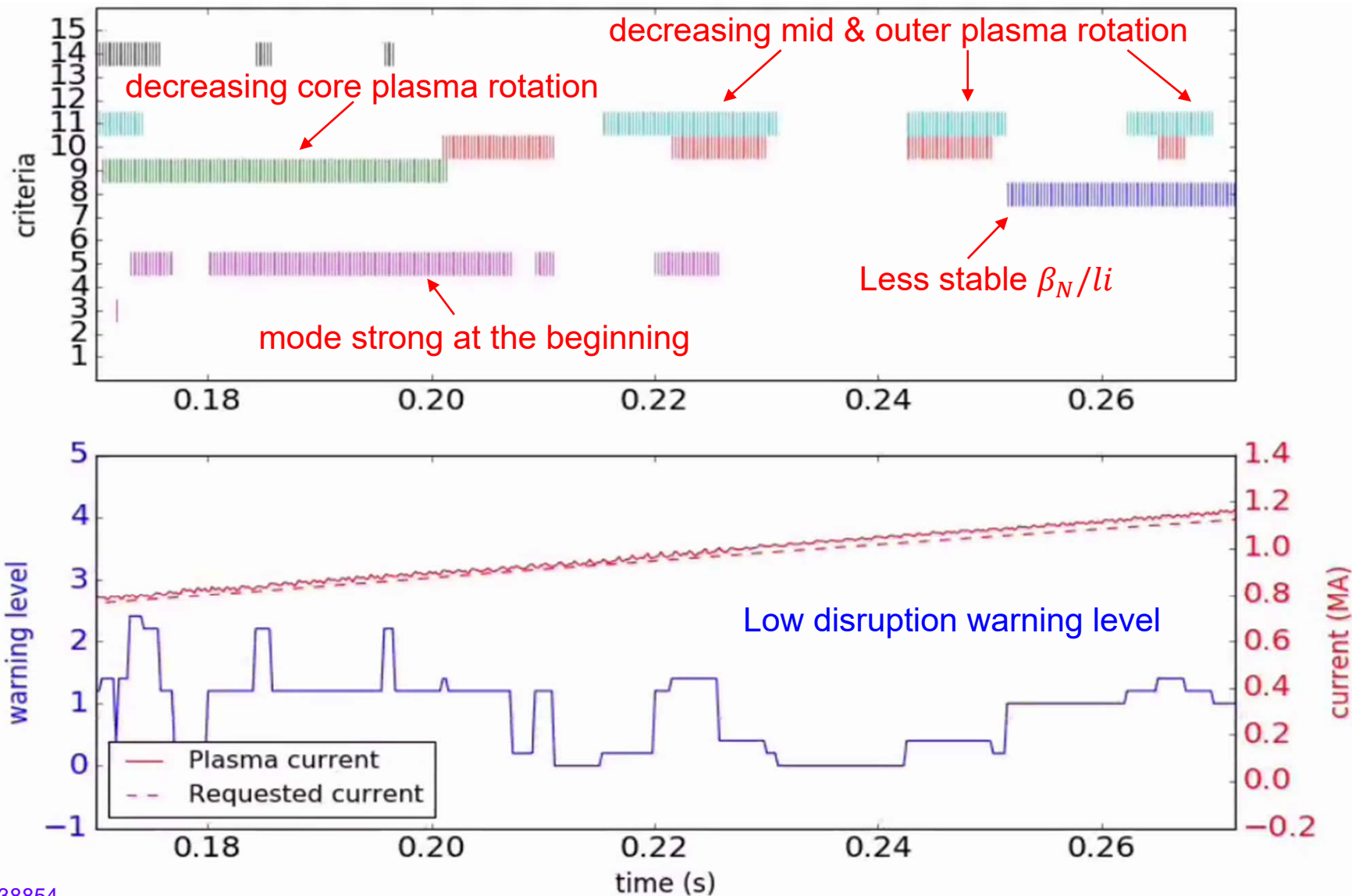
- ❑ Separate into three periods of mode activity
  - ❑ During startup
  - ❑ At start of flat top
  - ❑ At start of ramp-down



