

Runaway Generation in a Tokamak Plasma

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Outline

- Runaway generation processes in the presence of large inductive electric fields in axisymmetric geometry
 - Four dimensional reconstruction of the Runaway Probability Function (RPF)
- Two example cases:
 - Dreicer production
 - Avalanche amplification
- Self-Consistent runaway formation in an axisymmetric plasma
 - Runaway formation during the current quench

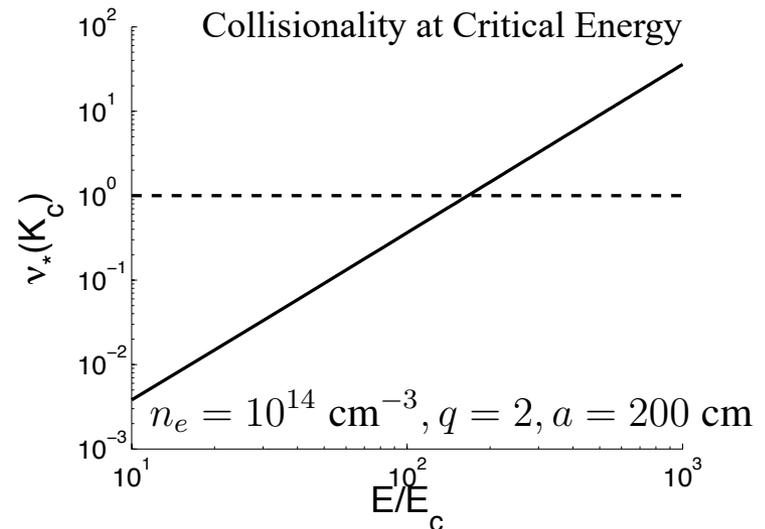
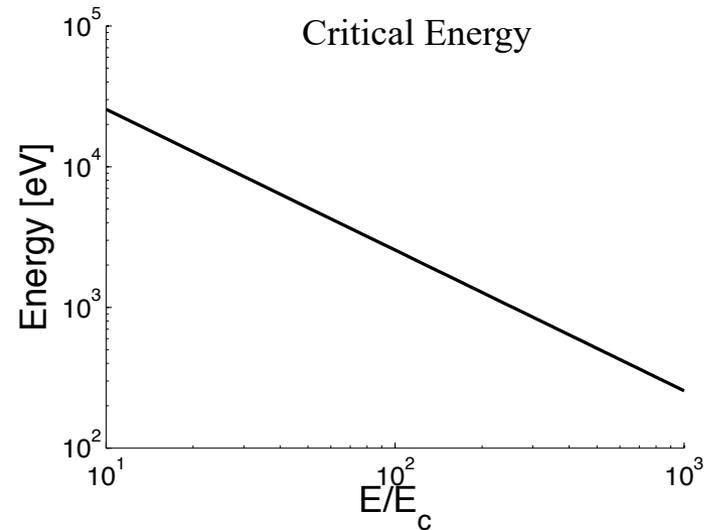
Motivation: Runaway Generation Processes in Tokamak Plasmas for Large Inductive Electric Fields

- Our intuition of how toroidal geometry impacts runaway generation is largely based on electron trapping
 - Implies a reduction of runaway generation as the minor radius is increased [**Rosenbluth-Putvinski 1997**]

- The critical energy for an electron to run away in a hydrogen plasma can be approximated by:

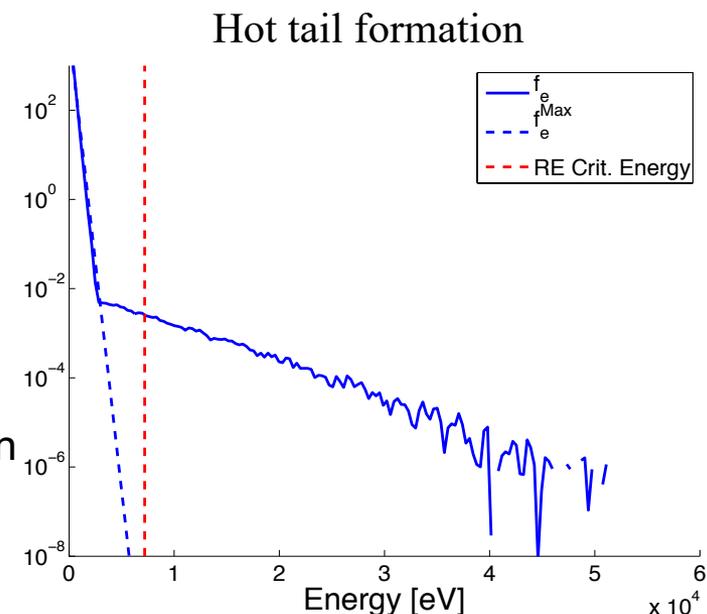
$$\mathcal{K}_c \approx \left(\frac{m_e c^2}{2} \right) \left(\frac{E_c}{E} \right)$$

- For large electric fields this energy can be several hundred eV
 - **Electrons at these modest energies are often characterized by $\nu_* \gg 1$**

