

The role of impurity transport and temperature in MGI induced runaway dynamics

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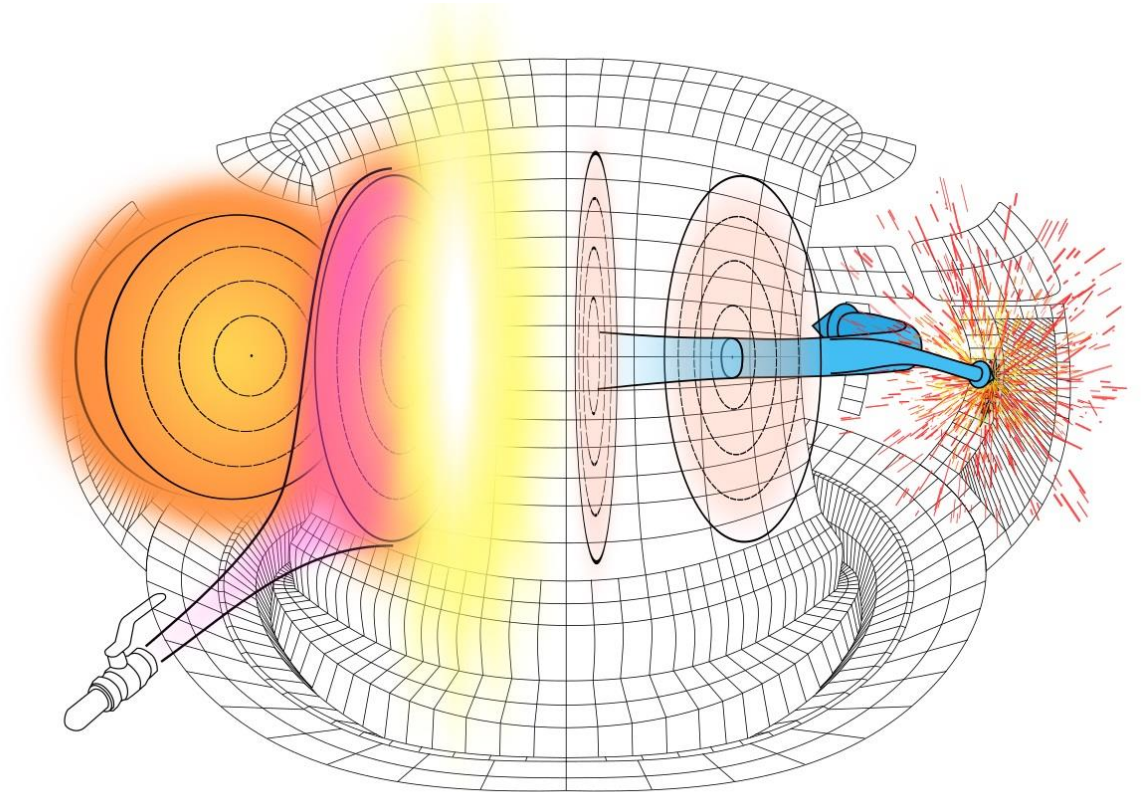
[†] See author list of H. Meyer et al. *Nucl. Fusion* **59**, 112014 (2019)

[‡] See author list of B. Labit et al. *Nucl. Fusion* **59**, 086020 (2019)

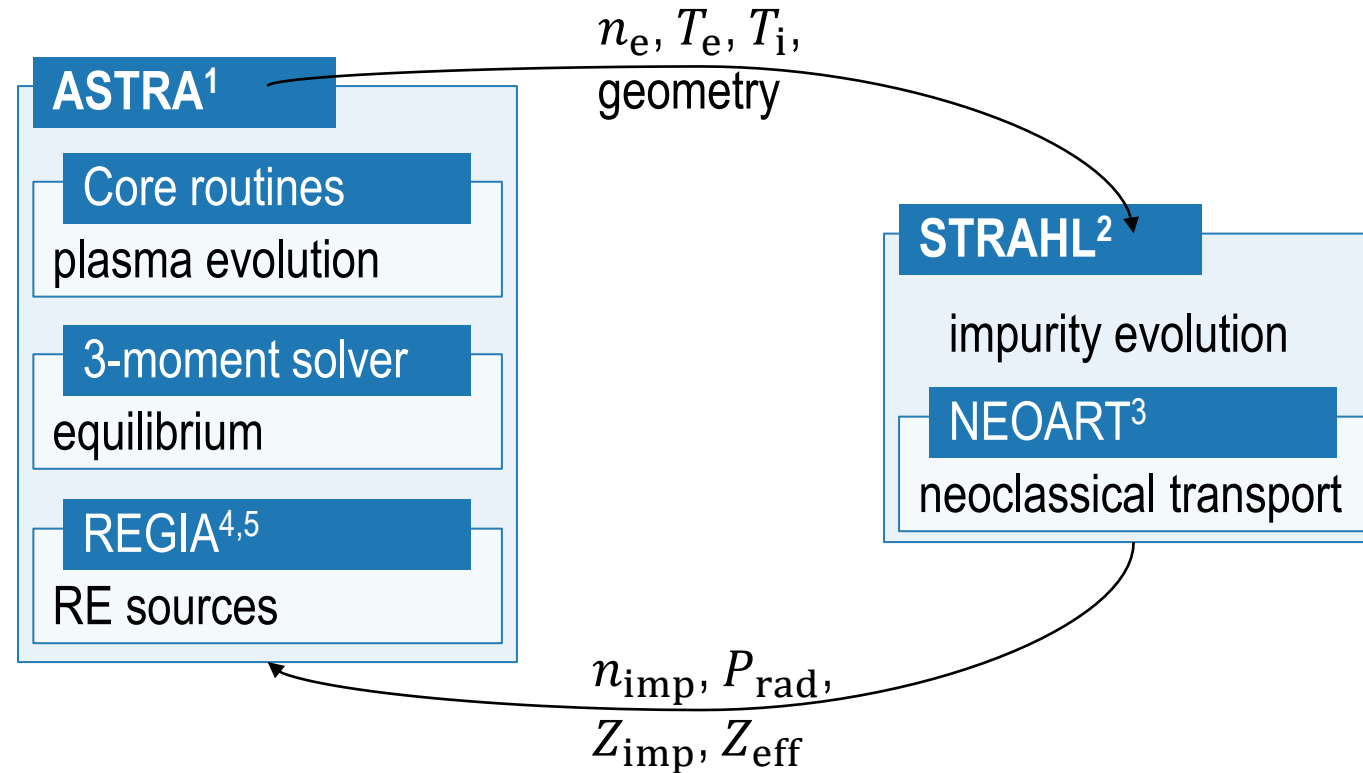
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1. The transport model ASTRA-STRAHL
2. ASDEX Upgrade runaway electron experiments
3. Simulating ASDEX Upgrade #33108
 - a. Runaway electron generation
 - b. The role of impurity transport
 - c. Impact of pre-disruption temperature
4. Conclusions



ASTRA-STRAHL: the coupled transport codes



¹ Fable et al. *Plasma Phys. Control. Fusion* **55**, 074007 (2013)

² Dux et al. *Nucl. Fusion* **39**, 1509 (1999)

³ Peeters. *Phys. Plasmas* **7**, 268 (2000)

⁴ Linder et al. *Nucl. Fusion* **60**, 096031 (2020)

⁵ Linder et al. *J. Plasma Phys.* **87**, 905870301 (2021)

ASTRA-STRAHL: background plasma evolution with ASTRA

Evolution of plasma quantities Y through macroscopic transport equation¹

$$\frac{1}{V'} \frac{\partial}{\partial t} (V' Y) = \frac{1}{V'} \frac{\partial}{\partial \rho} \left(V' \langle (\nabla \rho)^2 \rangle \left[D \frac{\partial Y}{\partial \rho} - v Y \right] \right) + \sum_i S_i$$

Temperatures T_e, T_i

- Ohmic heating
- Impurity radiation
- Electron-to-ion heat exchange
- Rapid transport during breakup of magnetic surfaces^{2,3}
(more on this later)

Poloidal flux Ψ

- Influenced by RE generation
- j_p profile flattened during TQ onset

Electron density n_e

- From quasineutrality

¹ Fable et al. *Plasma Phys. Control. Fusion* **55**, 074007 (2013)

² Linder et al. *Nucl. Fusion* **60**, 096031 (2020)

³ Linder et al. *J. Plasma Phys.* **87**, 905870301 (2021)

ASTRA-STRAHL: impurity evolution with STRAHL

Evolution of plasma quantities Y through macroscopic transport equation

$$\frac{1}{V'} \frac{\partial}{\partial t} (V' Y) = \frac{1}{V'} \frac{\partial}{\partial \rho} \left(V' \langle (\nabla \rho)^2 \rangle \left[D \frac{\partial Y}{\partial \rho} - v Y \right] \right) + \sum_i S_i$$

Impurity densities

- Charge state resolved
- Atomic processes: electron-impact ionization and recombination (coefficients from ADAS¹)
- Neoclassical transport from NEOART²
- Neutral gas propagation at speed of sound
- Rapid transport during breakup of magnetic surfaces^{3,4}
(more on this later)
- Impurity radiation from line radiation, continuum radiation and ionization losses

¹ Summers. The ADAS User Manual, version 2.6.