shot 138854

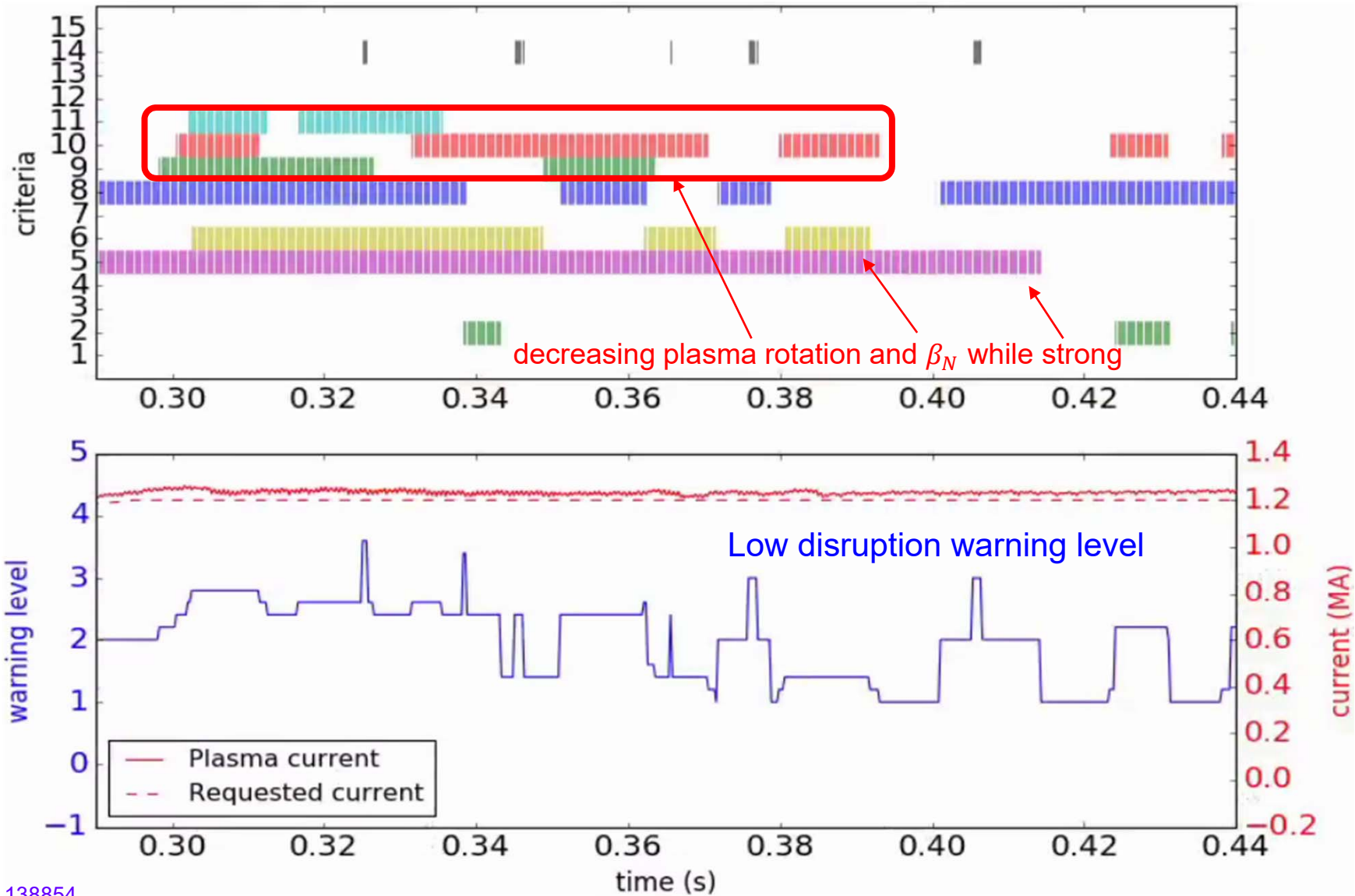


# 1<sup>st</sup> Period: Safe mode and plasma activity is shown by relatively low disruption warning level



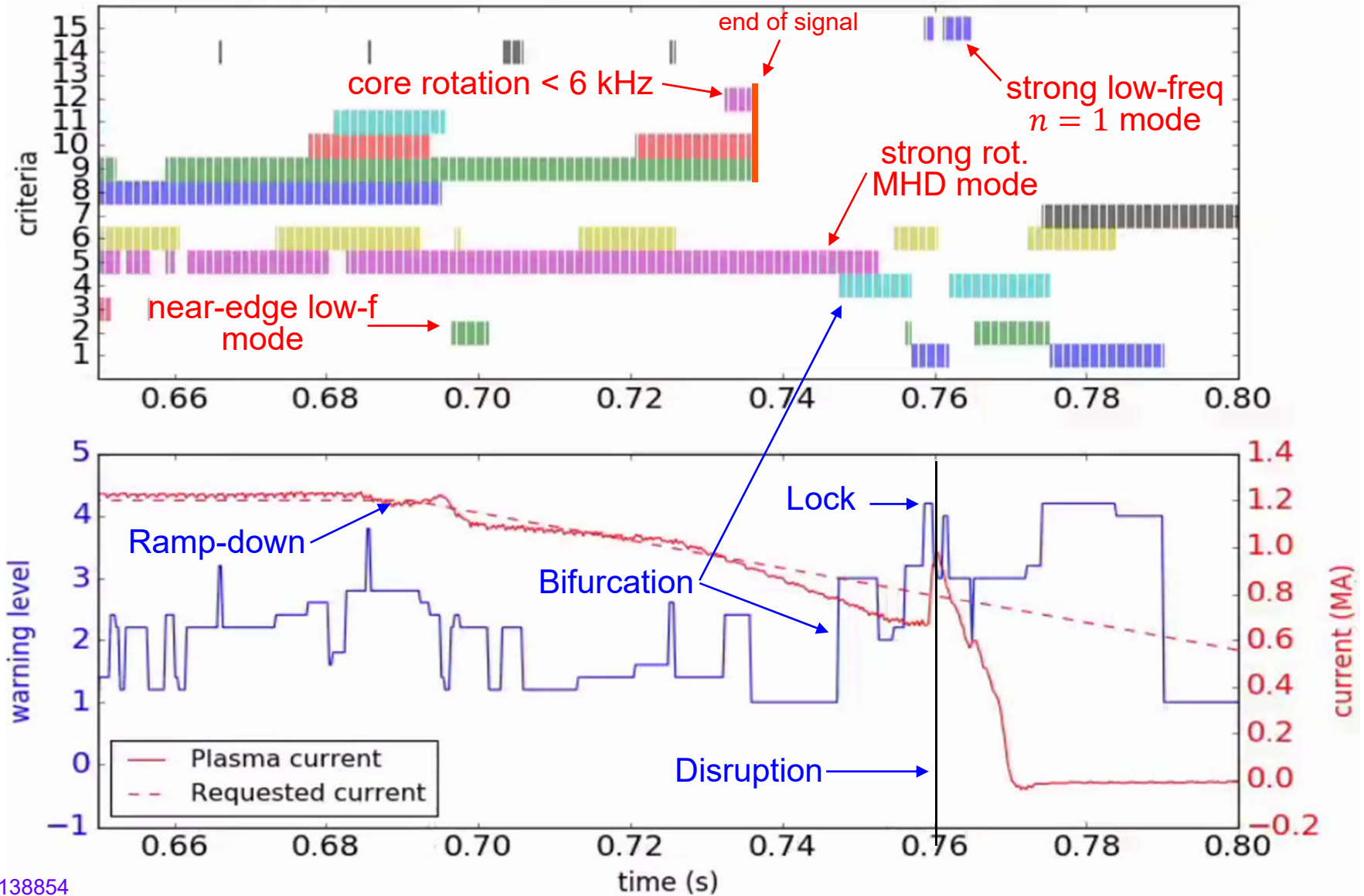
shot 138854

## 2<sup>nd</sup> Period: Modes lead to dip in plasma rotation but plasma recovers and warning levels remain low



shot 138854

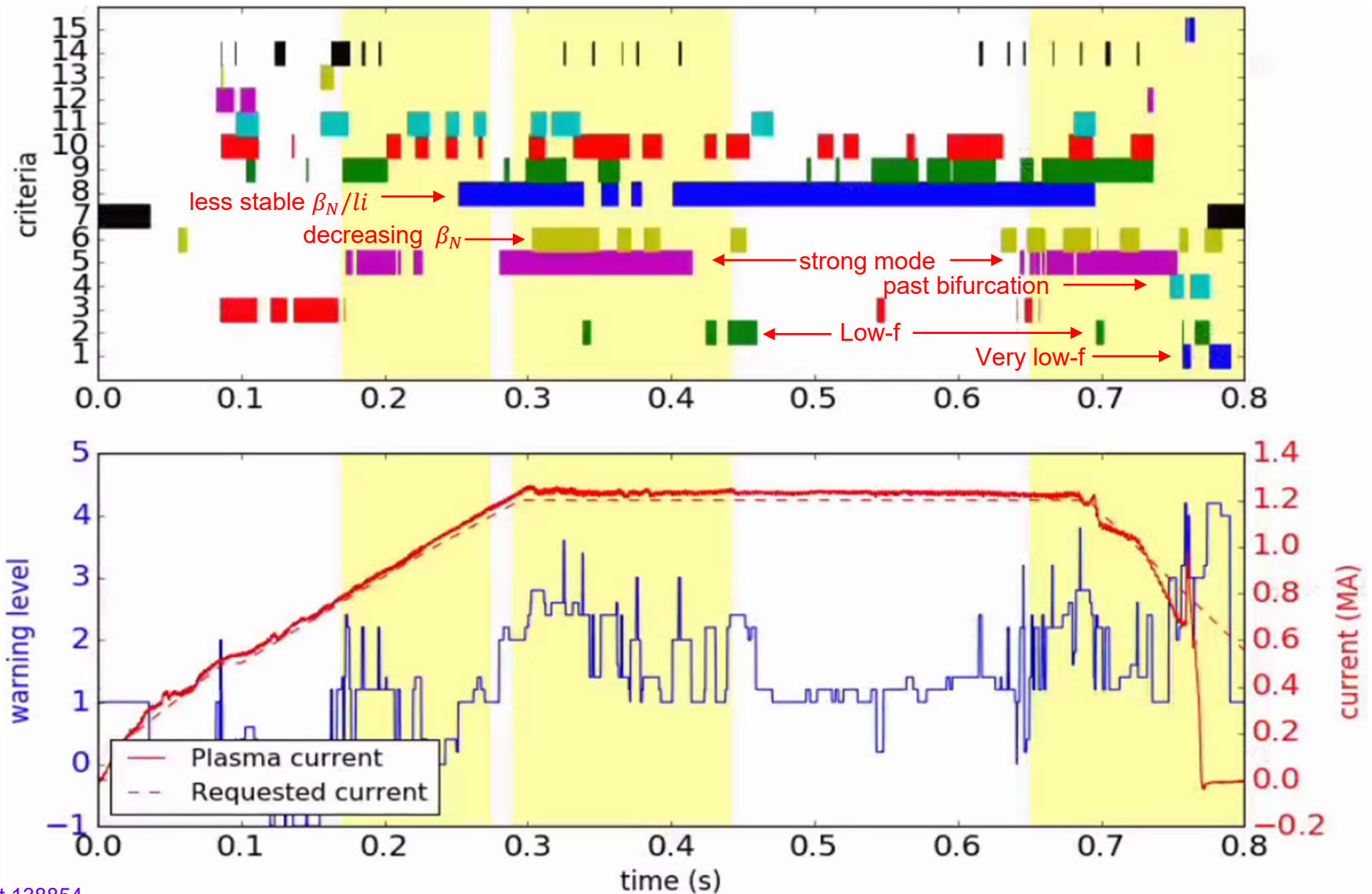
# 3<sup>rd</sup> Period: Warning level increases as plasma bifurcates, locks, and disrupts