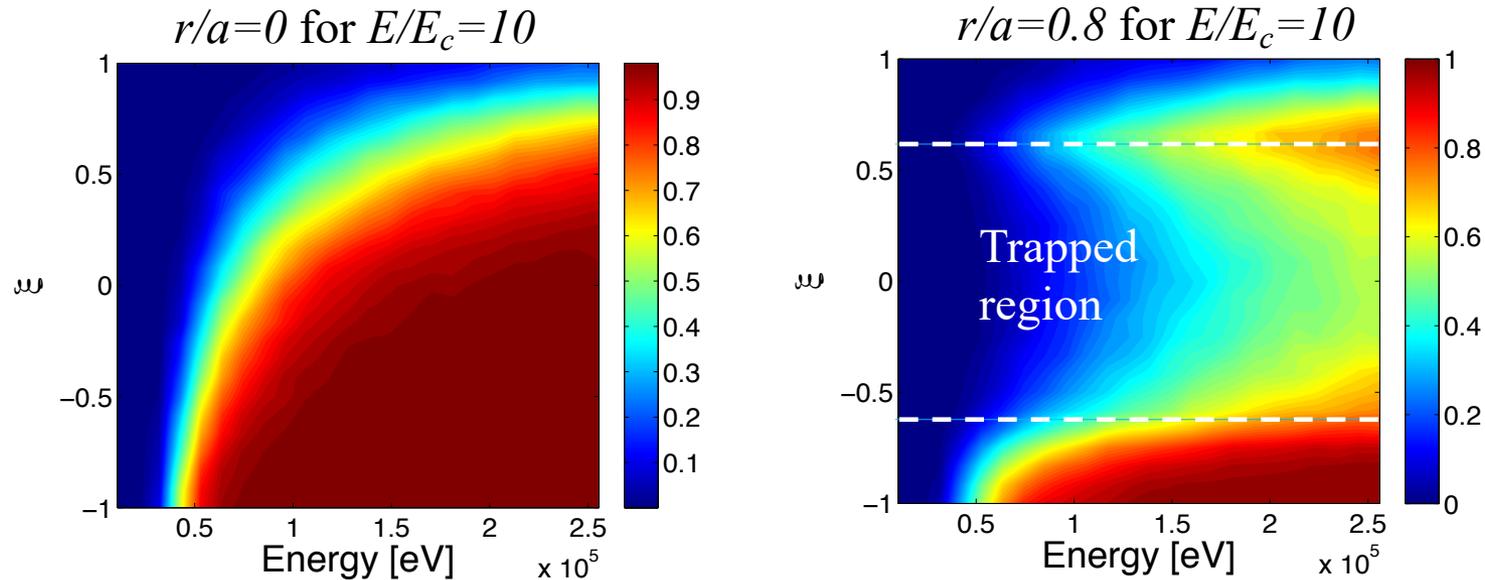


Drift Kinetic Description of Runaway Electrons

- Particle based guiding-center solver for 3D-2V runaway electron population [McDevitt et al. 2019] → does not require asymptotically small collisionality
 - Large-angle collisions described by a Möller source
 - Seed mechanisms (hot tail and Dreicer) incorporated via a variable weight scheme
 - Flux-surface averaged inductive electric field can be evolved self-consistently
- Provides high physics fidelity description of:
 - Runaway seed formation
 - Avalanche amplification of initial seed population
 - Self-consistent evolution of flux-surface averaged inductive electric field