² Peeters. *Phys. Plasmas* **7**, 268 (2000)

³ Linder et al. *Nucl. Fusion* **60**, 096031 (2020)

⁴ Linder et al. *J. Plasma Phys.* **87**, 905870301 (2021)

ASTRA-STRAHL: Runaway Electron Generation In ASTRA (REGIA)

Evolution of plasma quantities Y through macroscopic transport equation

$$\frac{1}{V'} \frac{\partial}{\partial t} (V' Y) = \frac{1}{V'} \frac{\partial}{\partial \rho} \left(V' \langle (\nabla \rho)^2 \rangle \left[D \frac{\partial Y}{\partial \rho} - v Y \right] \right) + \sum_i S_i$$

Runaway electron current density

- Runaway sources S_i from standalone Fortran module (github.com/o-linder/runawayelectrongeneration)
- Separate populations of RE due to different generation mechanisms
- Average velocity $\langle v_{RE} \rangle = c$
- No RE losses
- Feed-back on Ψ evolution

Fortran module¹

- **Dreicer generation**
 - Classical model by Connor & Hastie²
 - CODE neural network by Hesslow *et al*³
- **Hot-tail generation**
 - Model by Smith & Verwichte⁴
- **Avalanche generation**
 - Classical model by Rosenbluth & Putvinski⁵
 - High-Z model by Hesslow *et al*⁶
- **Nuclear generation:** not implemented
(*Recall, application to ASDEX Upgrade*)

¹ Linder et al. *Nucl. Fusion* **60**, 096031 (2020)

² Connor et al. *Nucl. Fusion* **15**, 415 (1975)

³ Hesslow et al. *J. Plasma Phys.* **85**, 475850601 (2019)

⁴ Smith et al. *Phys. Plasmas* **15**, 072502 (2008)

⁵ Rosenbluth et al. *Nucl. Fusion* **37**, 1355 (1997)

⁶ Hesslow et al. *Nucl. Fusion* **59**, 084004 (2019)

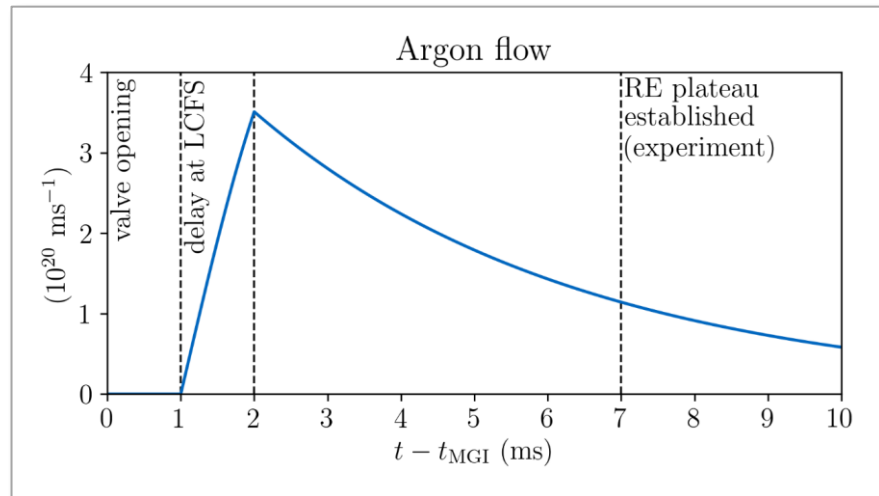
ASTRA-STRAHL: Description of MGI and TQ

Massive gas injection

- Outflow from gas valve described by continuity equation¹
- Inward propagation with thermal velocity (for Ar):

$$v_{th} = \sqrt{T/m} = 246 \text{ m/s}$$

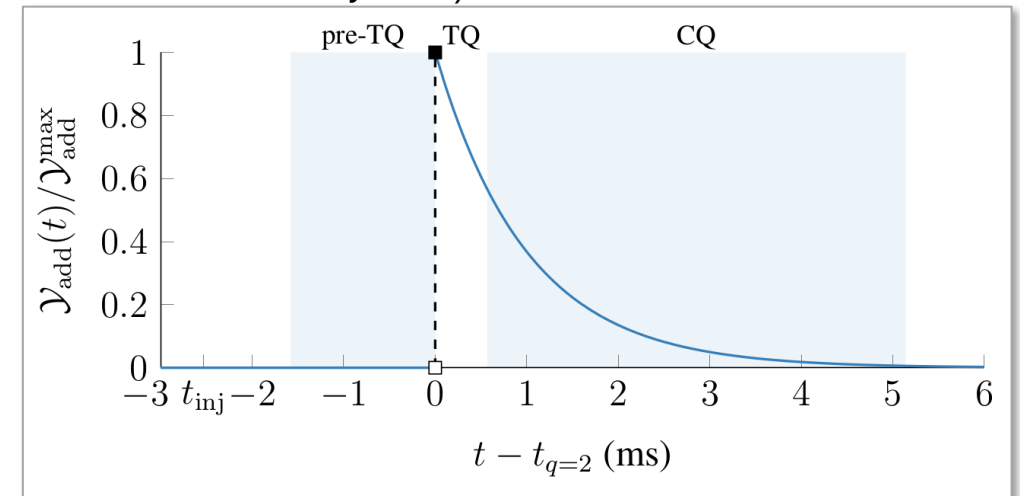
- In AUG: valve opens within 1 ms
- In ASTRA: source located 1 cm outside LCFS
→ 1 ms delay
(no need to model propagation from valve to LCFS)



¹Pautasso et al. *Nucl. Fusion* **47**, 900 (2007)

Break-up of magnetic surfaces / onset of TQ

- Cold gas front reaches $q = 2$ surface, triggers $(m, n) = (2, 1)$ MHD modes (+ higher harmonics)
- In experiment: flattens j_p profile, drop in l_i , I_p spike
- In ASTRA^{2,3}: j_p flattened when $\left| \frac{dj_p}{d\rho} \frac{1}{j_p} \right| > 50$ at $q = 2$
- Additional transport: $\gamma_{add}(t) = \gamma_{add}^{max} \exp\left(-\frac{t-t_{q=2}}{\tau_{add}}\right)$
(more on the necessity later)



²Linder et al. *Nucl. Fusion* **60**, 096031 (2020)

³Linder et al. *J. Plasma Phys.* **87**, 905870301 (2021)

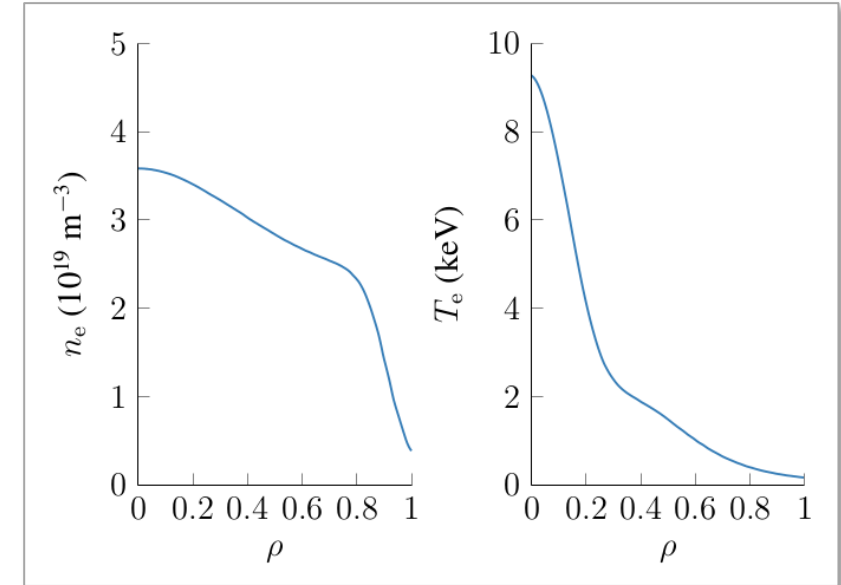
ASDEX Upgrade runaway electron experiments¹⁻³

MGI in AUG #33108

- Circular L-mode limiter plasma
- Low density ($3 \times 10^{19} \text{ m}^{-3}$), high temperature (9 keV)
- Central ECRH (2.6 MW)
- Argon injection ($0.73 \text{ bar} \times 100 \text{ cm}^3 \sim 7 N_D$)

Application

- Used as base case for simulations
- Similar discharges selected for comparison of simulations with experimental trend
(*impact of T_e*)



Quantity	AUG #33108	similar shots
$I_{p,0}$ (MA)	0.76	0.60 – 0.90
p_{Ar} (bar)	0.73	0.60 – 0.85
B_{tor} (T)	2.50	2.30 – 2.70
q_{95}	3.79	3.50 – 4.10

¹ Pautasso et al. *Nucl. Fusion* **55**, 033015 (2015)

² Pautasso et al. *Plasma Phys. Control. Fusion* **59**, 014046 (2017)

³ Pautasso et al. *Nucl. Fusion* **60**, 086011 (2020)