shot 138854



# Example 1: Complete shot overview of warning levels shows relative severity of mode activity

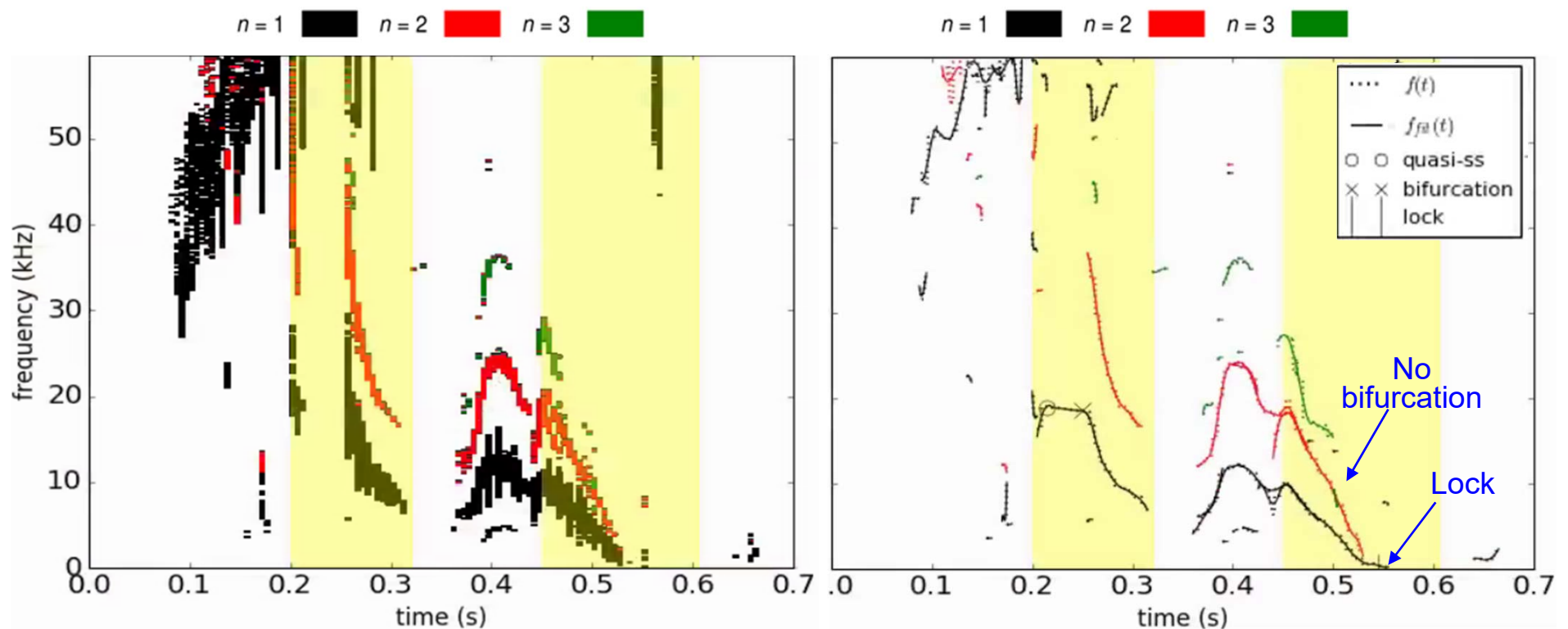


shot 138854



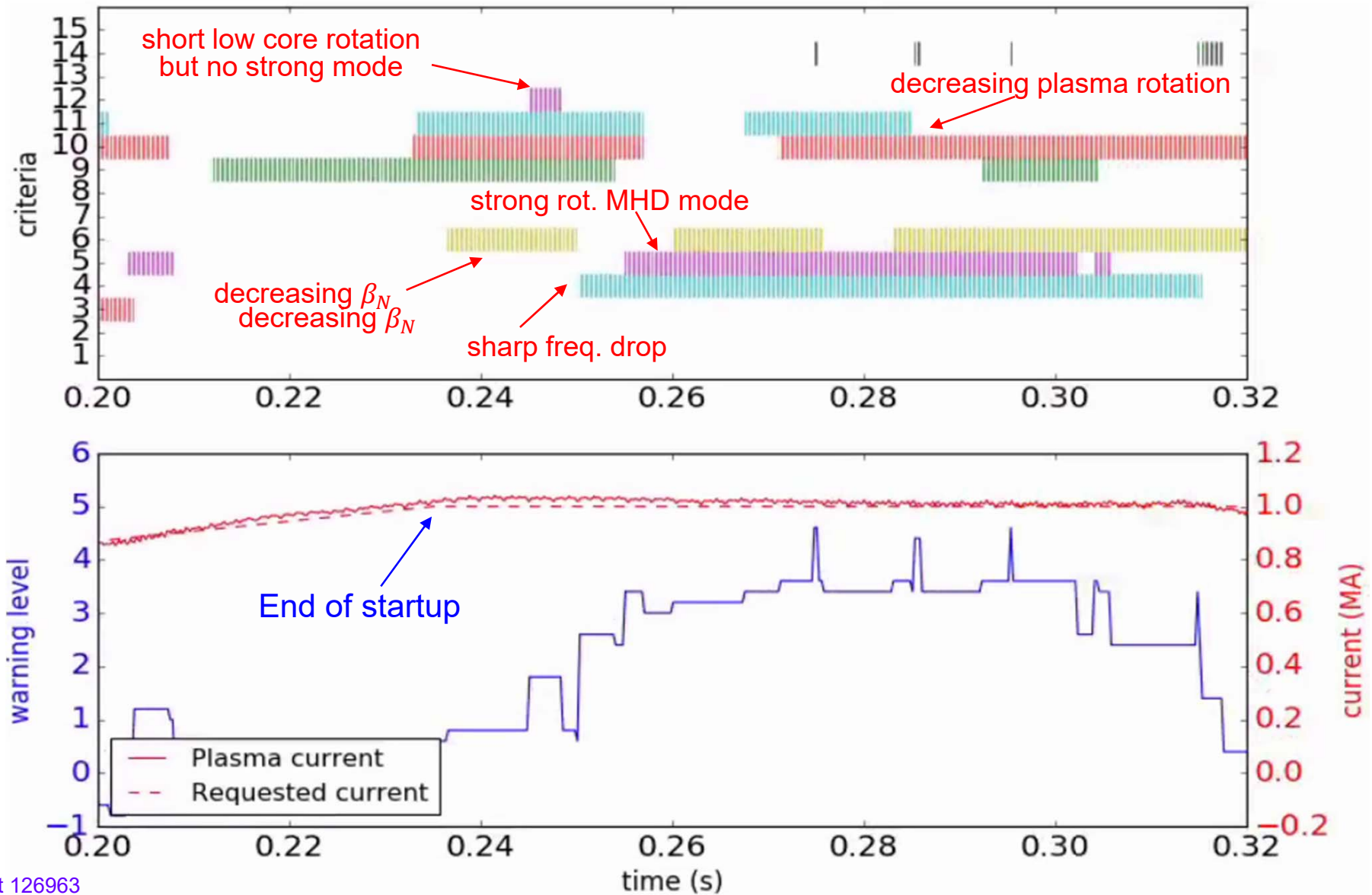
## Example 2: Mode slowing and locking without bifurcation

- Bifurcation may be avoided if island size reduces through mode evolution
- Separate into 2 regions:
  - Sharp decrease in mode rotation frequency
  - Slowing and locking without a bifurcation (then disrupts)



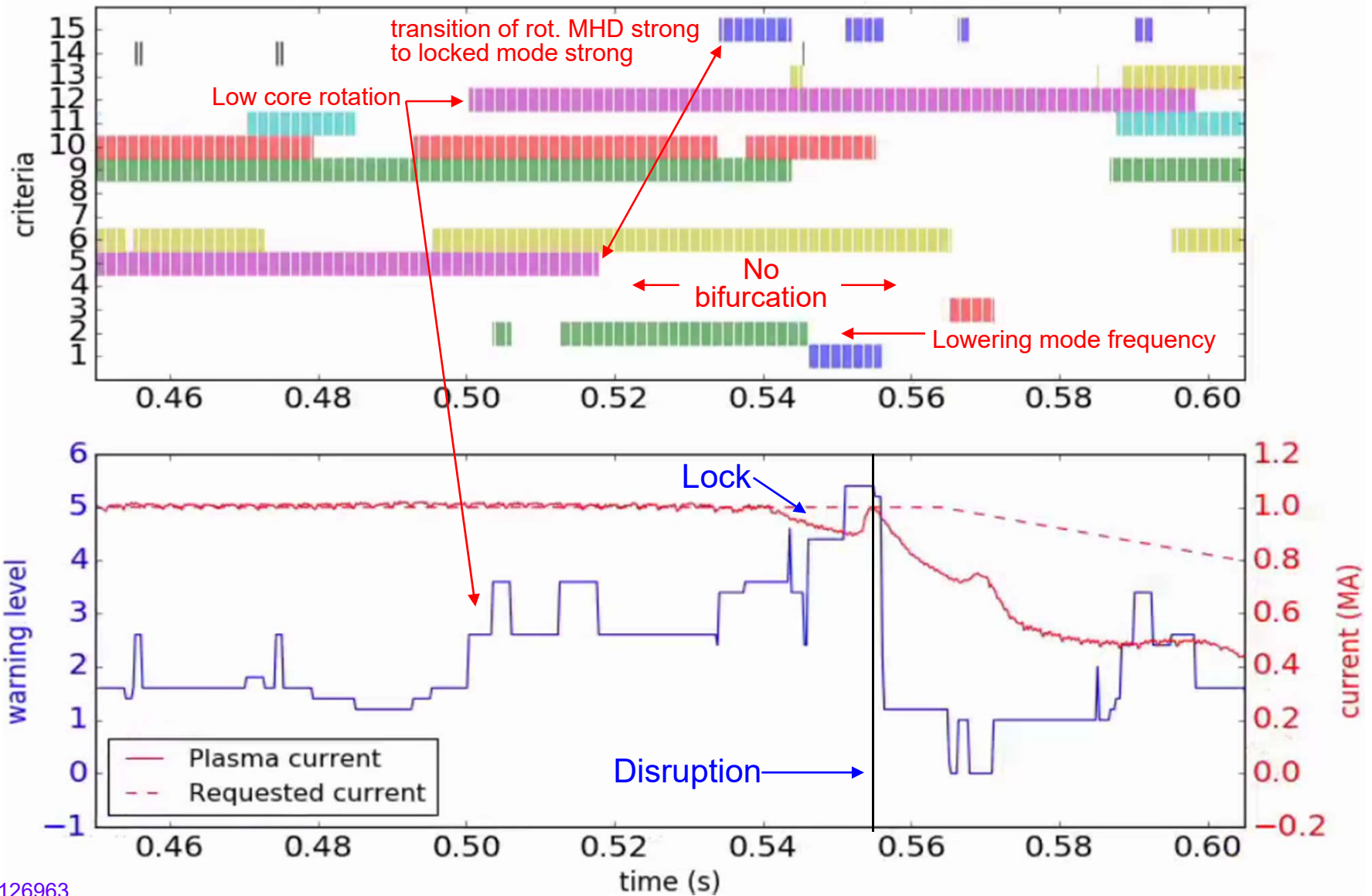
shot 126963

# 1<sup>st</sup> Period: Sharp drop in mode rotation leads to increase in warning level



shot 126963

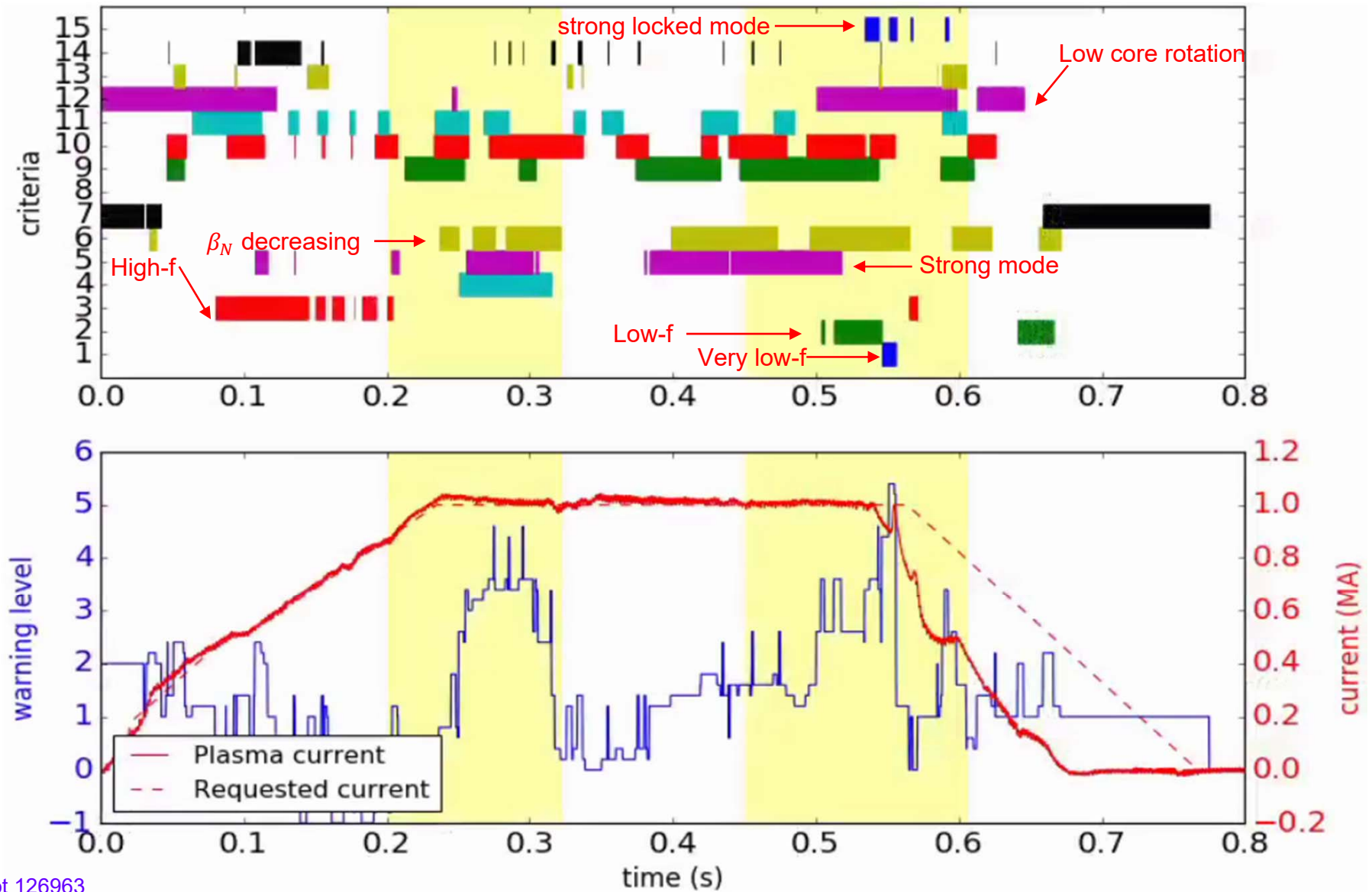
## 2<sup>nd</sup> Period: Rising warning level without bifurcation due to low plasma and mode rotation