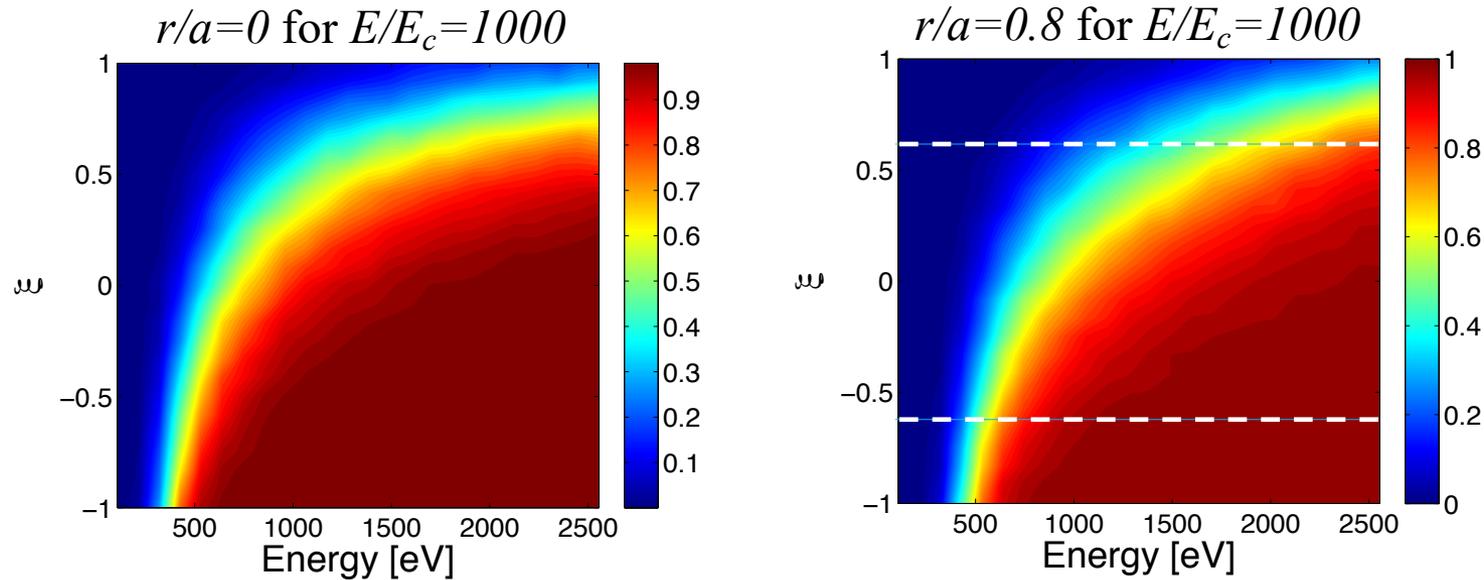


Runaway Probability Function in Toroidal Geometry: Weak Inductive Electric Field



- Interesting to contrast the runaway probability function (RPF) [Liu et al. 2016, Zhang et al. 2017] for $r/a=0$ and $r/a=0.8$
 - Radiation neglected here \rightarrow electrons accelerated to arbitrarily high energy are deemed runaways
 - Electrons that reach the thermal energy are deemed to not run away
- The RPF exhibits a strong local minimum at $\xi = 0$ for the off-axis case
 - Significantly reduces the efficiency of runaway generation at large minor radius

Runaway Probability Function in Toroidal Geometry: Strong Inductive Electric Field

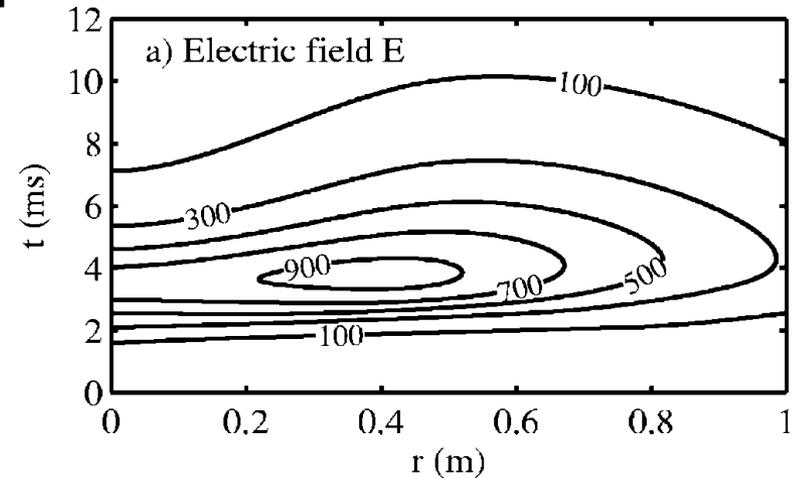


- For strong inductive electric fields, off-axis RPF no longer strongly reduced in “trapped” region
 - The large collisionality near the critical energy to run away prevents electrons from completing a bounce orbit
 - Impact of electron trapping is largely negated

Inductive Electric Field During a Tokamak Disruption

- The characteristic strength of the inductive electric field can be estimated based on the available poloidal flux [Boozer 2018]
- An ITER-like case with $75 \text{ V} \cdot \text{s}$ of poloidal flux and a 100 ms current decay implies an average loop voltage of 750 V
 - This implies $E/E_c \approx 380$ for $n_e = 10^{14} \text{ cm}^{-3}$, $T_e = 10 \text{ eV}$, and $\ln \Lambda = 10$
- Maximum inductive electric field generally much larger

JET-like case
[Smith et al. 2006]

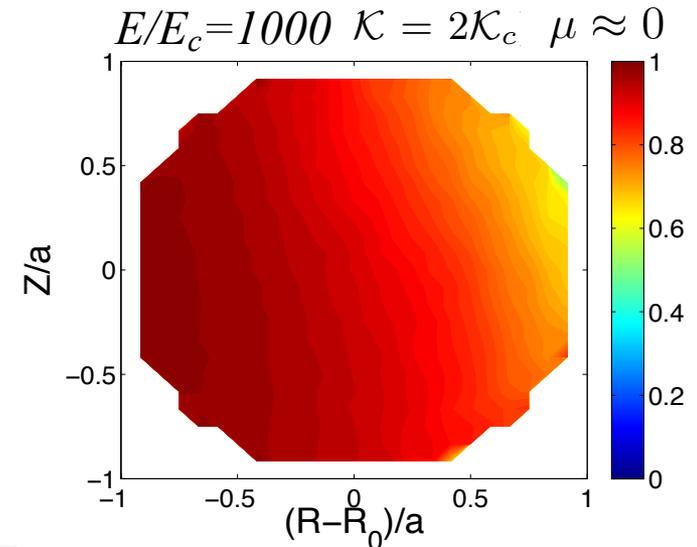
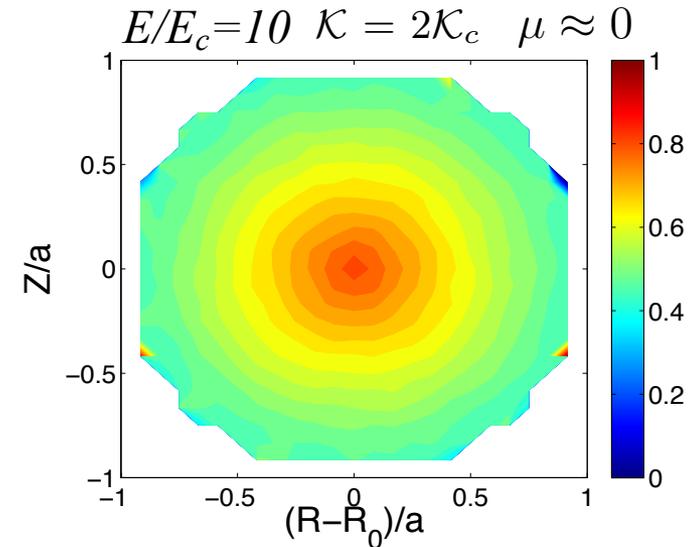