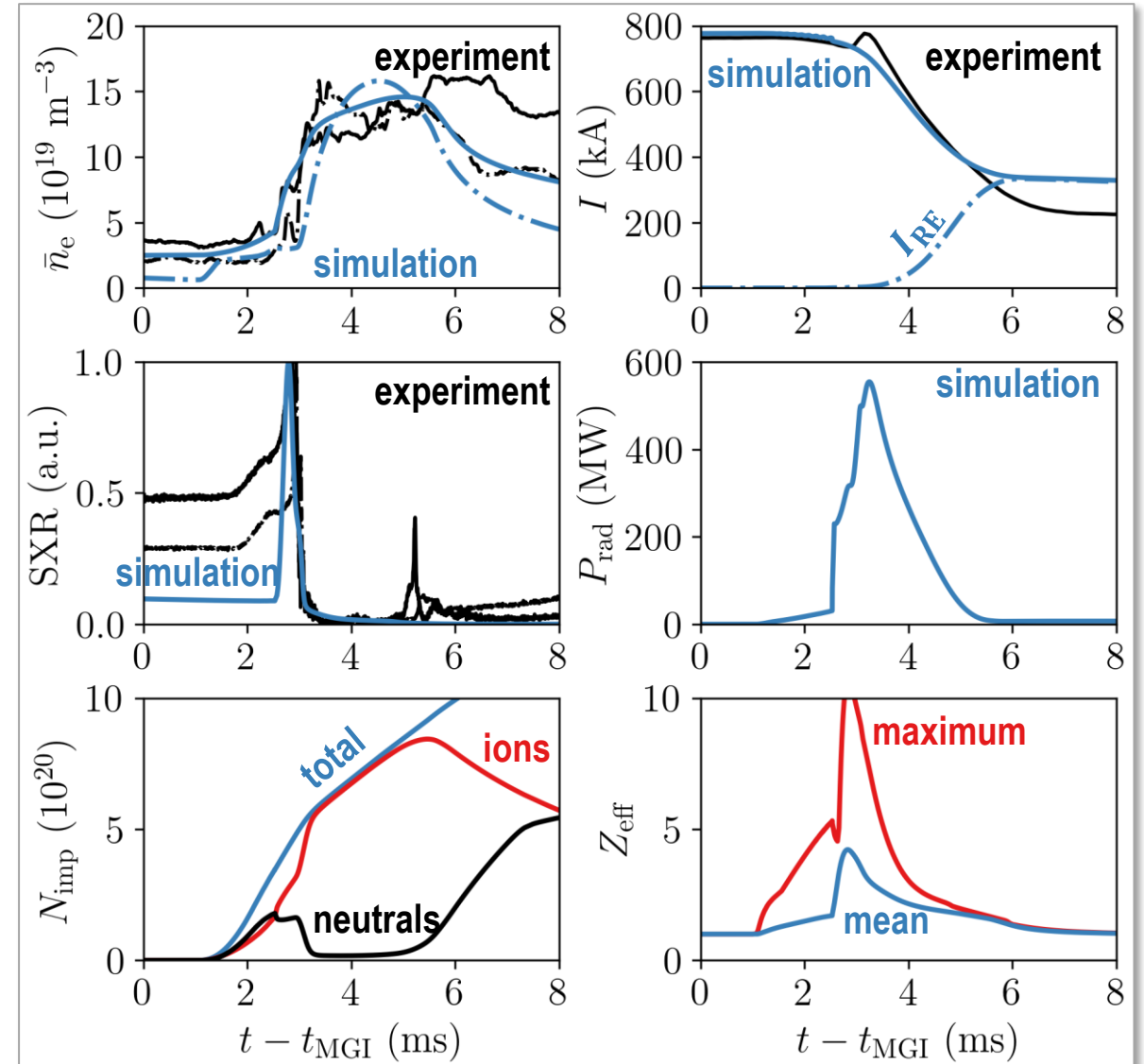
Simulating ASDEX Upgrade #33108

Key experimental observations reproduced

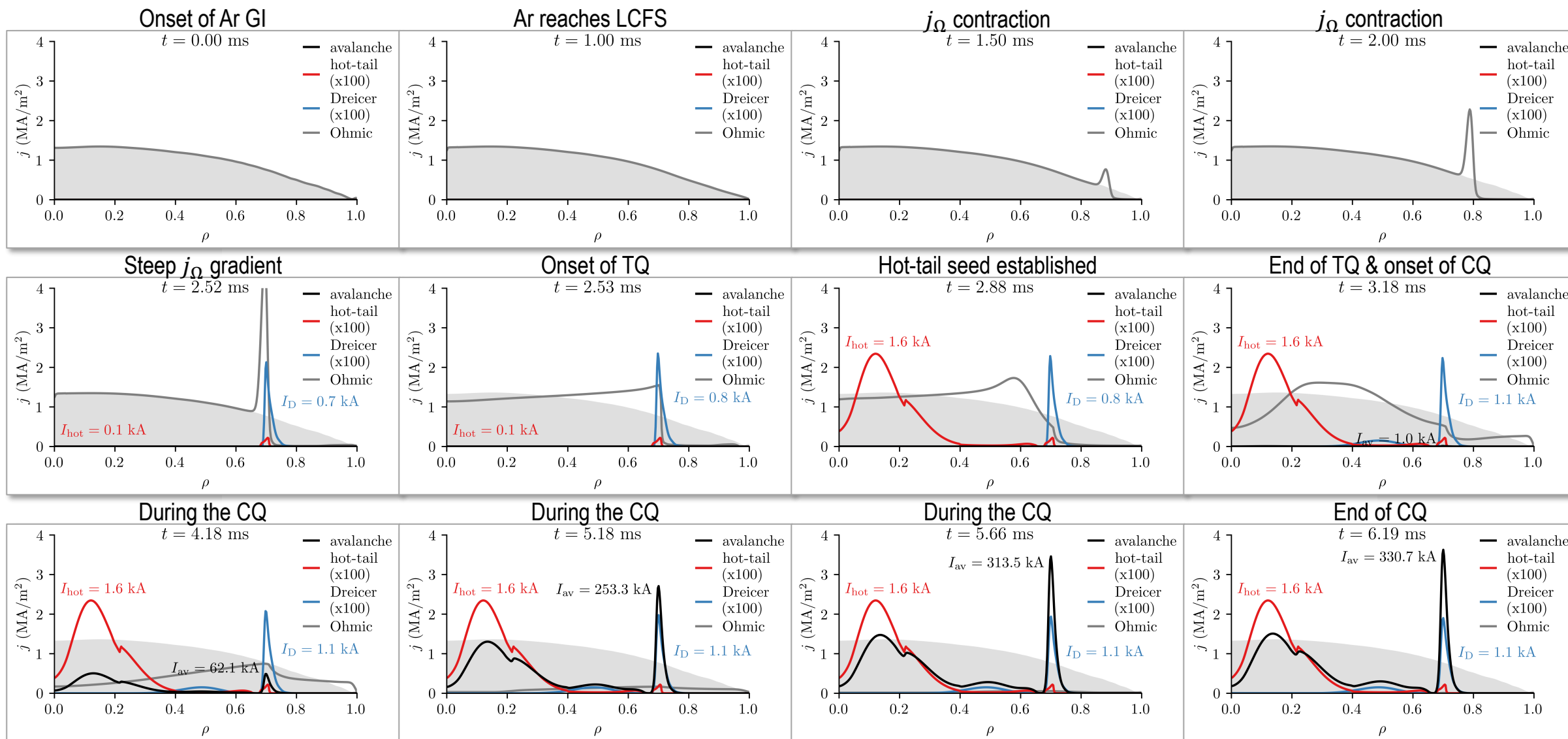
- Increase of electron density \bar{n}_e
- Decay of plasma current I_p
- Occurrence of TQ

Simulation features

- Density increase reproduced
→ current decay reproduced
- Density increase requires additional transport
 $D = 100 \text{ m}^2/\text{s}, \quad v = -1000 \text{ m/s},$
 $\tau = 1.0 \text{ ms}$
- Thermal energy dissipated by impurity radiation
- Ohmic heating during CQ → prolonged radiation
- Distinct phases of disruption covered
(pre-TQ, TQ, CQ)



Runaway electron generation: current evolution



Runaway electron generation: contributions

Seed generation

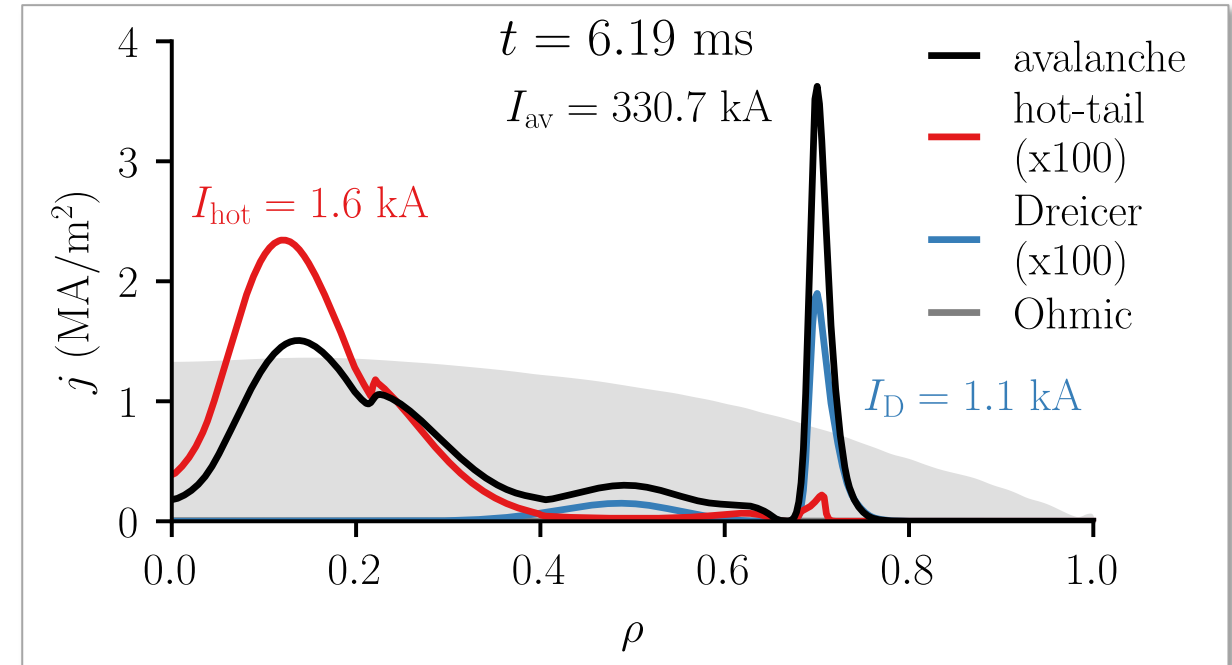
- Only a few kA
- Similar contributions by hot-tail & Dreicer mechanisms

Avalanching

- Seed multiplication
 - Generates 331 kA of REs
 - Final RE beam avalanche dominated
- RE seed of minor importance
(varying strength & composition)