shot 126963



## Example 2: Complete shot overview of warning levels shows relative severity of mode evolution

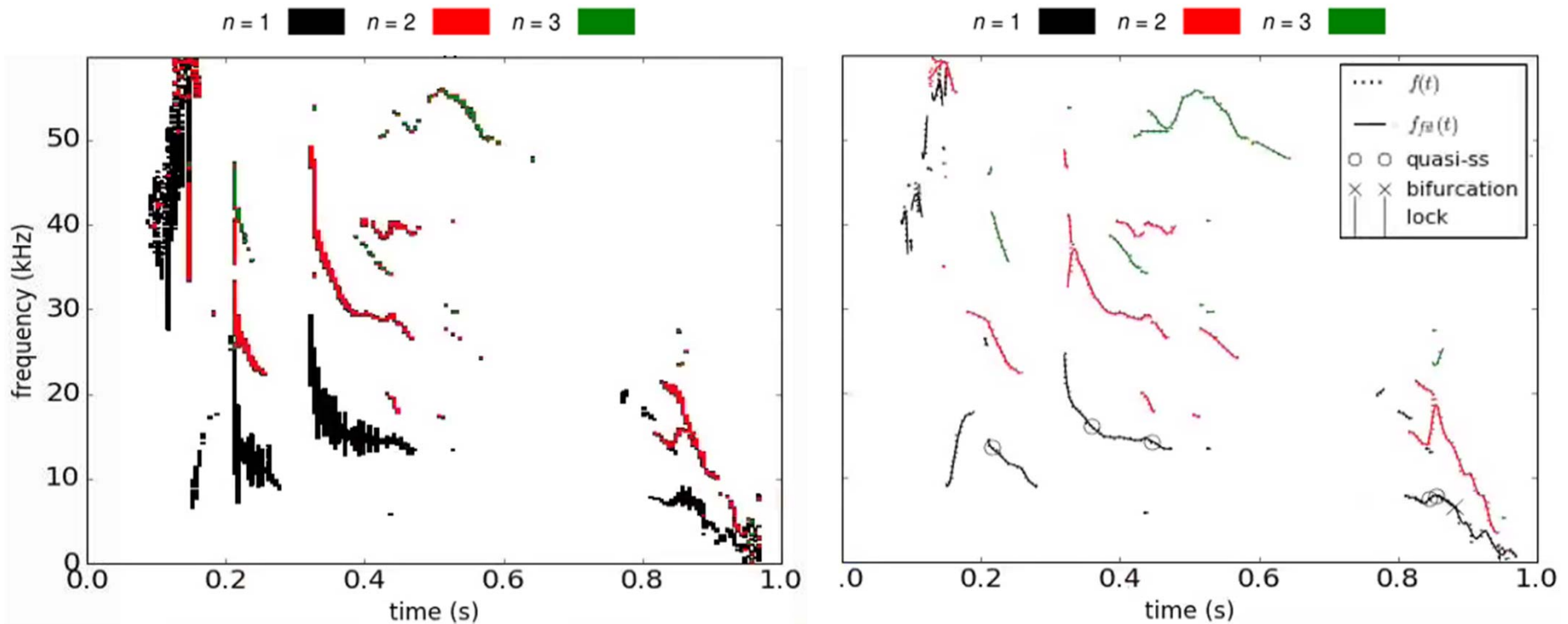


shot 126963



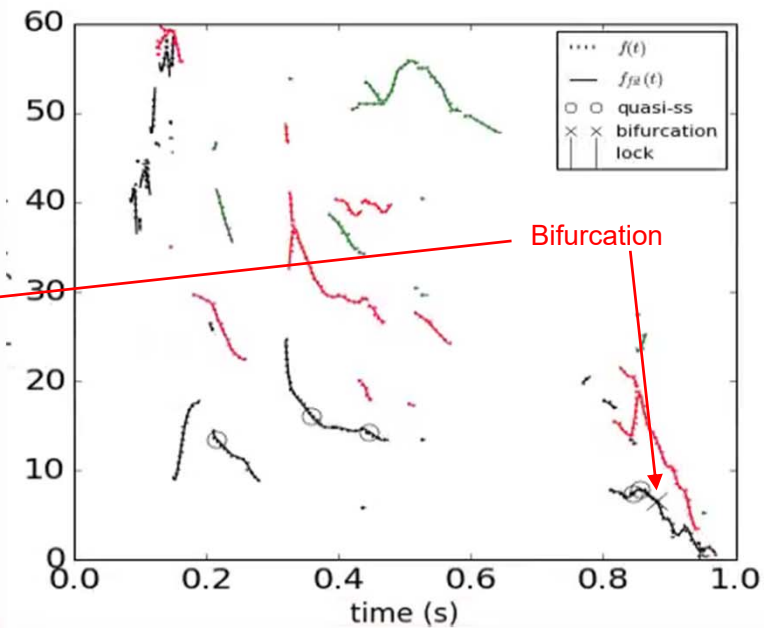
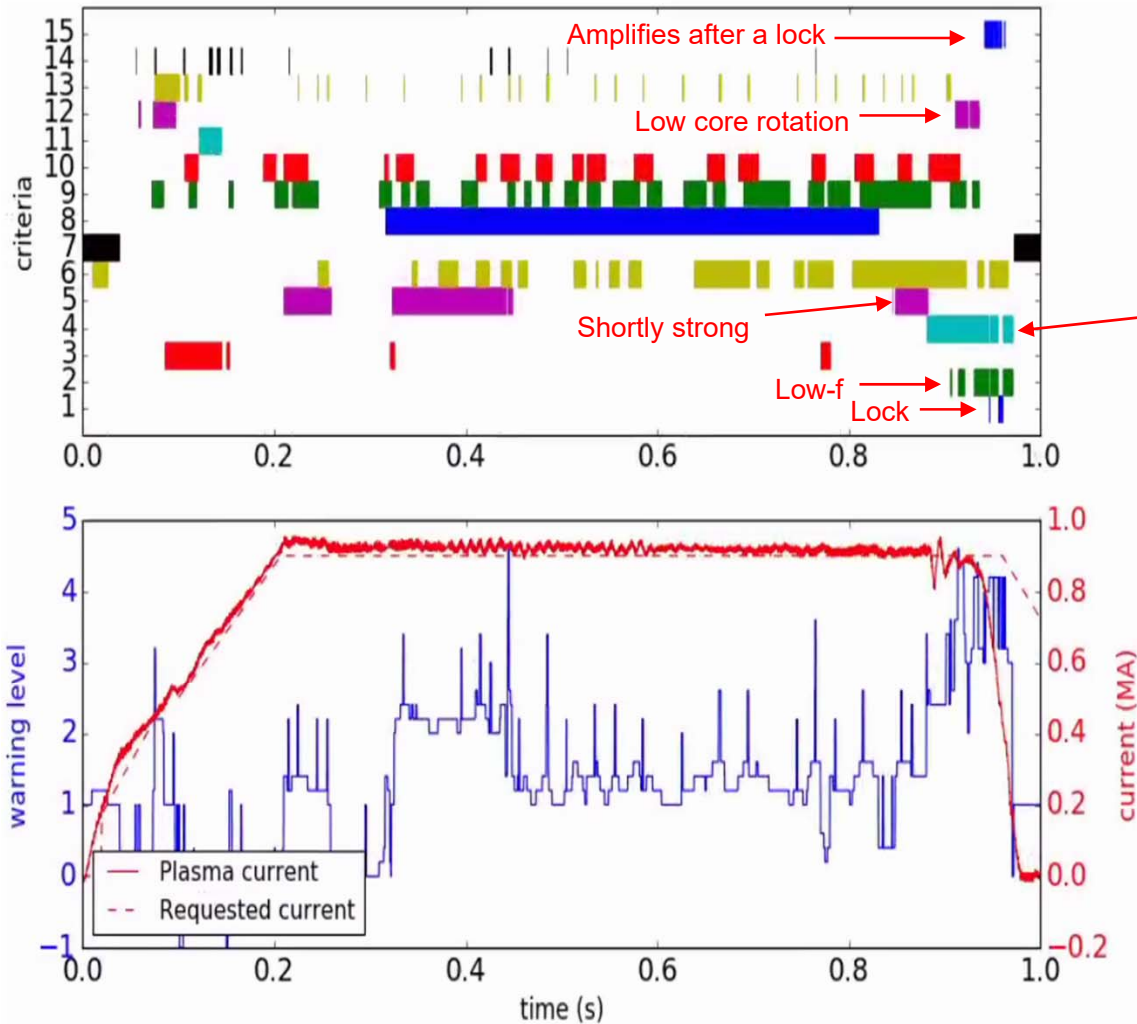
## Example 3: Tearing mode approaching marginal island width

- More subtle case as the aim is to stabilize the mode with decreasing island size
- Locked modes amplify after plasma rotation is low enough