Runaway Electron Generation is Strongly Localized for Large Electric Fields

- For a large inductive electric field electrons can gain a significant amount of energy in a single toroidal transit
- Specifically, for an ITER-like case with an average loop voltage of 750 V
 - An electron can gain up to 750 eV during a single toroidal transit
 - The critical energy at this electric field is 670 eV
 - Electrons can more than double their energy in a single toroidal transit
 - For $q \gtrsim 1$, electrons can be accelerated before sampling the entire flux surface
- The inductive electric field in tokamak geometry scales as $1/R$
 - Implies strong poloidal localization of runaway generation for large inductive electric fields

Runaway Probability Function in Configuration Space

- In the low collisionality limit and a modest inductive electric field $f_e = f_e(\gamma, \mu, \psi)$
- For large inductive electric fields the RPF is no longer a flux surface function $\Leftrightarrow (\gamma, \mu, R, Z)$
 - The strong in-out asymmetry results from $E_\varphi \propto 1/R$
 - A weaker up-down asymmetry results from helicity of magnetic field line
- RPF substantially increased across poloidal cross section for large inductive electric field
 - Significant increase in efficiency of all runaway generation processes



Parallel Electric Field in Axisymmetric Tokamak Geometry

- Incompressibility $\nabla \cdot \mathbf{j} = 0$, but $\nabla \cdot \mathbf{j}_\perp \neq 0$ implies [Helander-Sigmar]

$$j_{\parallel} = -\frac{I(\psi)}{B} \frac{dp}{d\psi} + K(\psi) B$$

- For a low-beta poloidal plasma, $j_{\parallel}/B \approx K(\psi) \Leftarrow$ Flux surface function
- From Ohm's law

$$E_{\parallel} = \eta j_{\parallel} = \eta B \left(\frac{j_{\parallel}}{B} \right) \approx \eta B K(\psi)$$

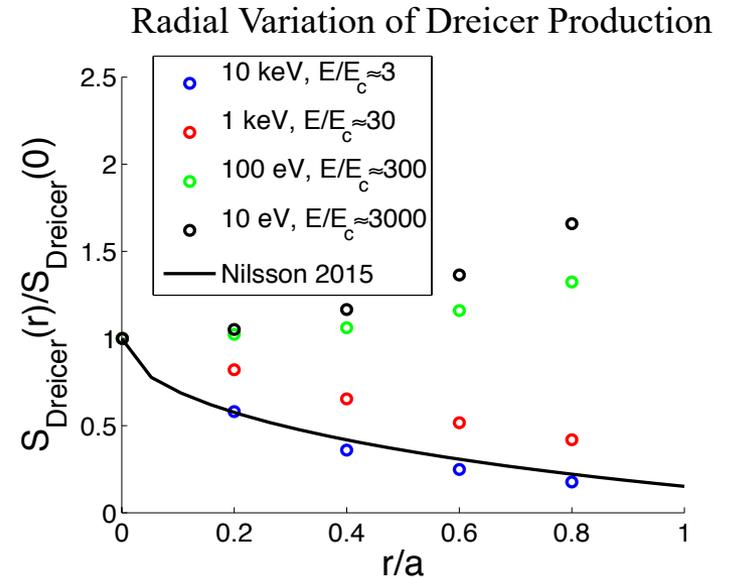
- In simplest limit $\eta = \eta(Z_{eff}, T_e) = \eta(\psi)$, $E_{\parallel} \propto B \propto 1/R$
- More complex cases possible for poloidally and toroidally localized impurity deposition \Leftrightarrow treat in future work

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Dreicer Production in Tokamak Geometry

- Considering Dreicer production as a function of electric field strength
 - E/E_D held constant while the temperature is scanned
 - Noting $E/E_c = (m_e c^2 / T_e) (E/E_D) \Leftrightarrow$ results in the strength of electric field being varied
- For modest values of the inductive electric field (high temperature) the results from Nilsson et al. 2015 are reproduced