Experimental comparison

- Higher I_{RE} simulated due to absence of RE losses



Runaway electron generation: impact of the RE seed

Comparison with only one seed mechanism used

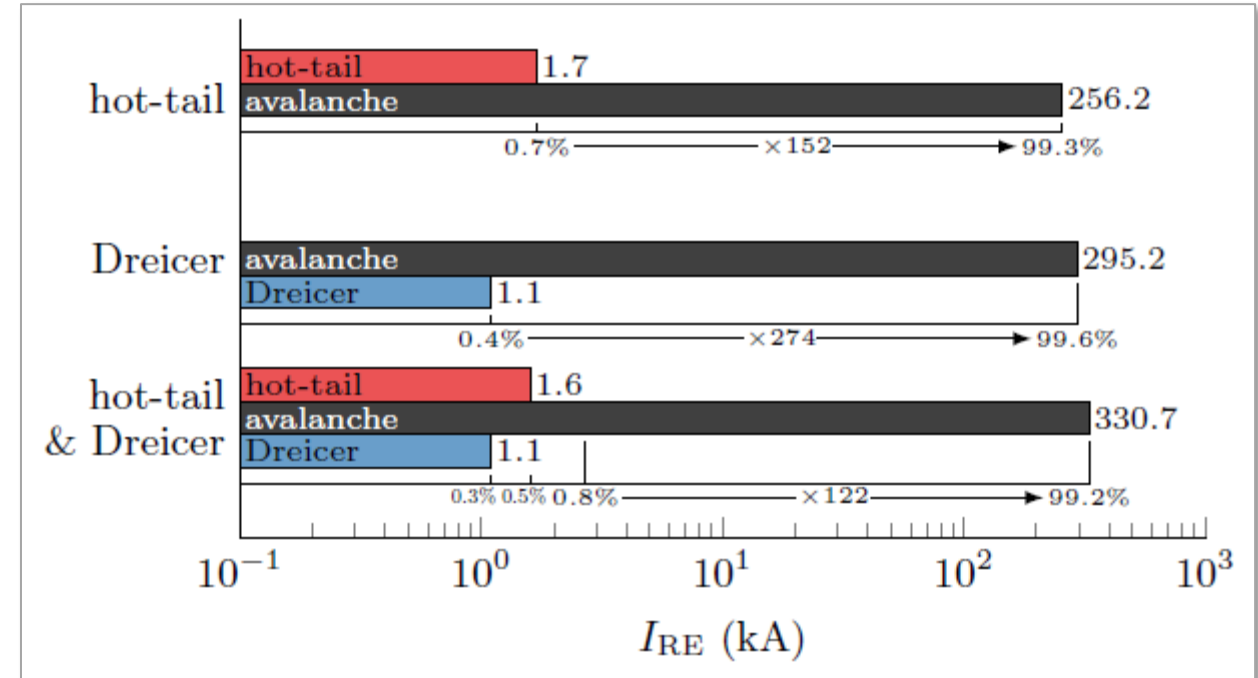
- Reduction of I_{RE}^{seed} does not affect RE multiplication with equal weight:

$$\text{hot-tail: } -37\% I_{RE}^{seed} \rightarrow -23\% I_{av}$$

$$\text{Dreicer: } -59\% I_{RE}^{seed} \rightarrow -11\% I_{av}$$

- Decay of I_{Ω} at similar time scales, avalanche multiplication time determines post-CQ I_{RE} (feedback on Ψ -evolution)

→ **Exact strength of RE seed is of secondary importance due to dominating avalanche generation**



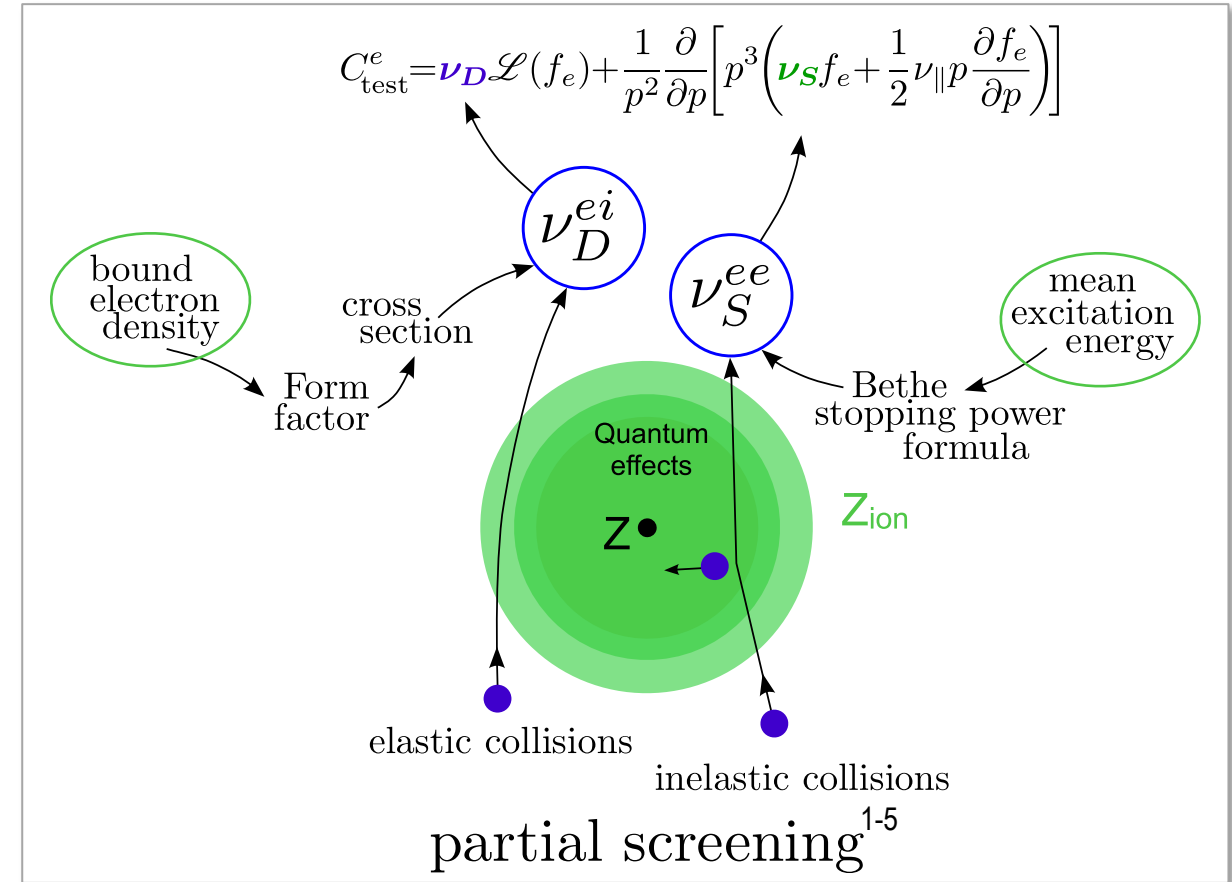
Runaway electron generation: impact of partially ionized impurities

Impact of partially ionized impurities¹⁻⁵

- Increased electron-ion friction → hinders runaway
- Relevant in MGI scenarios
- Classical formulae⁶⁻⁷ assume full ionization
- Effects considered in state-of-the-art models⁴⁻⁵

ASTRA-STRAHL simulations⁸

- Assess importance of partial screening in self-consistent simulations:
state-of-the-art⁴⁻⁵ ↔ classical⁶⁻⁷



¹ Hesslow et al. *Phys. Rev. Lett.* **118**, 255001 (2017)

² Hesslow et al. *Plasma Phys. Control. Fusion* **60**, 074010 (2018)

³ Hesslow et al. *J. Plasma Phys.* **84**, 905840605 (2018)

⁴ Hesslow et al. *Nucl. Fusion* **59**, 084004 (2019)

⁵ Hesslow et al. *J. Plasma Phys.* **85**, 475850601 (2019)

⁶ Connor et al. *Nucl. Fusion* **15**, 415 (1975)

⁷ Rosenbluth et al. *Nucl. Fusion* **37**, 1355 (1997)

⁸ Linder et al. *Nucl. Fusion* **60**, 096031 (2020)

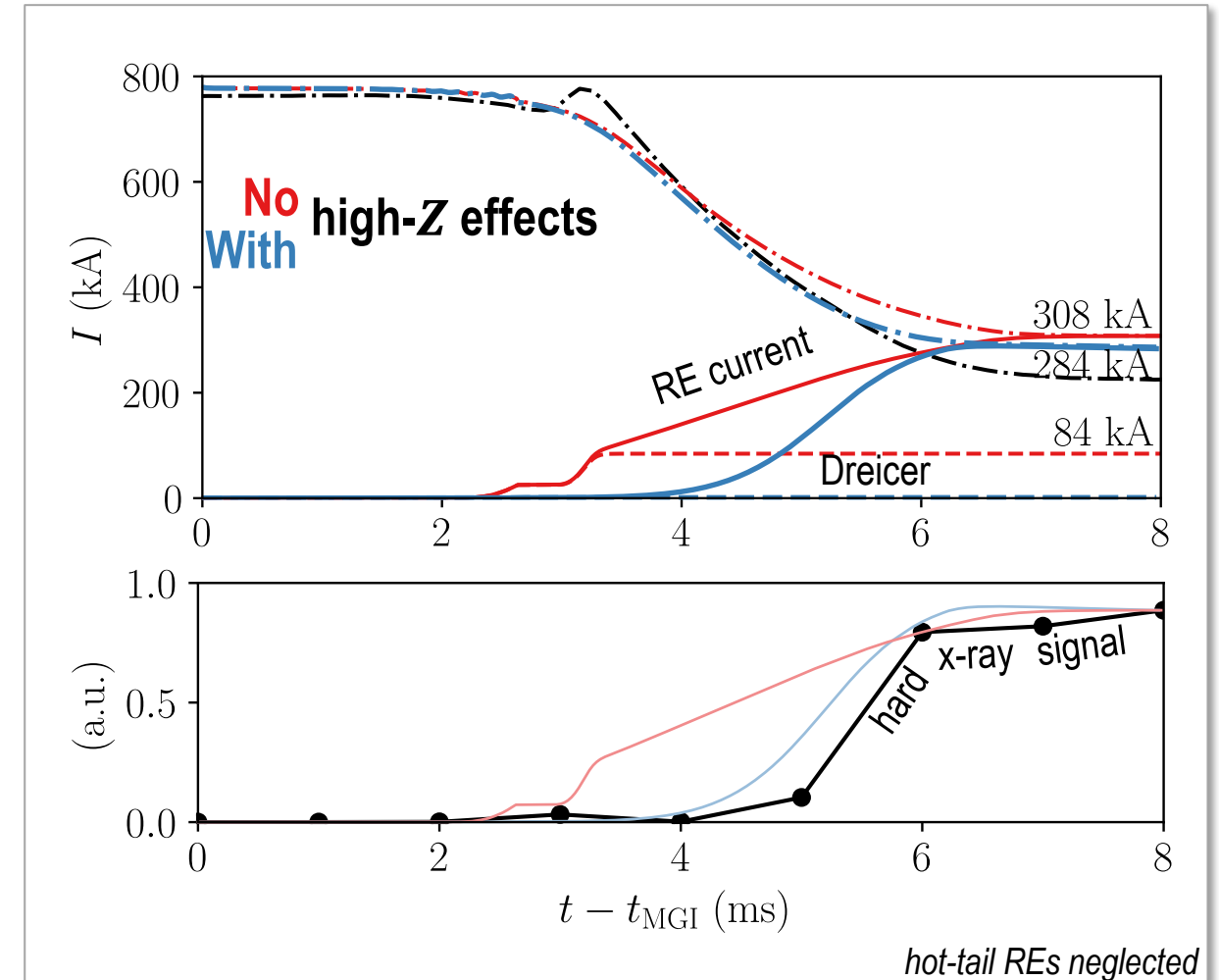
Runaway electron generation: model validation