shot 130190

# Example 3: Warning level increases primarily by lowered plasma rotation and mode frequency even at low amplitude

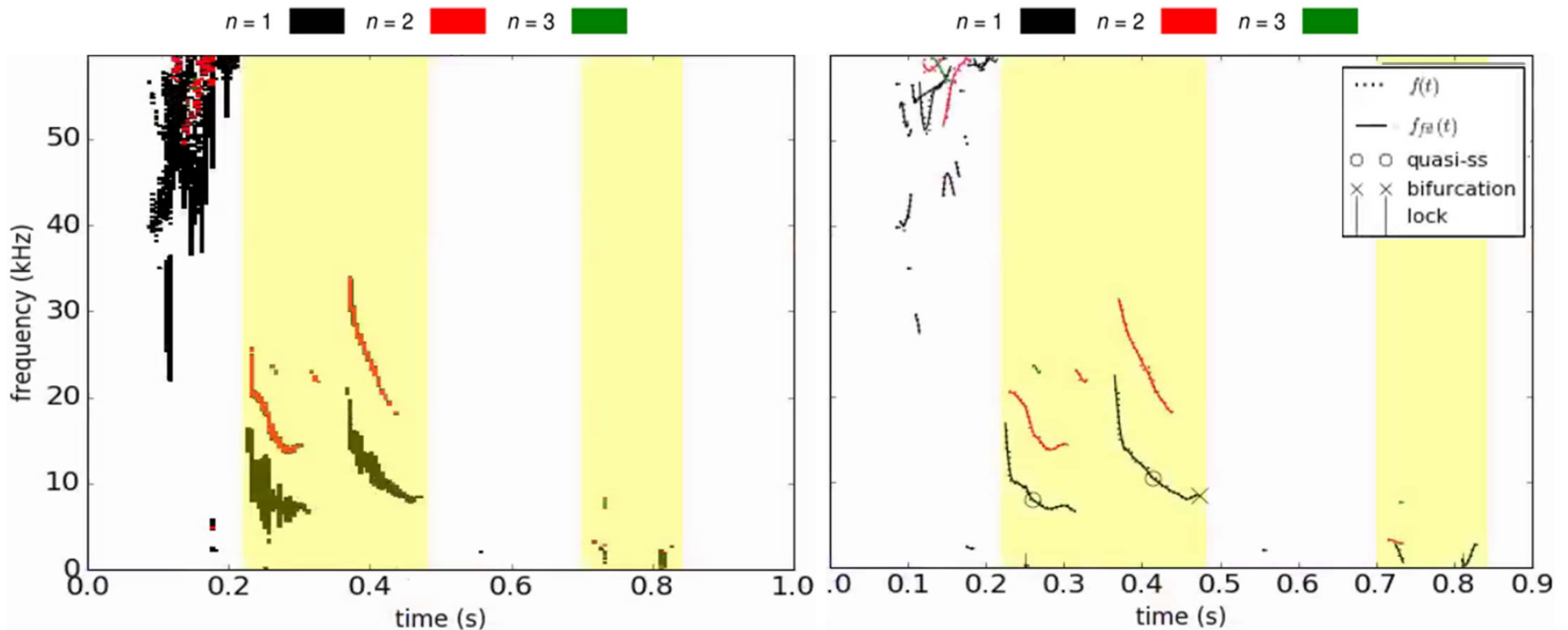


□ Rising warning level to disruption

shot 130190

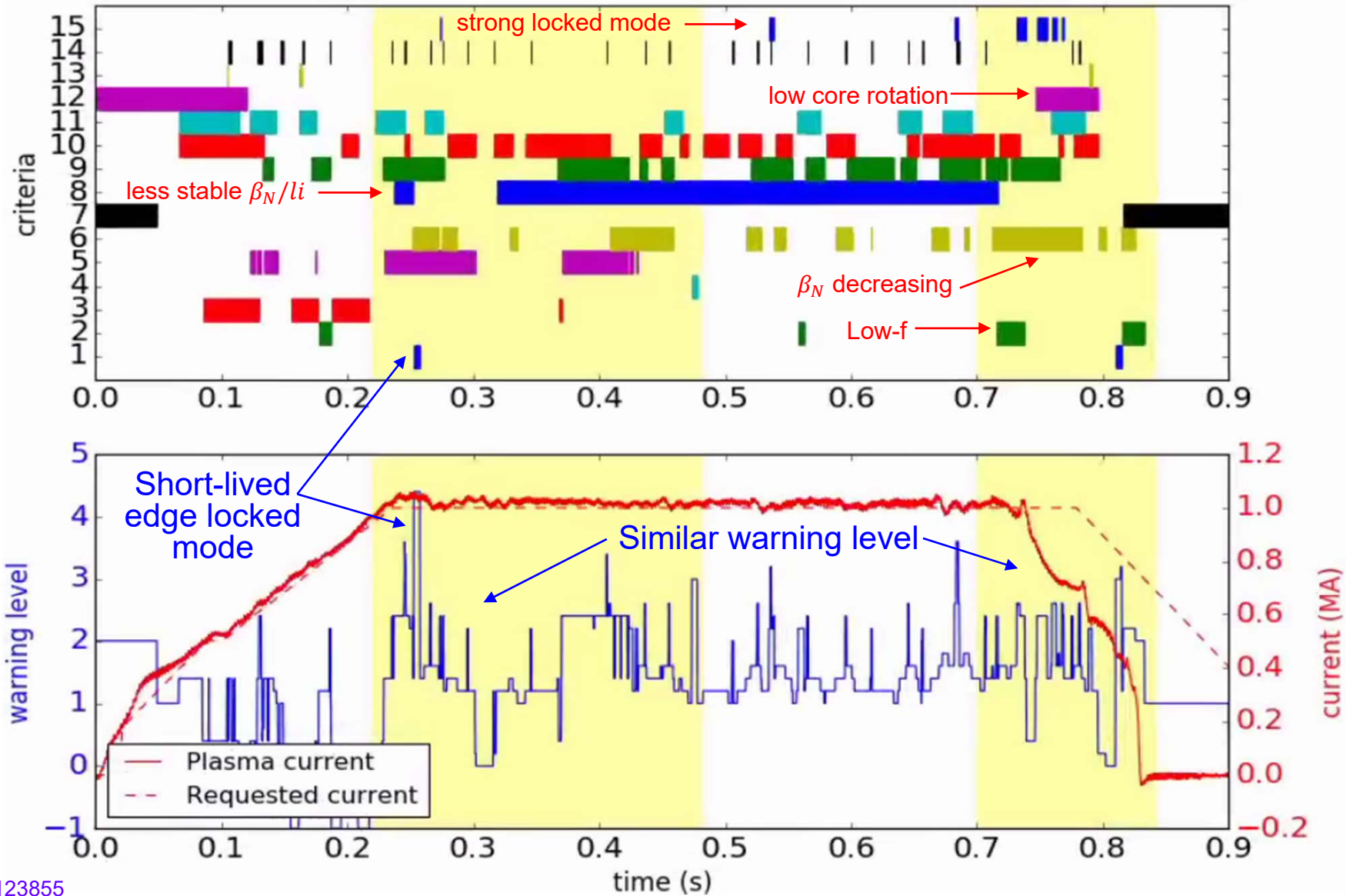
## Example 4: Rotating MHD modes disappear and plasma disrupts

- ❑ The spectrogram follow a similar pattern for locked mode predominant shots
  - ❑ Rotating MHD modes disappear after startup
  - ❑ Very low-f mode activity near disruption



shot 123855

# Example 4: Rotating MHD event warning levels correctly miss locked mode induced disruption



shot 123855



# New automated identification of rotating MHD modes in DECAF is showing good success for disruption forecasting

## □ Summary

- Developed a tool for analysis of rotating MHD mode activity in a tokamak plasma
- Used the tool to generate preliminary criteria for determining disruption warning levels. Tested in a variety of cases.

## □ Next steps

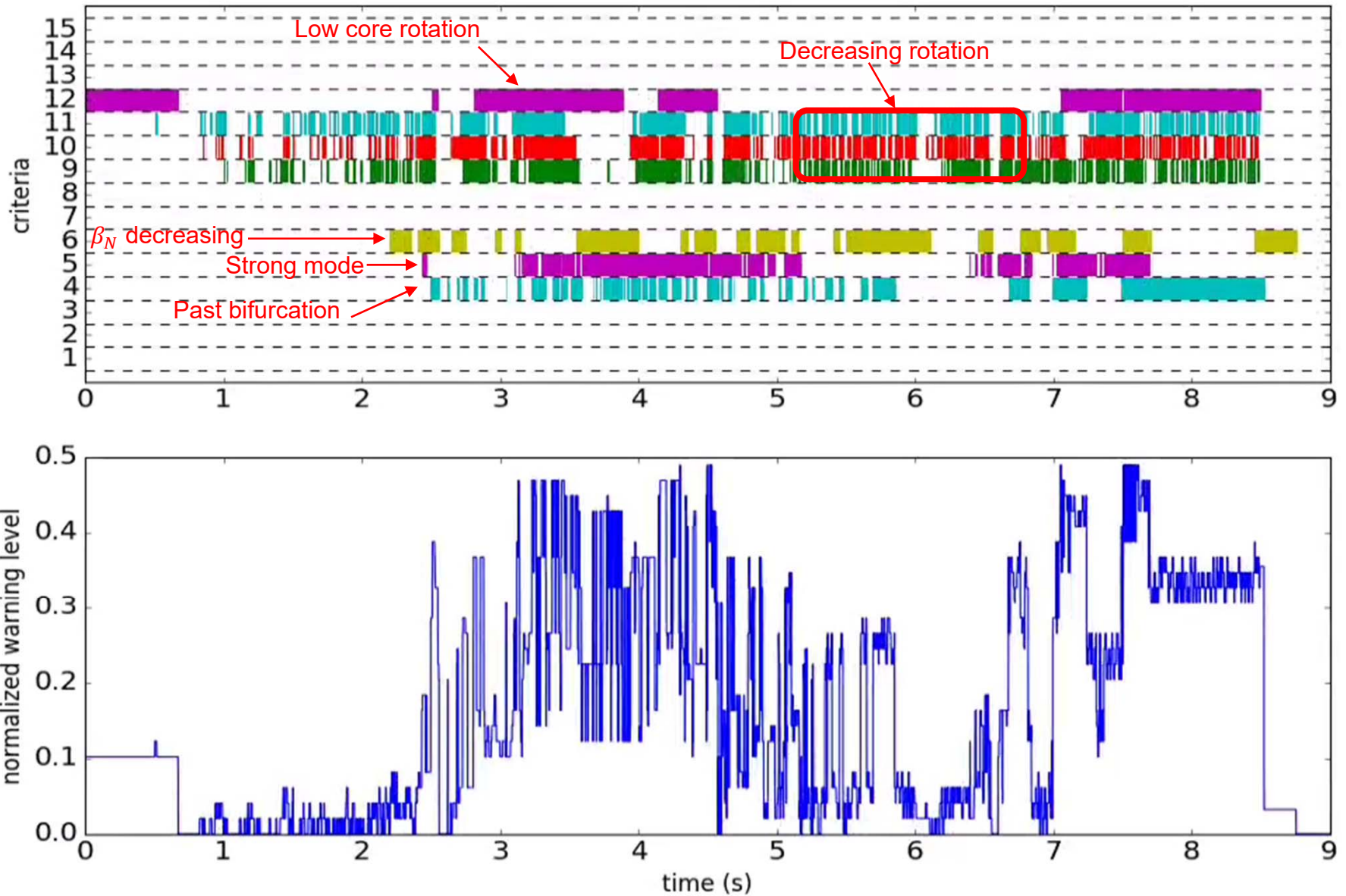
- Improve the identification of the bifurcation event with known physics models
- Optimize the rotating MHD analysis parameters for improved identification of the mode
- Couple the rotating MHD event to other events in DECAF (e.g. reduced RWM model)
- Improve the definition, and optimize the logic and weights of the criteria for improved disruption forecasting