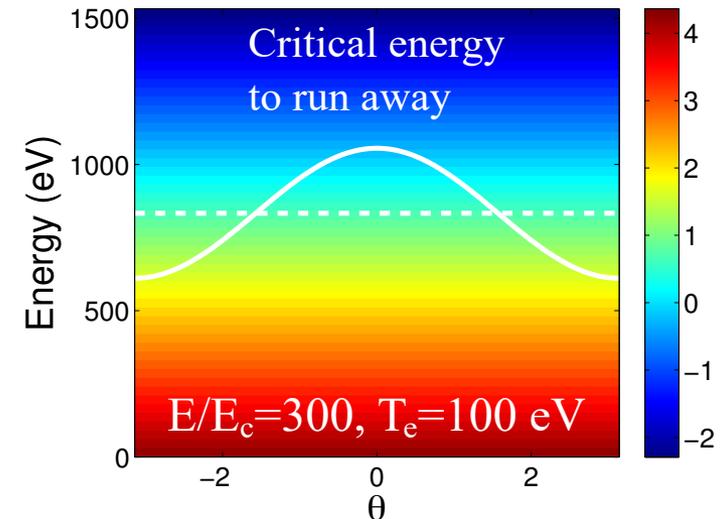
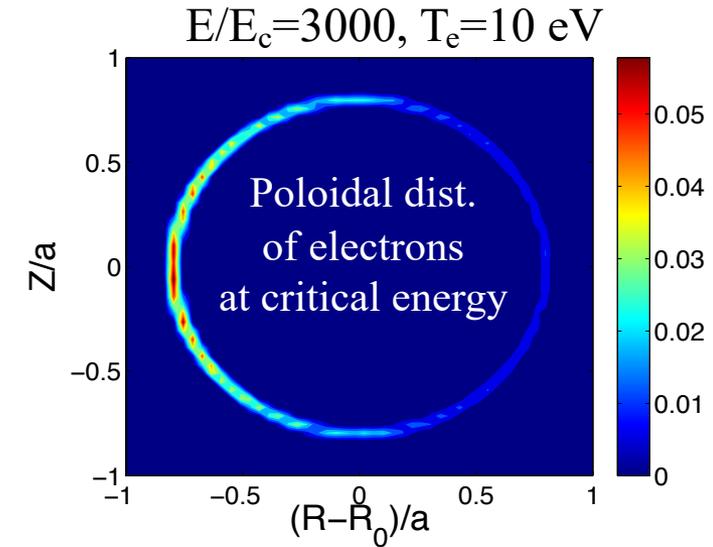


$$E/E_D = 0.06, n_e = 2 \times 10^{14} \text{ cm}^{-3}, Z_{eff} = 1$$

- For large inductive electric fields (low temperature) the present results deviate qualitatively from previous predictions
 - Dreicer production more efficient at larger minor radii

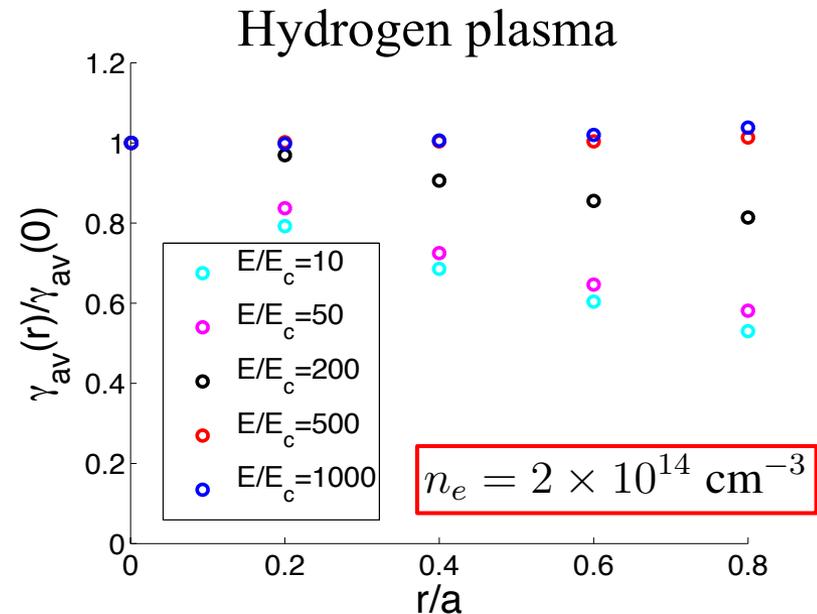
Runaway Distribution near Threshold Energy Strongly Asymmetric

- Noting the modulation of inductive electric field $E_\varphi \propto 1/R$
 - Runaway electrons more efficiently accelerated on inboard side
 - Less efficiently on outboard side
- Poloidal modulation does not cancel:
 - Dreicer production depends non-linearly on the electric field strength