Absence of high-Z effects

- Dreicer generation overestimated
(earlier onset & stronger, 84 kA)
- Avalanche multiplication reduced
(slower rise of RE current during CQ)
- Decay of total current slowed down
→ less Ohmic heating, less radiation
- Final I_{RE} similar, but different composition
- Hard x-ray signal: High I_{RE} only at end of CQ

→ Simulations consistent with experiment only when considering high-Z effects

→ High-Z interactions important for runaway!



The role of impurity transport: impact of transport mechanisms

Mechanisms considered

- Rapid redistribution
(MHD effects due to breakup of magnetic surfaces)
- Neoclassical effects

Absence of rapid redistribution

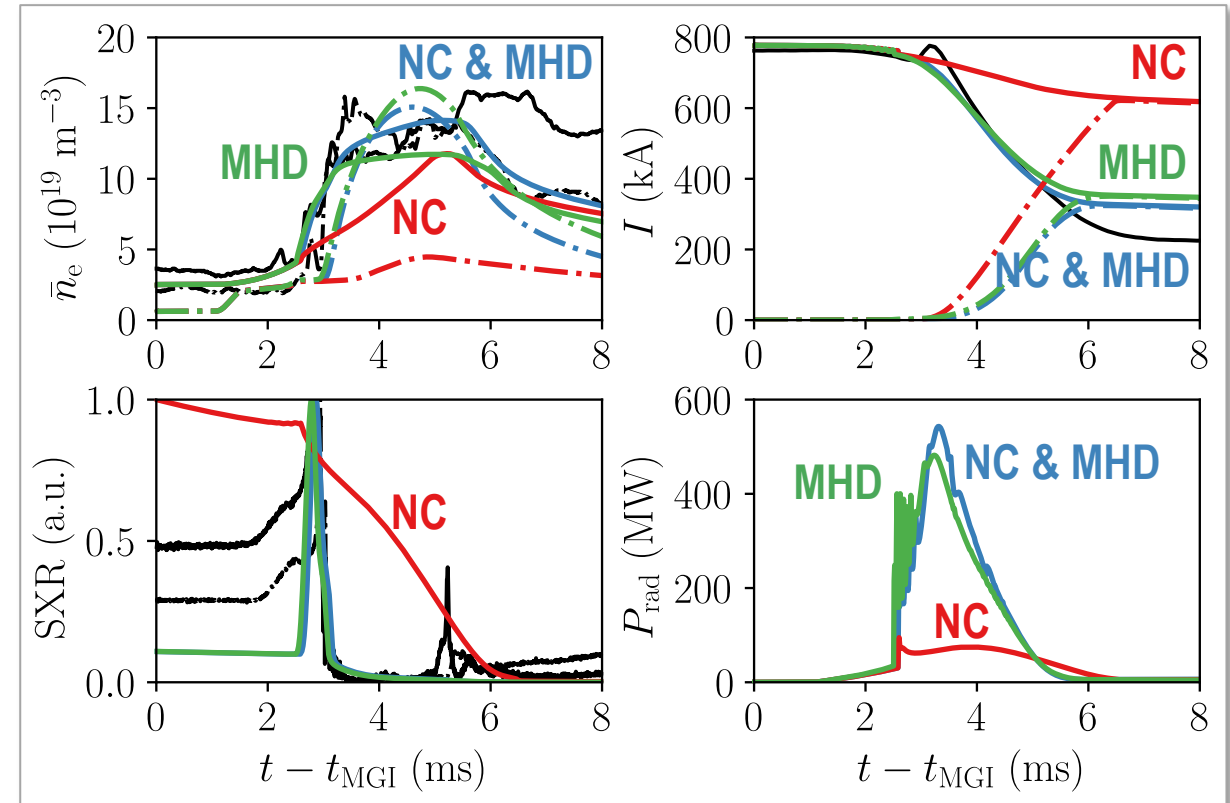
- Impurity propagation driven by neutral gas
- Increase of electron density \bar{n}_e not matched

→ **Much slower TQ!**

Absence of neoclassical effects

- Inward transport less effective

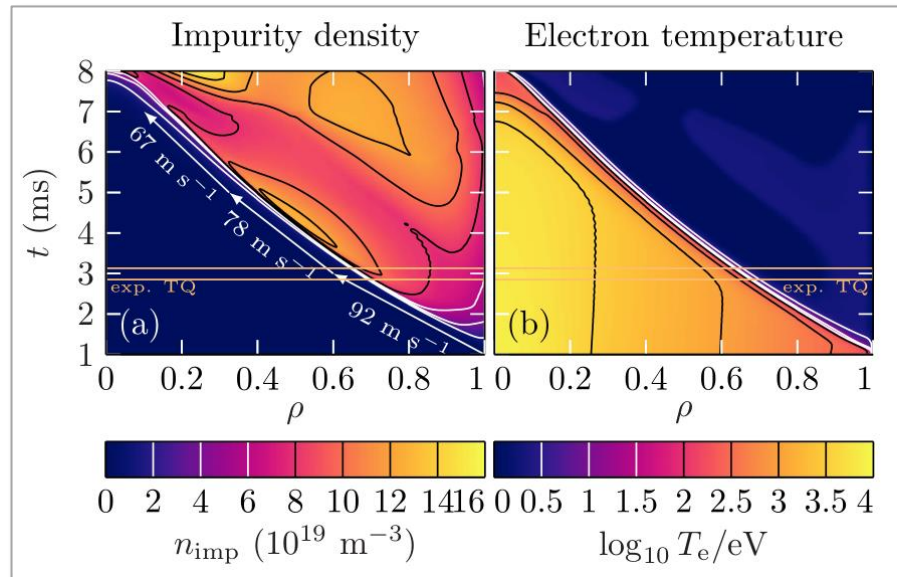
→ **Rapid redistribution & neoclassical effects relevant for impurity transport**



The role of impurity transport: rapid redistribution

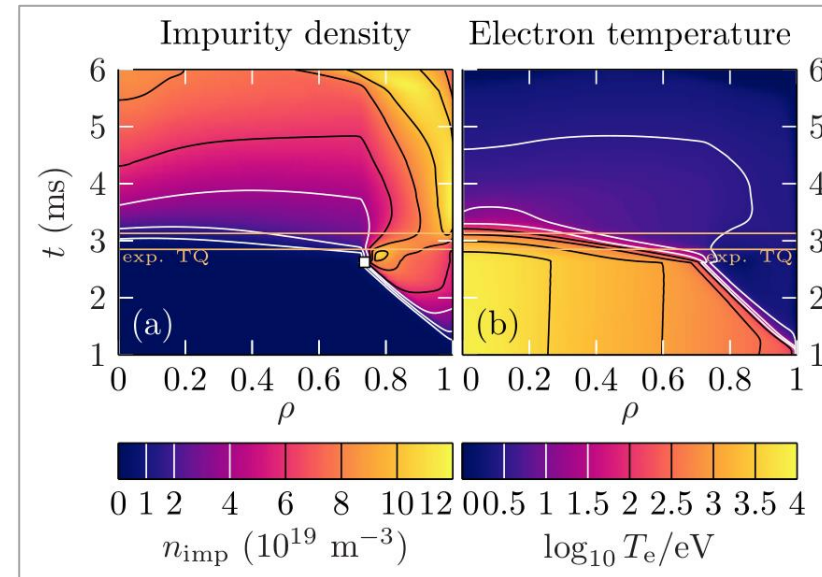
Absence of rapid redistribution

- Impurity propagation driven by neutral gas
- Slow TQ over several ms



Considering rapid redistribution

- Central impurity density increases during CQ
- TQ on experimental sub-ms time scales
- Note, only order of magnitude values used:
 $D = 100 \text{ m}^2/\text{s}, \quad v = -1000 \text{ m/s},$
 $\tau = 1.0 \text{ ms}$
(variation by around 50% describes experiment adequately)