**Thank you for listening**

**Any Questions?**

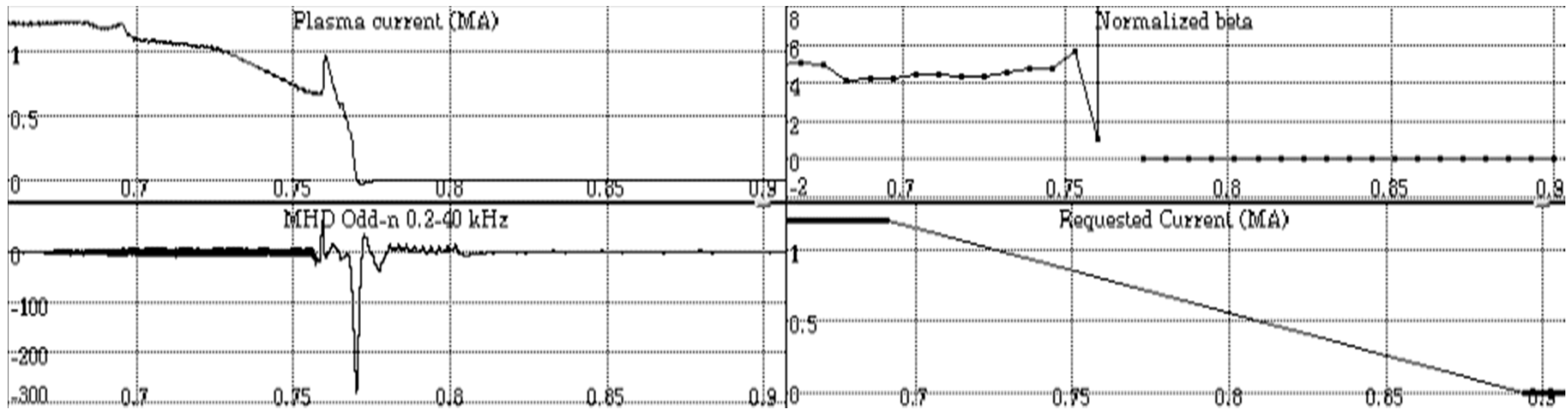
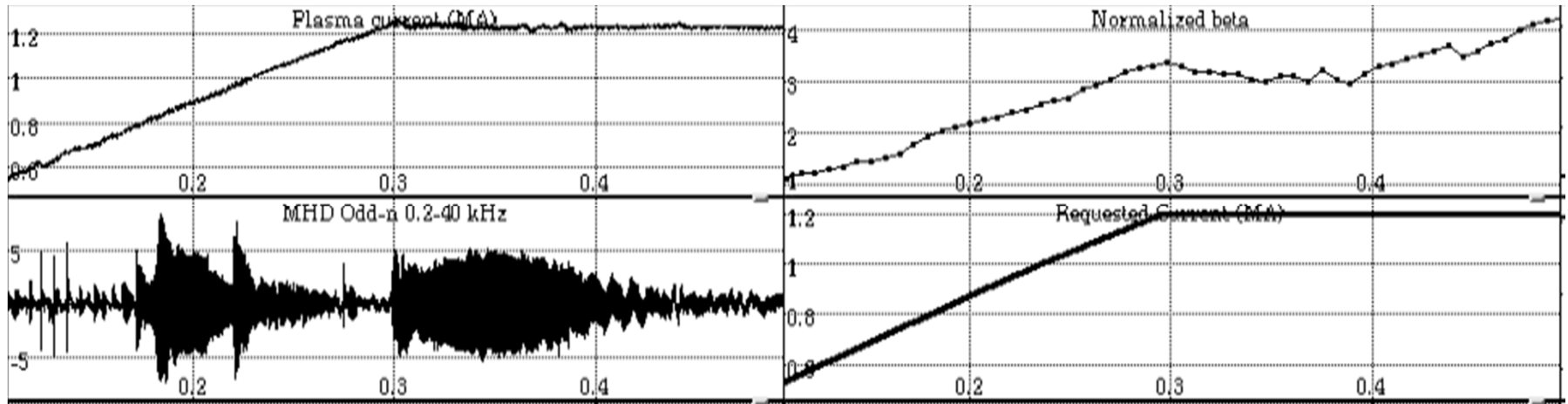
# BACKUPS

# KSTAR

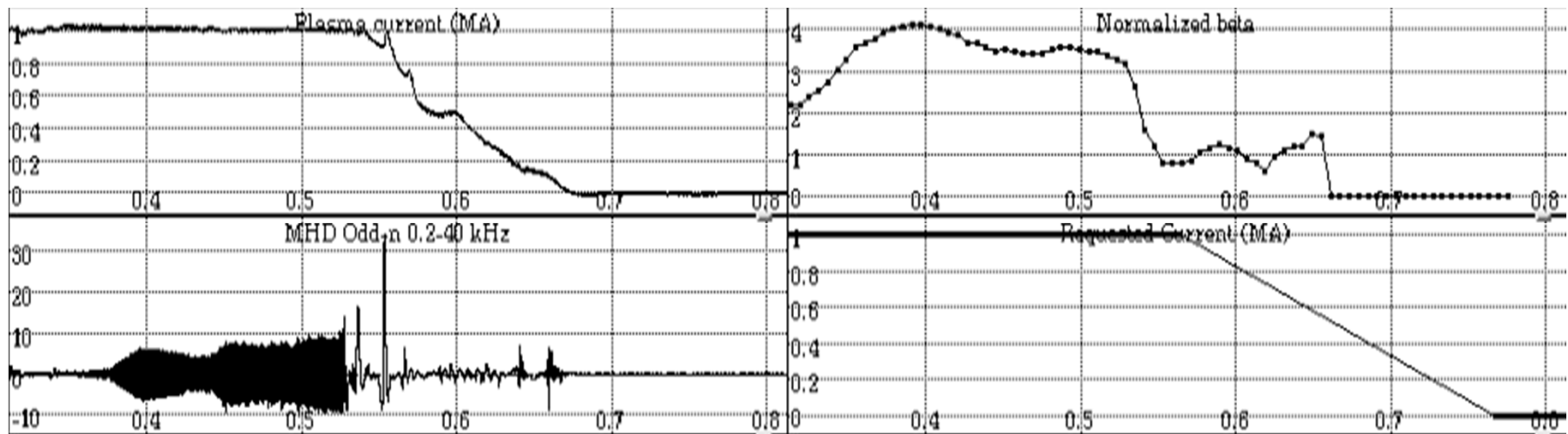
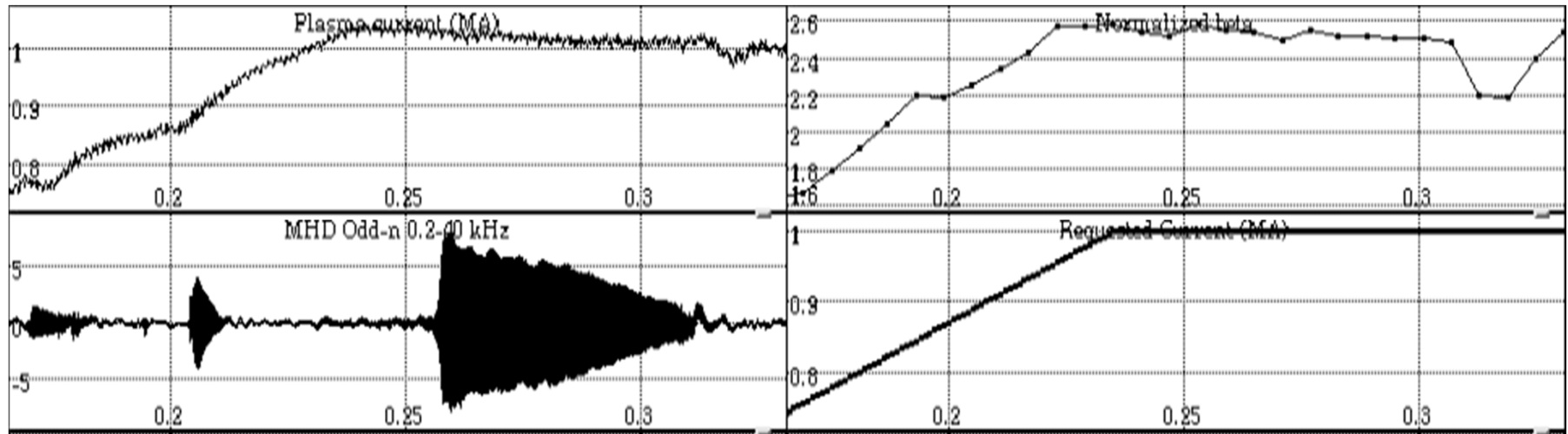