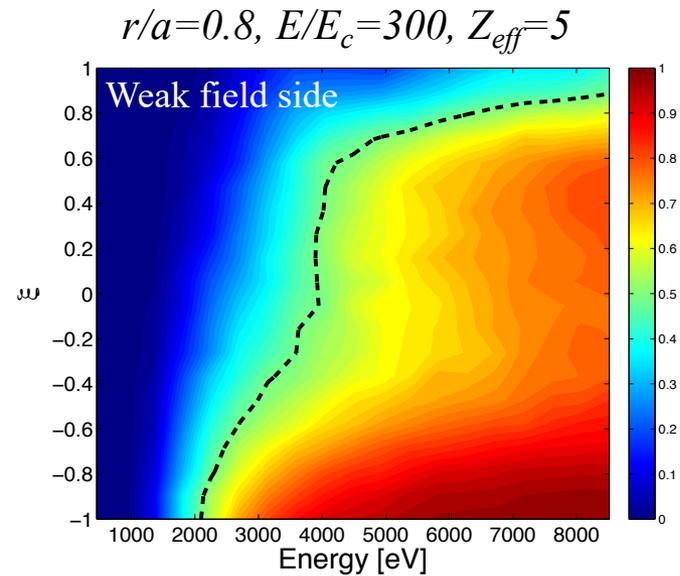
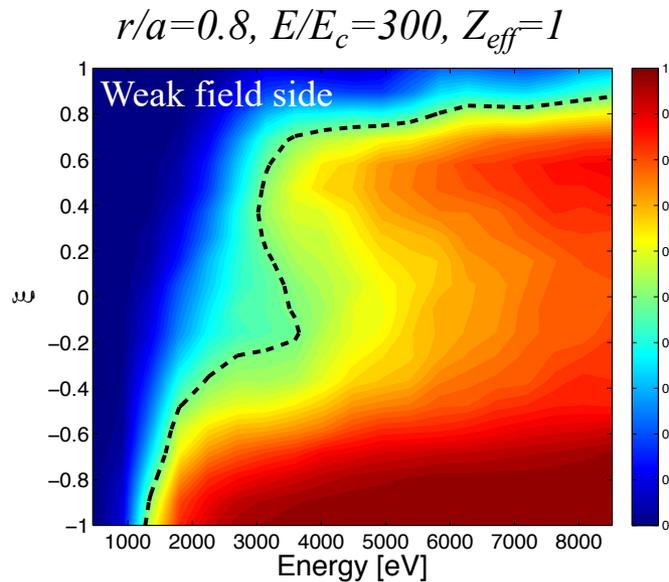


Avalanche Amplification for Large Electric Fields

- Related physics impacts avalanche amplification
- High collisionality at critical energy negates “neoclassical” reduction factor
- However, the avalanche growth rate is (approximately) linear with respect to the electric field:
 - $1/R$ modulation of inductive electric field will (nearly) cancel
 - Little to no increase expected at large minor radii for asymptotically large electric fields



Impact of Impurities on Runaway Probability Function

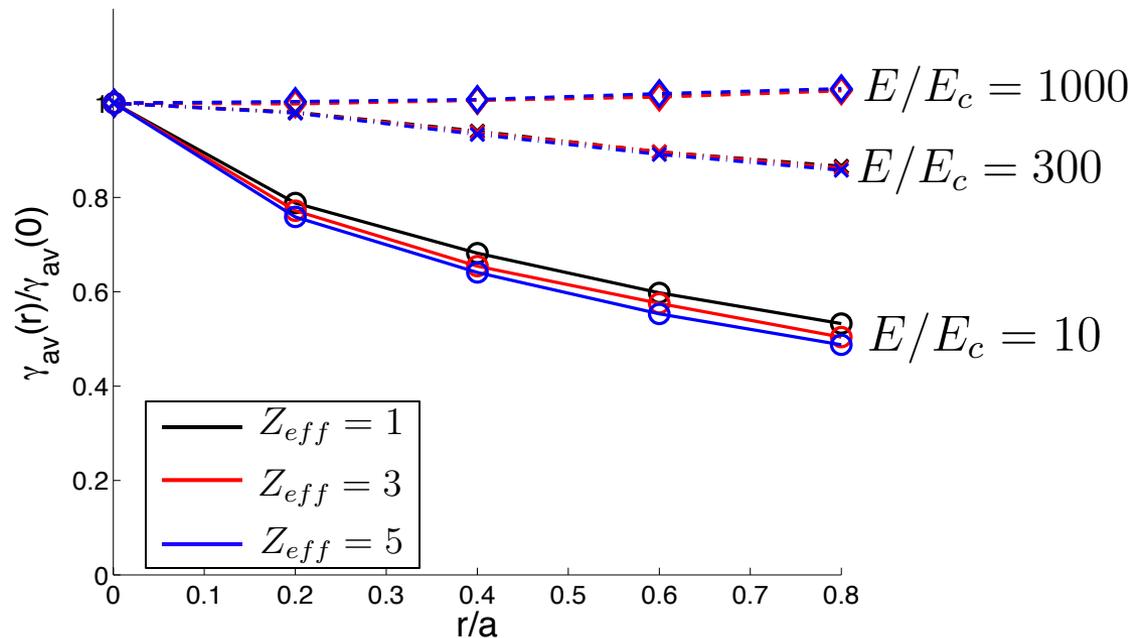


- Presence of impurities modifies the collisionality via two partially compensating trends

$$\nu_* \equiv \frac{\tau_{bounce}}{\tau_{detrap}} \propto n_e (Z_{eff} + 1) \left(\frac{c}{v}\right)^4$$