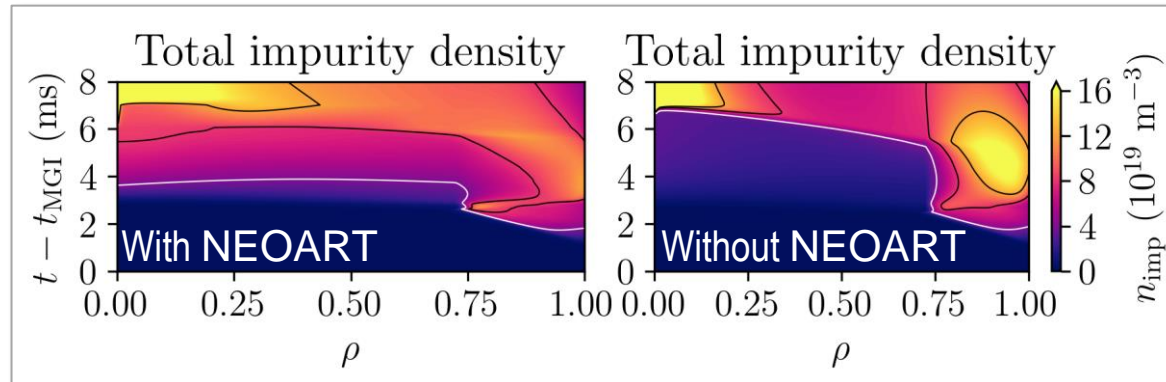
The role of impurity transport: neoclassical transport

In absence of additional transport

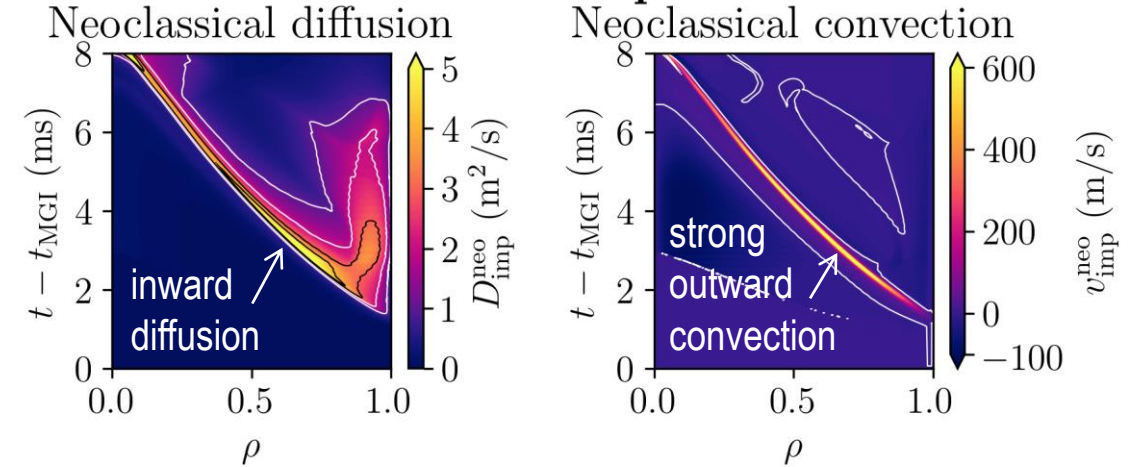
- Diffusion & strong outward convection almost cancel
- Propagation driven by neutrals
- Slow inward propagation of material

With additional transport

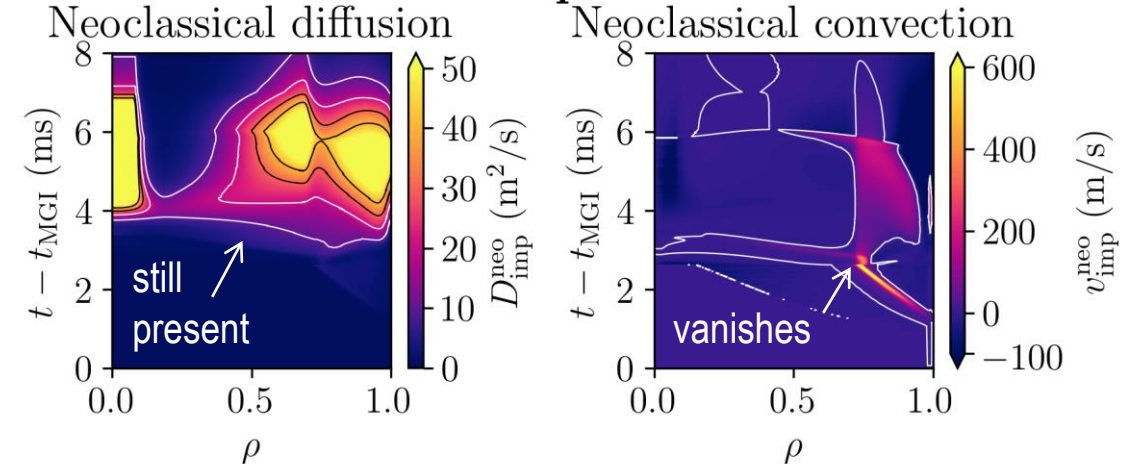
- Outward convection vanishes; diffusion present
- Neoclassical transport contributes noticeably to inward transport
(current decay too slow in absence of neoclassical effects)



Without additional transport



With additional transport



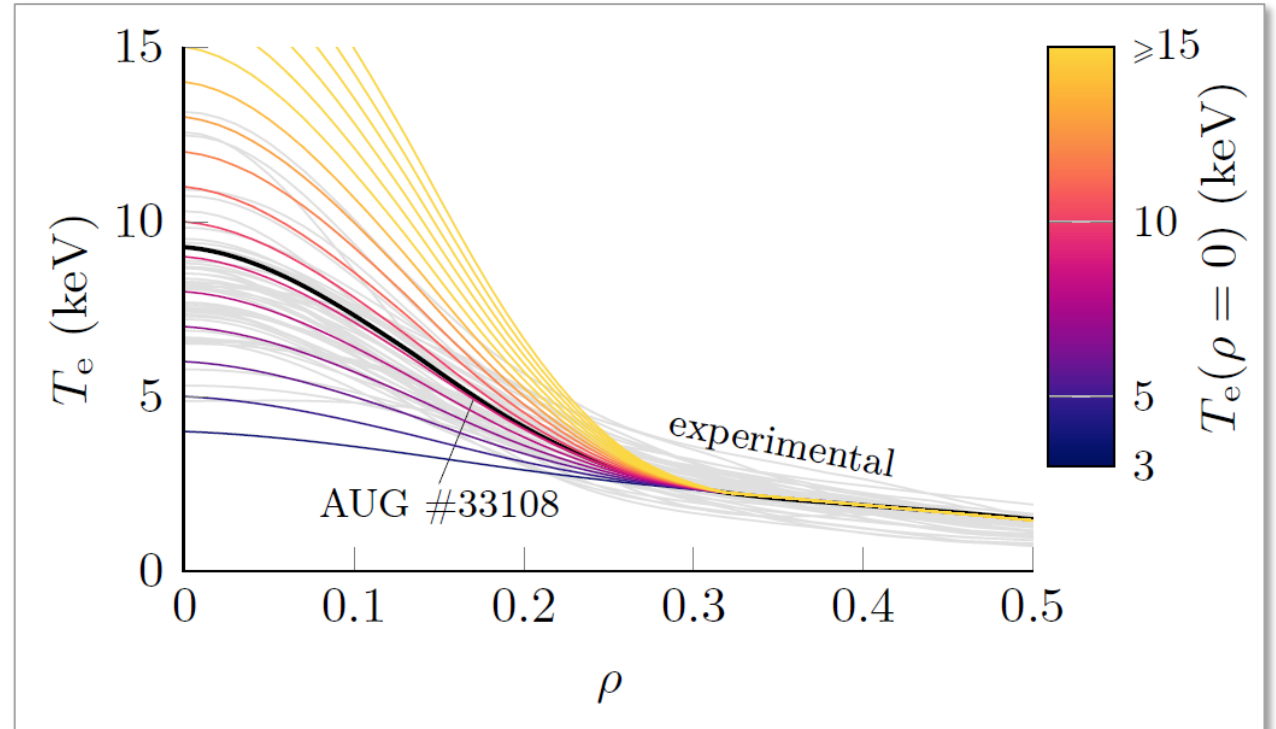
Impact of pre-disruption temperature: simulation setup

Setup

- In AUG experiments, on-axis ECRH during last 0.1 ms prior to MGI
- Scale ECRH contribution of $T_e(\rho)$ in AUG #33108

$$T_e(\rho) = \underbrace{\frac{T_{\text{tar}} - T_{\text{bg}}(0)}{T_{\text{ECRH}}(0)}}_{\text{target}} T_{\text{ECRH}}(\rho) + \underbrace{T_{\text{bg}}(\rho)}_{\text{background}}$$