# Shot 138854



# Shot 126963

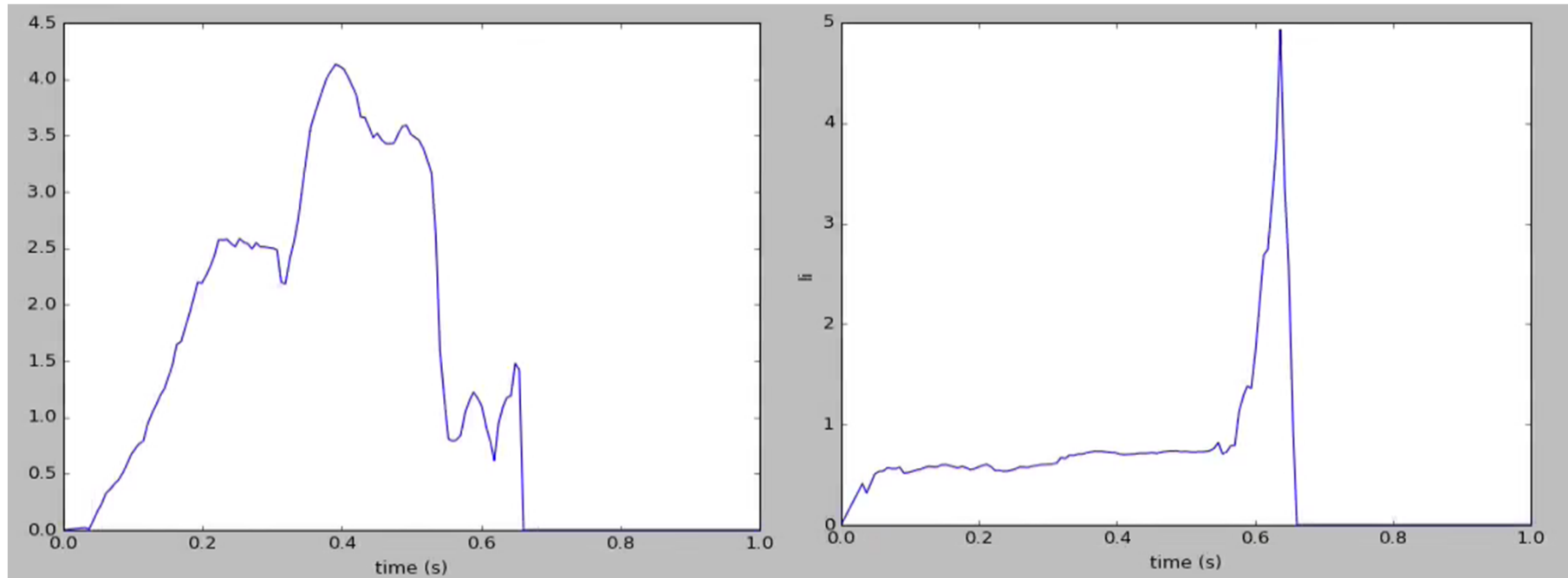


# Shot 126963

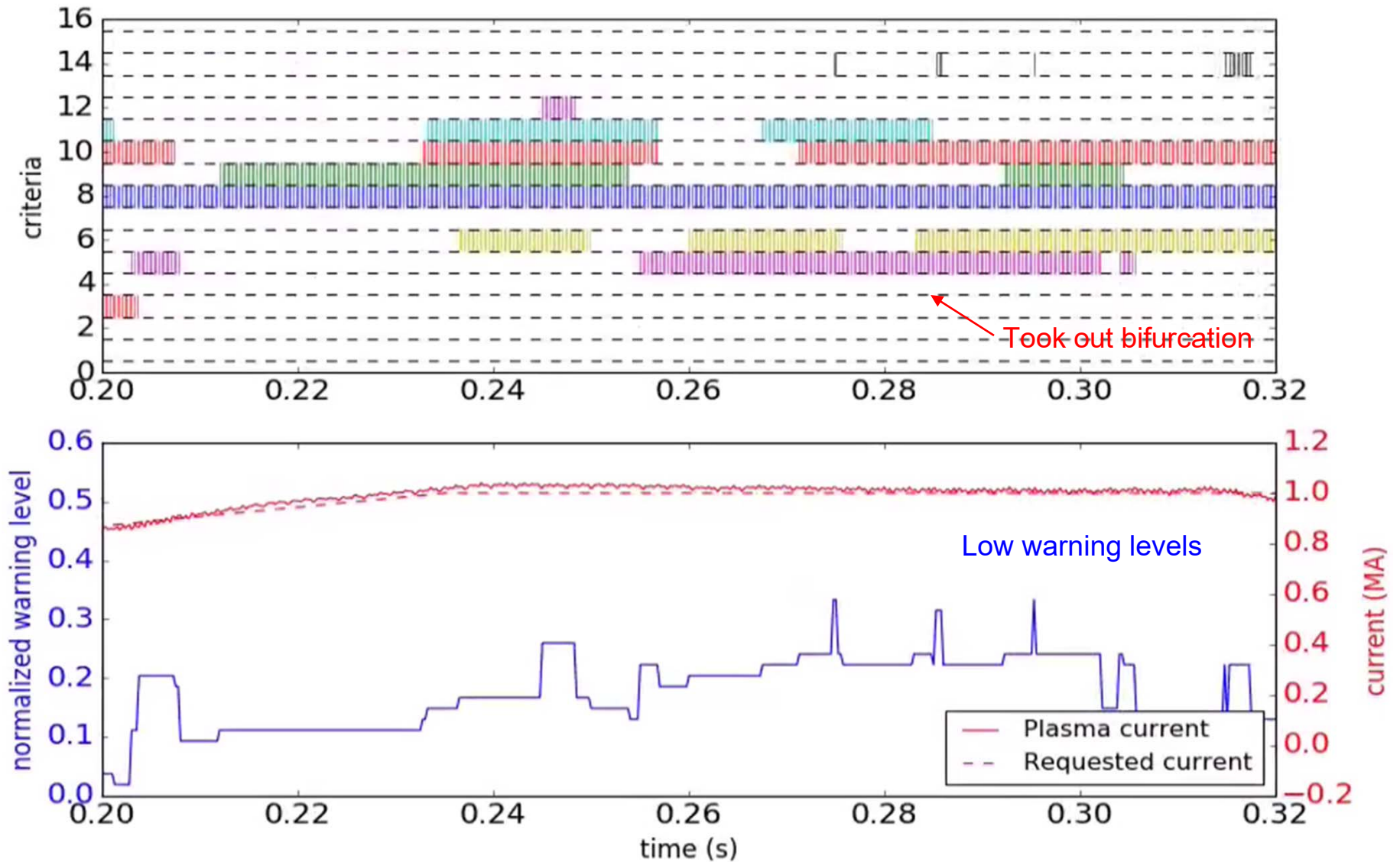
- Low betaN shot with increasing li (betaN/li outside of stable range)