- Critical energy to runaway increased
- Pitch-angle scattering more efficient at a given energy

Impact of Impurities on Avalanche Amplification



- Presence of impurities only modestly impact radial modulation of avalanche amplification factor
 - Amplification factor reduced as radius is increased for small E/E_c
 - Amplification factor approximately constant for large E/E_c

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Runaway Electron Formation: Axisymmetric Plasma

- Interested in identifying the impact of the above physics on RE formation in an axisymmetric tokamak plasma
- Seek testbed for exploring coupling of RE to field evolution
- Incorporate accurate description of RE dynamics:
 - RE generation processes in toroidal geometry for arbitrary collisionality regimes
 - Spatial transport of RE for plasmas with large impurity content [McDevitt et al. 2019]
 - Finite orbit width effects
 - ...
- Allows for spatial profile of RE current to be determined
 - MHD stability of RE current carrying plasma

RE Generation during Current Quench

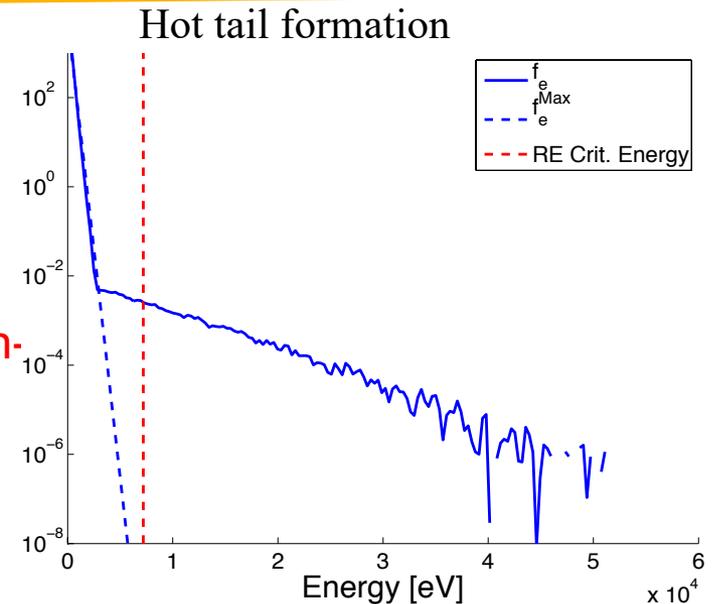
- Will evolve flux surface averaged induction equation

$$\nabla^2 \mathbf{E} = \mu_0 \frac{\partial \mathbf{j}}{\partial t}$$

- Along with a modified Ohm's law [Rosenbluth-Putvinski 1997]:

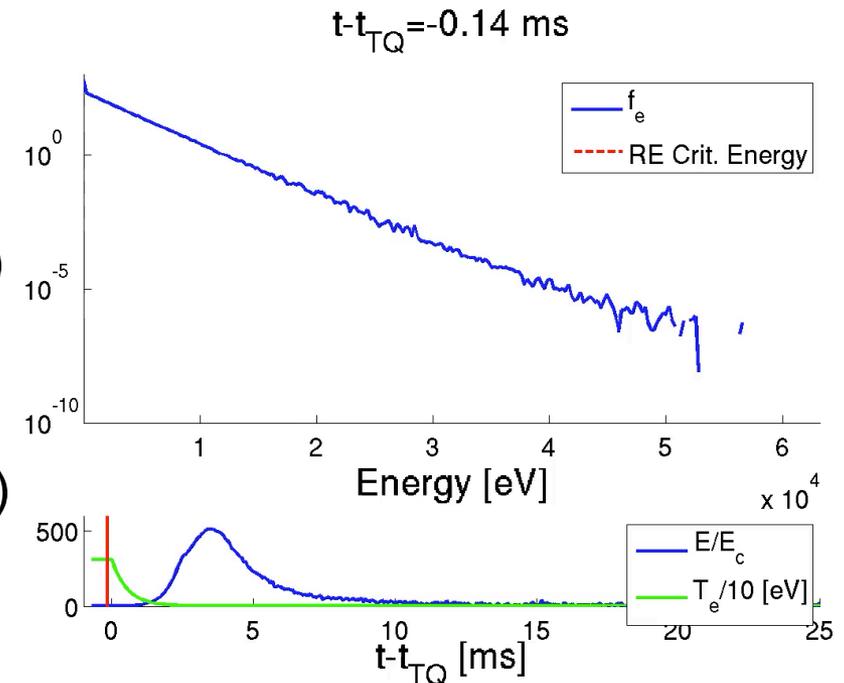
$$E_{\parallel} = \eta (j_{\parallel} - j_{RA})$$

- j_{RA} evaluated from kinetic solution
 - Density and temperature profiles prescribed
- Incorporating seed mechanisms requires resolving both the tail and bulk plasma non-perturbatively
 - Variable weight scheme employed to improve resolution of tail population: marker particles split as they are accelerated
 - Only tail electrons fed back into field solve $\Leftrightarrow j_{RA}$