- Temperature unaffected for $\rho > 0.35$



Impact of pre-disruption temperature: the RE seed

Dreicer population

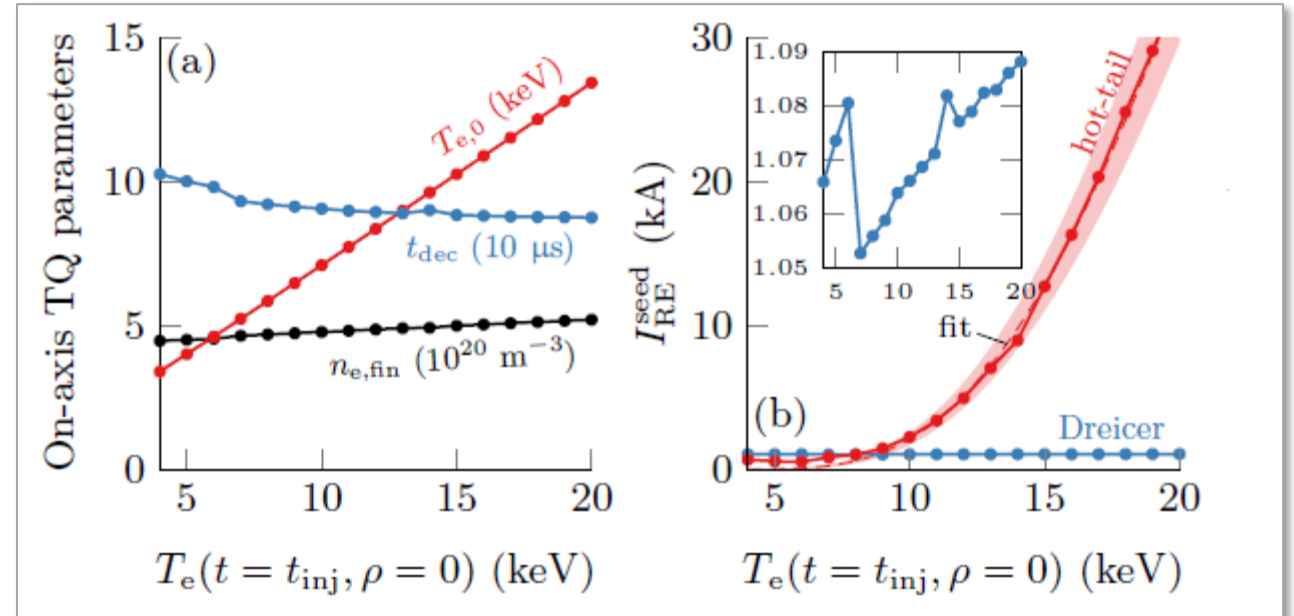
- Virtually unaffected: $I_D = 1.1$ kA
- No (significant) T_e change in region of strongest generation

Hot-tail population

- Grows exponentially
 $I_{\text{hot}}: 0.6 \text{ kA} \rightarrow 33.7 \text{ kA}$
- Strongest increase above 10 keV
- Described by exponential

$$I_{\text{hot}}^{\text{fit}}(T_{e,0}(\rho = 0)) = (914 \pm 58) \exp \left(-4 \left\{ \frac{\tilde{\nu} \ln \Lambda(t_0) \langle n_{e,\text{fin}} t_{\text{dec}} \rangle}{T_{e,0}(\rho = 0)^{3/2}} \right\}^{2/3} \right) \text{ kA}$$

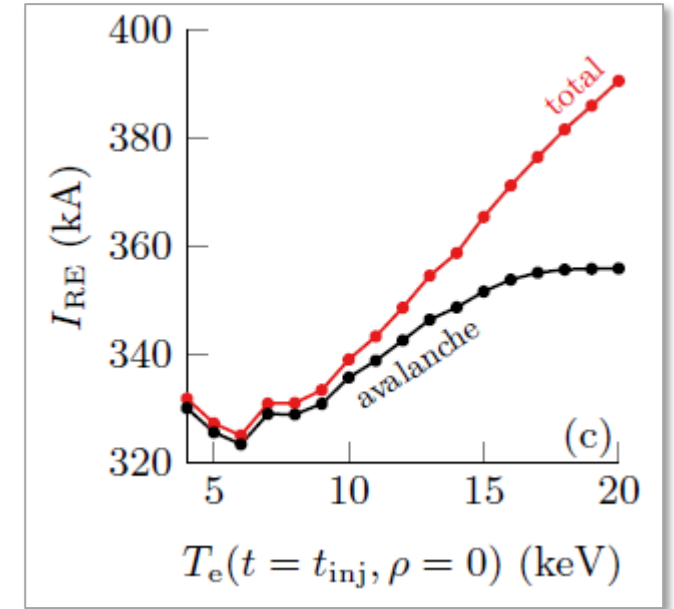
- Strong increase of temperature (by design), but density not at similar rate
→ **Strong increase of hot-tail runaway for hotter plasmas**



Impact of pre-disruption temperature: avalanche & total current

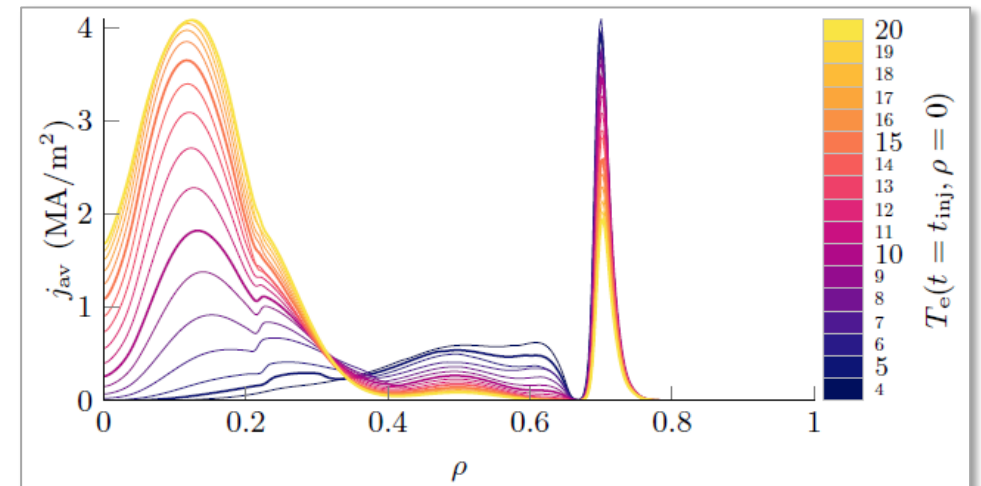
Multiplication

- Avalanche (& total) RE current ~ 330 kA for $T_e < 9$ keV
- Between 9 keV and 17 keV, I_{av} increases
(additional multiplication between 2 – 3)
- Avalanche current saturates for $T_e > 17$ keV at 356 kA
- Radial distribution of j_{av} changes (as hot-tail becomes more important):
mid radius & $q = 2 \rightarrow \rho \sim 0.12$



Total current

- For $T_e > 9$ keV, grows linearly due to hot-tail contribution
 - At $T_e = 20$ keV, hot-tail constitutes 9% I_{RE}
- **Relative importance of multiplication decreases due to finite poloidal magnetic flux available**
(less avalanching in ITER?)



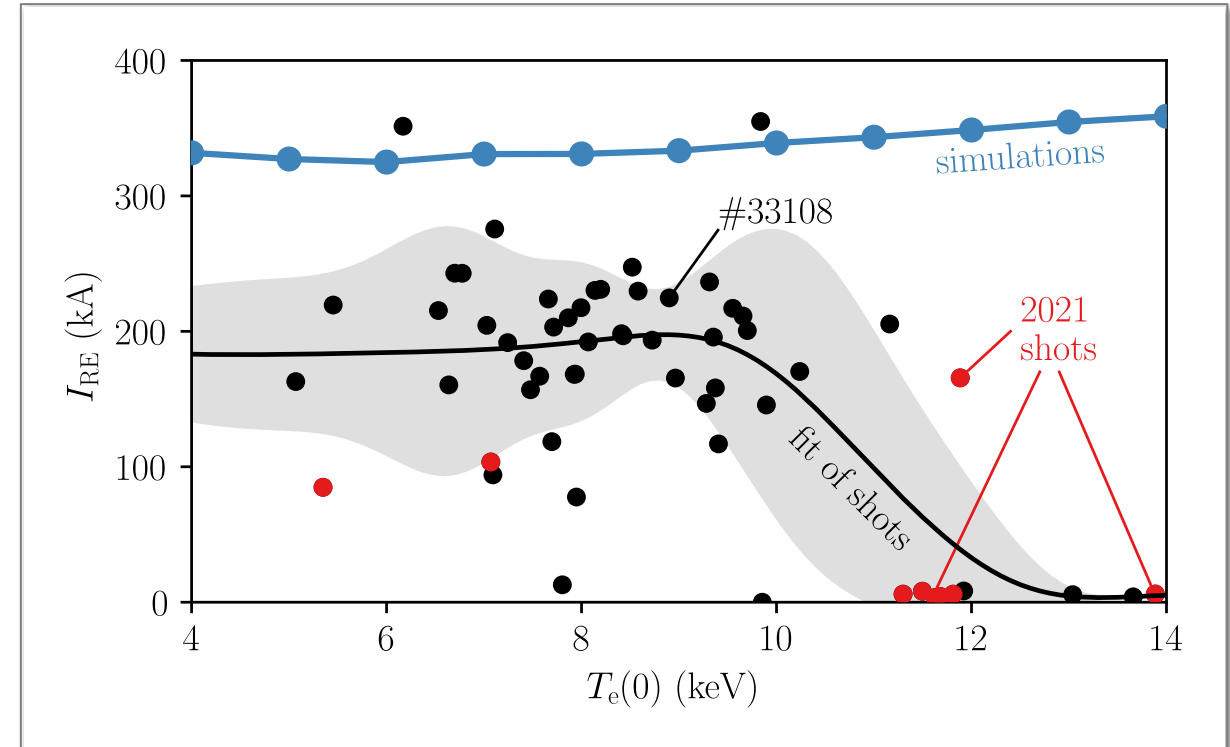
Impact of pre-disruption temperature: experimental comparison

For $T_e < 9$ keV

- RE current \sim constant (experiment & simulation)
- Simulated I_{RE} larger due to absence of RE losses


For $T_e > 9$ keV

- In simulation, I_{RE} increasing (hot-tails)
- None in experiment at $T_e > 12$ keV
- In 2021 campaign, one discharge with RE beam close to 12 keV
- Reason: Loss of RE seed during breakup of magnetic surfaces?