$\beta_N$

$li$

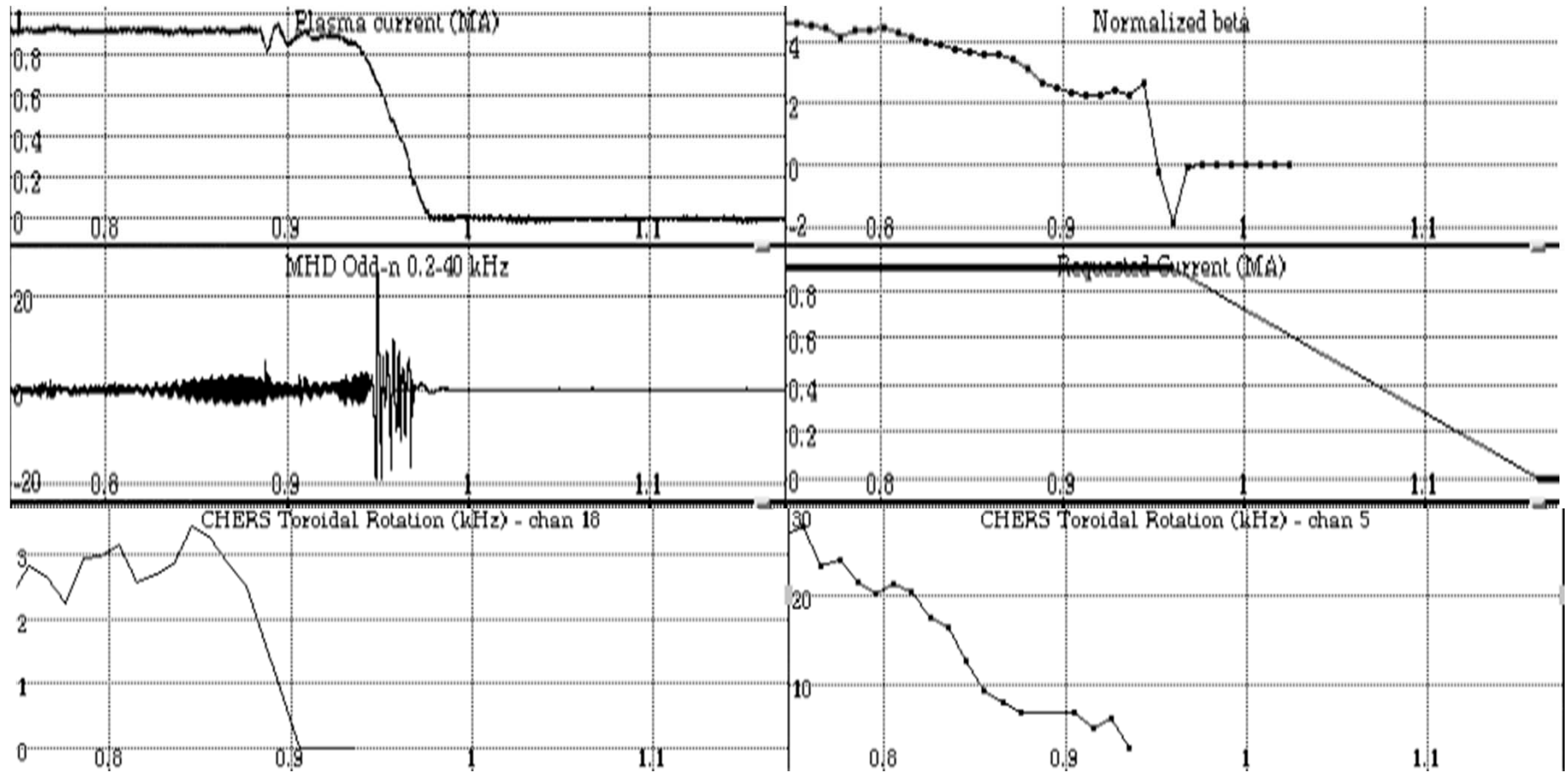


# Shot 126963

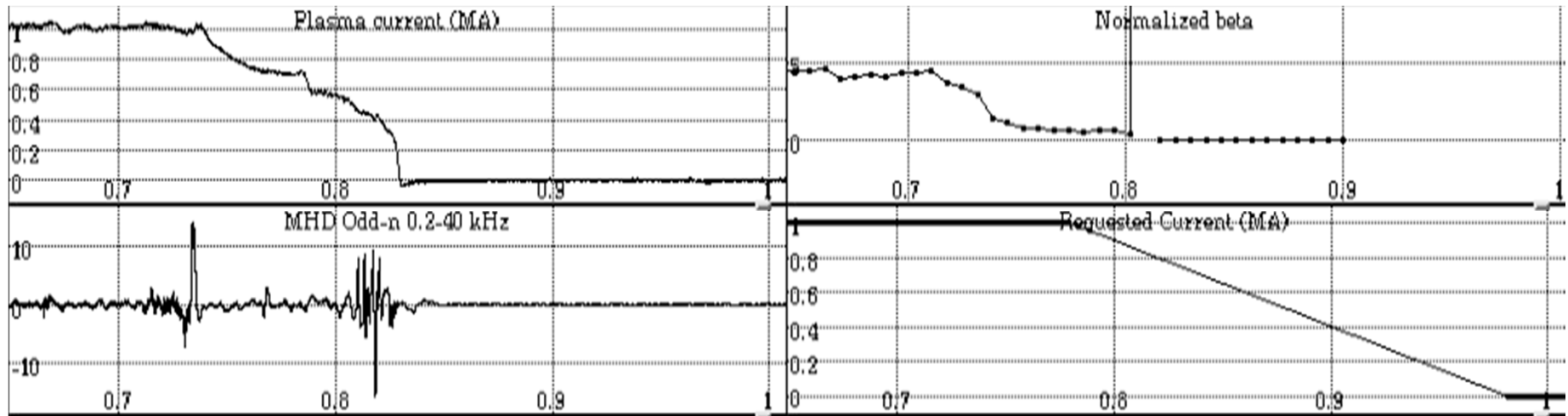
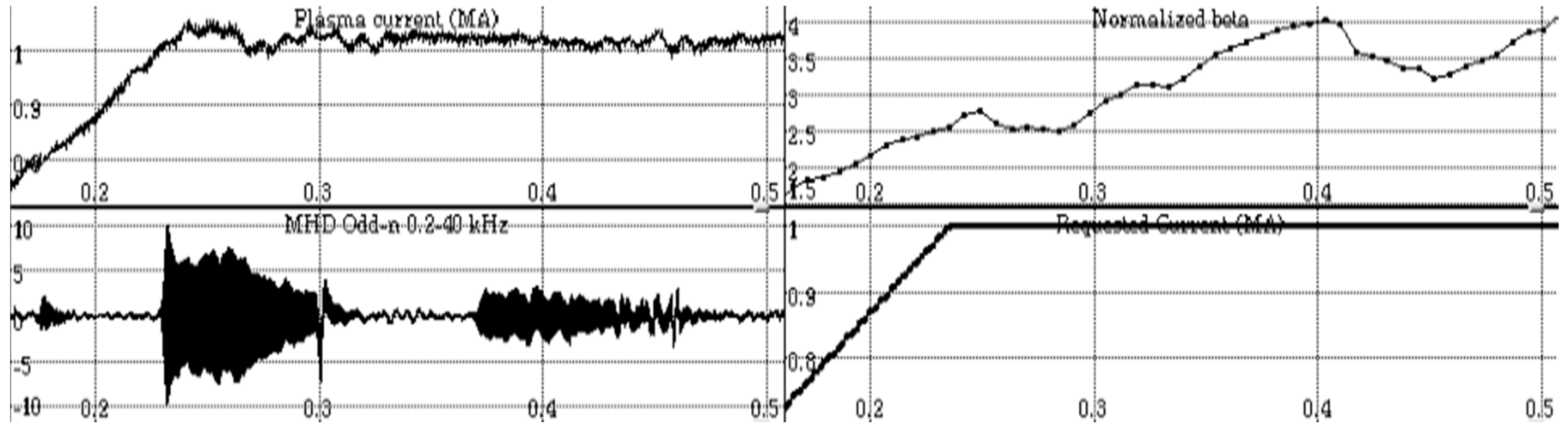




# Shot 130190



# Shot 123855



## Torque balance of plasma rotation shows frequency bifurcation due to mode drag

- The drive torque  $T_{aux}$  from neutral beam injection
- The drag torque from plasma viscosity is expected to be negative and proportional to the angular speed of the plasma (like friction):

$$T_{2D} = -\frac{(I\Omega)}{\tau_{2D}}$$

- The EM drag torque is more complicated and depends on whether the plasma slips with respect to the magnetic flux
- “No slip”:
- “Slips”:

$$T_{mode} = -\frac{k_1}{\Omega}$$

$$T_{mode} = -k_1\Omega$$

- $k_1$  is proportional to the island width of TM

# The model using a “no slip” condition has no steady state solutions at a large enough island width ( $k_1$ )

□ For steady state

solutions:  $\left(\frac{d(I\Omega)}{dt} = 0\right)$

□  $k_1 = 0$  : “red curve”

□ No mode present

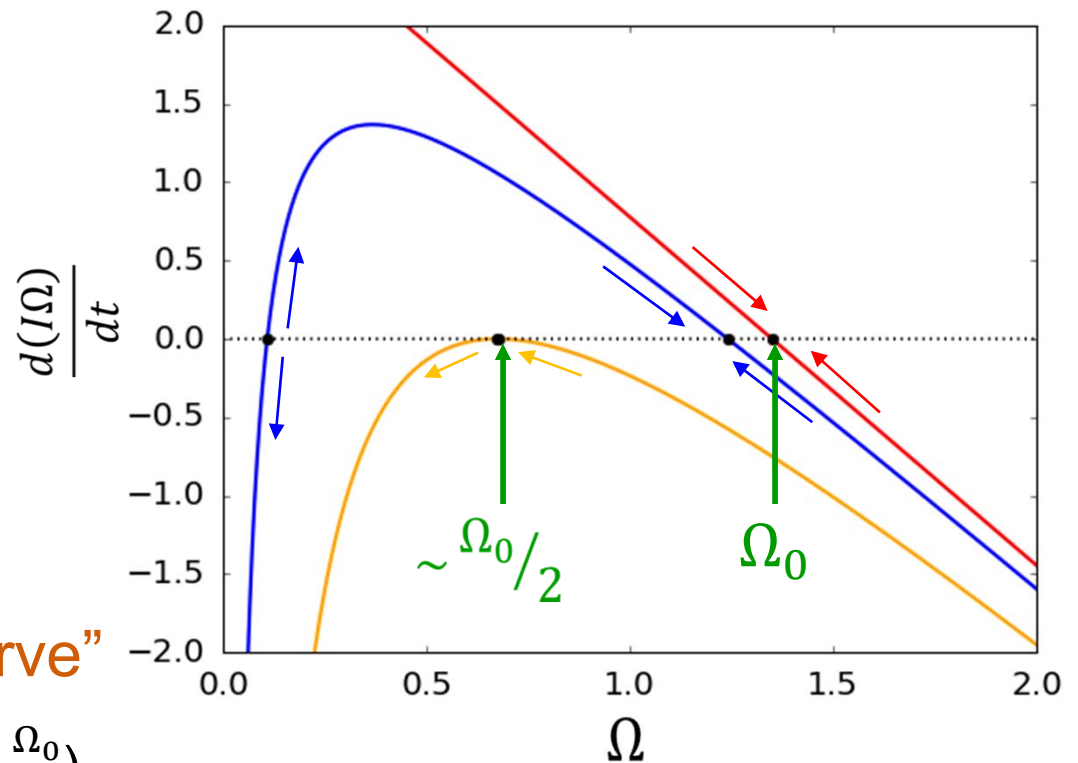
□  $k_1 < \frac{T_{aux}^2 \tau_{2D}}{4I}$  : “blue curve”

□ Two steady state solution

□  $k_1 = \frac{T_{aux}^2 \tau_{2D}}{4I}$  : “orange curve”

□ One steady state solution ( $\sim \frac{\Omega_0}{2}$ )

$$\frac{d(I\Omega)}{dt} = T_{aux} - \frac{k_1}{\Omega} - \frac{(I\Omega)}{\tau_{2D}}$$

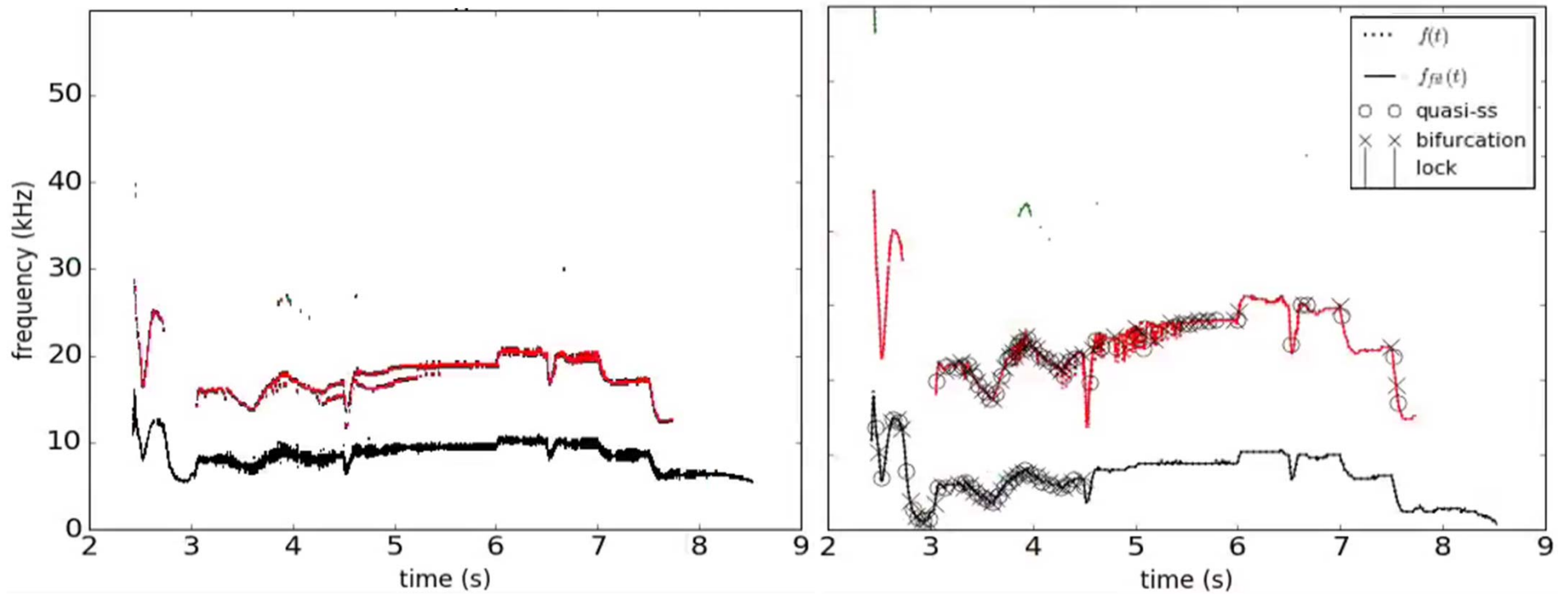


□ Bifurcation

• At close to half the steady state natural rotation frequency ( $\Omega_0$ )



# KSTAR



## Outline (~25 slides)

- ❑ Introduction (2)
- ❑ Algorithm description (5)
- ❑ Criteria description (4)
- ❑ Results (10)
  - ❑ NSTX (5)
    - Case 1
    - Case 2
    - Case 3
  - ❑ KSTAR (5)
    - Case 1
    - Case 2
    - Case 3
- ❑ Concl. & next steps (larger database, more machines, bifurcation) (2)