Current Transfer

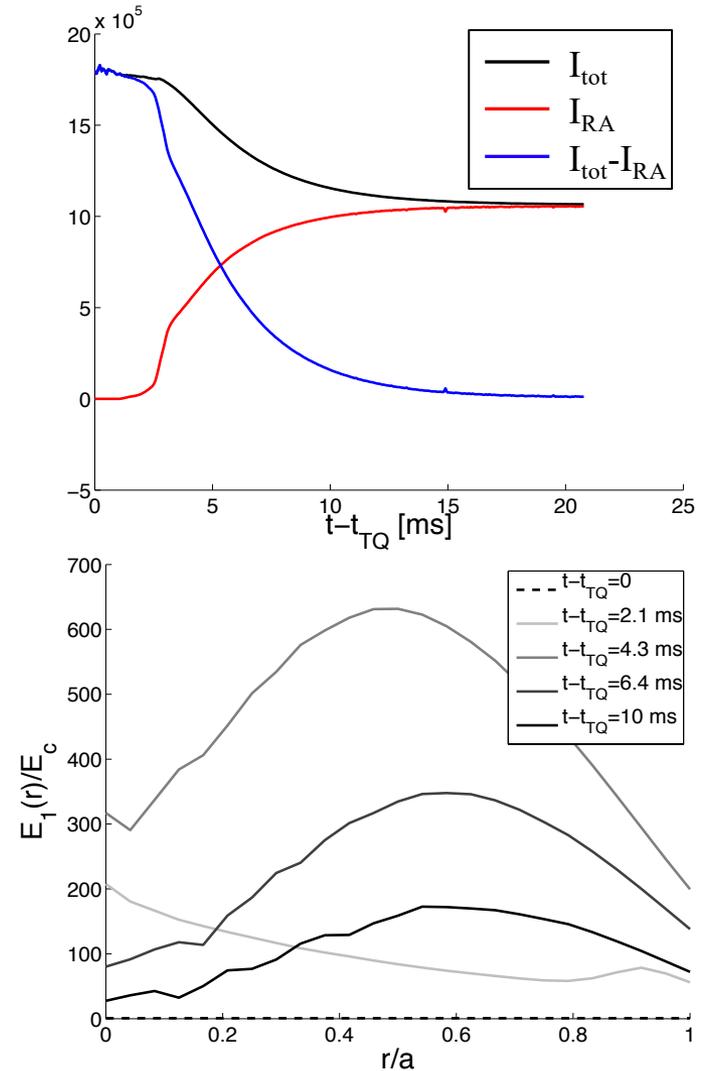
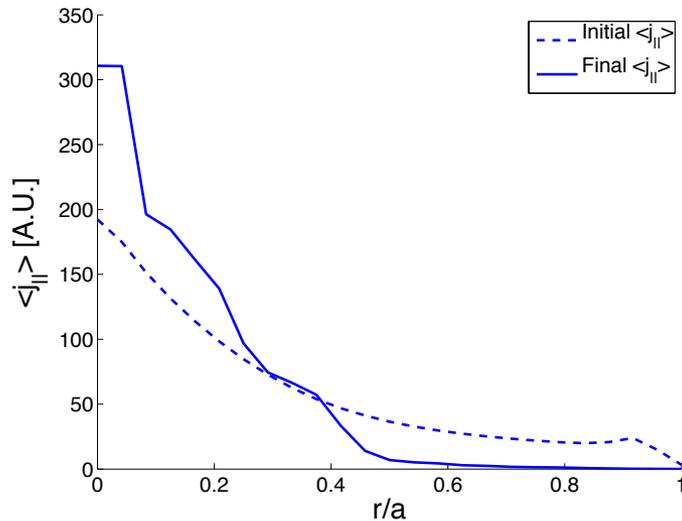
- Runaway generation occurs in three distinct phases
 - Hot tail generation:** $t-t_{TQ}=(1\text{ms}-2.3\text{ms})$
 - Strongly non-Maxwellian solution due to rapid thermal quench
 - Dreicer generation:** $t-t_{TQ}=(2.3\text{ms}-3\text{ms})$
 - Electric field directly accelerates electrons from thermal bulk
 - Avalanche amplification:** $t-t_{TQ}=(3\text{ms}-15\text{ms})$
 - Seed population amplified until RE's overtake plasma current



- Assume JET like shot with a thermal quench of $\tau_{TQ}=0.5\text{ ms}$
 - Hydrogen plasma assumed

Profile Evolution during Current Quench

- Current plateau forms on a timescale of 15 ms
- Once the runaway beam forms, electric field drops
 - Hollow E-field profile forms due to peaked RE current profile



Summary

- Runaway probability function found to have a non-trivial structure in the 4-D phase space (γ, μ, R, Z)
 - Runaway distribution function is not well approximated as a flux surface function near critical energy to run away
- The efficiency of runaway generation processes found to be strongly modified in the limit of large inductive electric fields
 - Dreicer production rate is found to be enhanced at finite minor radii
 - Avalanche amplification found to be approximately constant in radius
- Runaway generation coupled to a self-consistently evolving inductive electric field in tokamak geometry
 - Provides high physics fidelity description of 2D-2V runaway electron phase space evolution
 - Future work aimed at incorporating a self-consistent collisional radiative model