Further reading

More details on self-consistent ASTRA-STRAHL simulations of Ar MGI in ASDEX Upgrade #33108 are presented in the following publications:



PAPER


Self-consistent modeling of runaway electron generation in massive gas injection scenarios in ASDEX Upgrade

O. Linder¹ , E. Fable¹, F. Jenko¹, G. Papp¹ , G. Pautasso¹, the ASDEX Upgrade team^{2,1} and the EUROfusion MST1 team^{3,1}


Published 18 August 2020 • © EURATOM 2020

[Nuclear Fusion](#), Volume 60, Number 9

Citation O. Linder *et al* 2020 *Nucl. Fusion* 60 096031

 Article PDF

Linder et al. *Nucl. Fusion* **60**, 096031 (2020)
<https://doi.org/10.1088/1741-4326/ab9dcf>





JOURNAL OF PLASMA PHYSICS

Journal of Plasma Physics





Electron runaway in ASDEX Upgrade experiments of varying core temperature

Published online by Cambridge University Press: 07 May 2021

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Abstract

The formation of a substantial postdisruption runaway electron current in ASDEX Upgrade material injection experiments is determined by avalanche multiplication of a small seed population of runaway electrons. For the investigation of these scenarios, the runaway electron description of the coupled 1.5-D transport solvers ASTRA-STRAHL is amended by a fluid model describing electron runaway caused by the hot-tail mechanism. Applied in

Linder et al. *J. Plasma Phys.* **87**, 905870301 (2021)
<https://doi.org/10.1017/S0022377821000416>

Conclusions

1. **Successful ASTRA-STRAHL simulations of RE dynamics on ASDEX Upgrade**
(background plasma, MGI, RE generation)
2. **High- Z effects important for RE generation**
3. **Impurity transport due to MHD & neoclassical effects**
4. **Discrepancies w.r.t. experiment in high T_e scenarios suggest seed RE loss**

- CONNOR, J.W. and HASTIE, R.J.. Relativistic limitations on runaway electrons. *Nucl. Fusion* **15**, 415 (1975)
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- SMITH, H.M. & VERWICHTE, E.. Hot tail runaway electron generation in tokamak disruptions. *Phys. Plasmas* **15**, 072502 (2008)
- SUMMERS, H.P. The ADAS User Manual, version 2.6. <https://www.adas.ac.uk>.

Appendix: Average runaway electron velocity

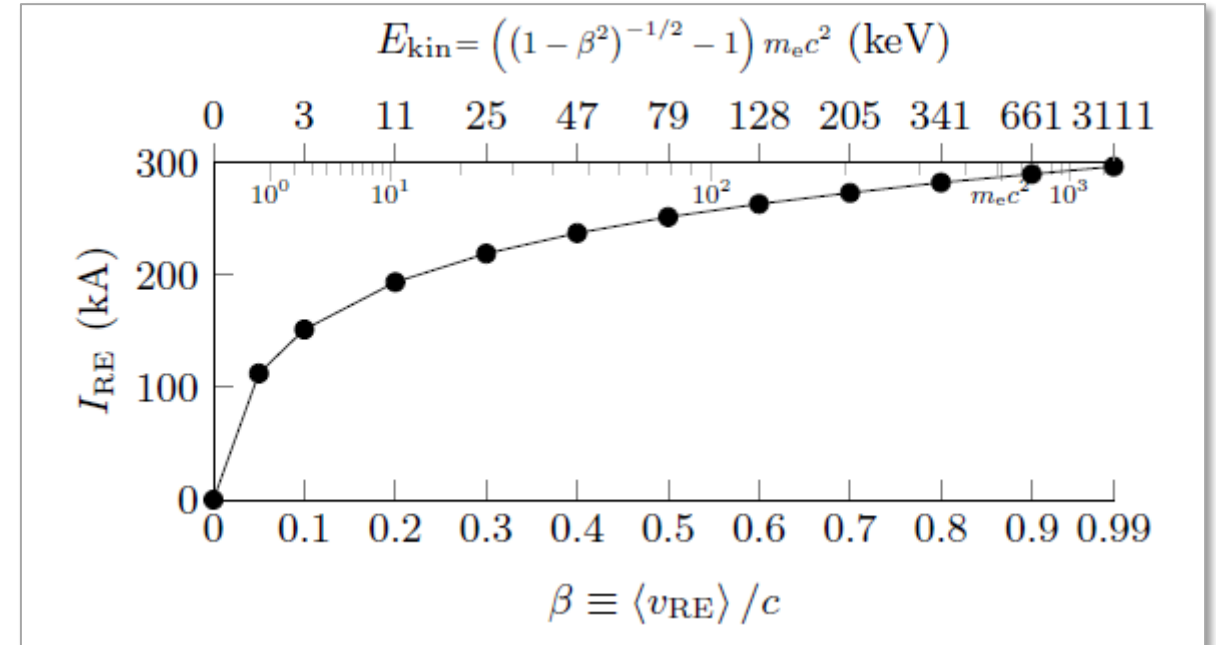
Impact of assumption $\langle v_{RE} \rangle = c$

- Valid for $E_{\text{kin}} \geq 3.1 \text{ MeV}$
($\leq 1\%$ deviation)
- Conditions not fulfilled during early stages
- Yet, reduction of $\langle v_{RE} \rangle$ to below c
→ slight decrease of I_{RE}
(only assuming $E_{\text{kin}} \sim T_{e,0}$: strong decrease)
- Reduction of $\langle v_{RE} \rangle \equiv$ reduction of seed population!
(mathematically)

$$\frac{\partial j_{\text{seed}}}{\partial t} = e \langle v_{RE} \rangle S_{\text{seed}} = e (c\beta) S_{\text{seed}} = ec (\beta S_{\text{seed}})$$

$$\frac{\partial j_{\text{av}}}{\partial t} = e \langle v_{RE} \rangle n_{RE} \tilde{S}_{\text{av}} = (j_{\text{av}} + j_{\text{seed}}) \tilde{S}_{\text{av}}$$

- **Avalanche contribution not affected proportionally;
total current only somewhat reduced**
(same argument as before!)



Appendix: Off-axis hot-tail density peaking

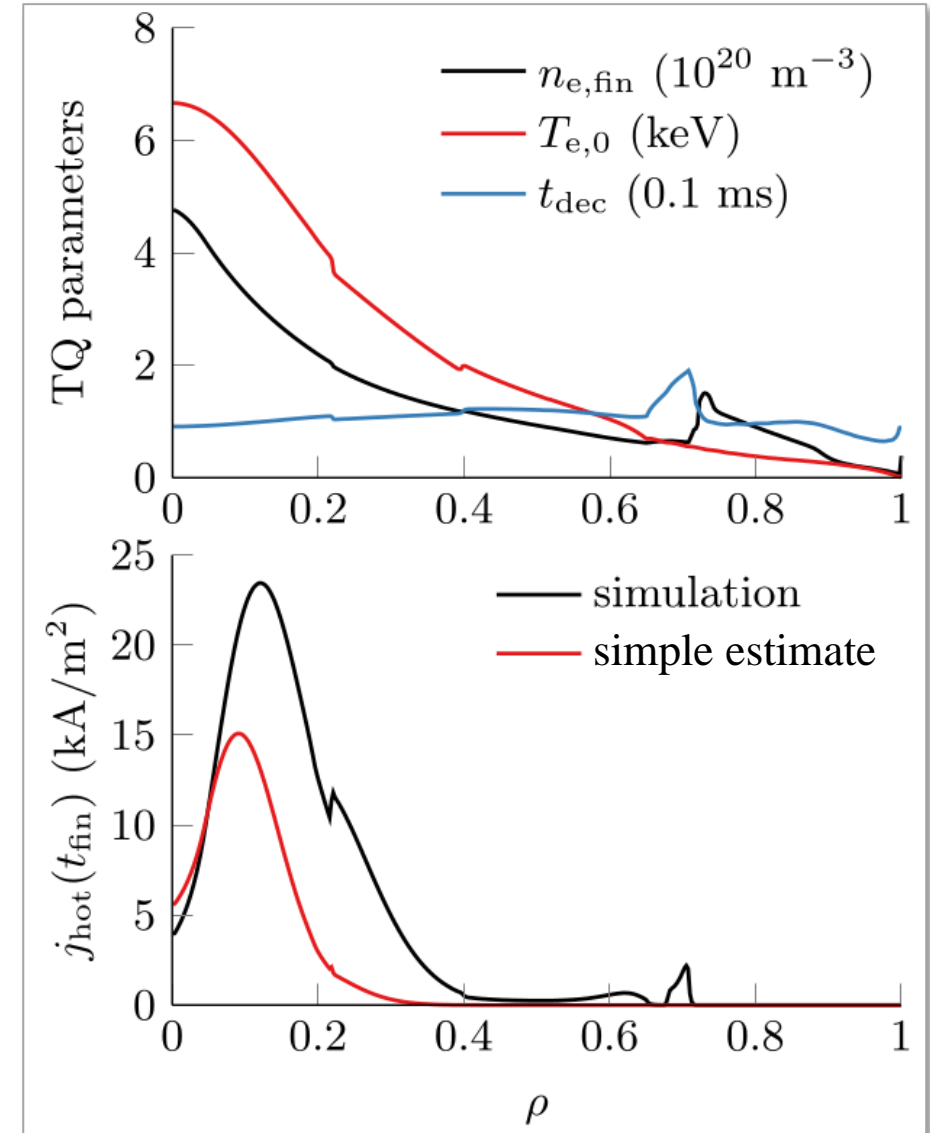
Important parameters for hot-tail generation¹

Simple estimate²

$$n_{\text{hot}}^{\text{simple}}(t_{\text{fin}}) \propto n_{\text{e},0} \exp\left(-4 \tilde{v} \frac{n_{\text{e,fin}}^{2/3} t_{\text{dec}}^{2/3}}{T_{\text{e},0}}\right)$$

- Pre-disruption temperature $T_{\text{e},0}$
- Decay time scale t_{dec}
- Post-disruption density $n_{\text{e,fin}}$

→ **Off-axis hot-tail peaking due to on-axis density peaking post-TQ**



¹ Smith et al. *Phys. Plasmas* **15**, 072502 (2008)

² Linder et al. *J. Plasma Phys.* **87**, 905870301 (2021)